

CEMİL KAYMAK

1.8.2008 / P.tes:

Denizle

**GEOMETRİ İÇİN  
BEYAZ BİR SAYFA AÇIN.**

**Ahmet DEMİR**

Bu kitapların her hakkı saklıdır. Hangi amaçla olursa olsun, testlerin tamamının veya bir kısmının Ahmet DEMİR'in yazılı izni olmadan kopya edilmesi, fotoğraflarının çekilmesi, herhangi bir yolla çoğaltıması, yayımılanması ya da kullanılması yasaktır. Bu yasağa uymayanlar gerekli cezai sorumluluğu ve soruların hazırlanmasındaki mali külfeti peşinen kabullenmiş sayılır.

**2008 Ağustos**

**Dizgi:**

Mesut ANAR

Meva KOCAARSLAN

Şükran SALTIK

Kitap için eleştirilerinizi veya taleplerinizi  
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Tel: 0505 680 53 86

## **Sevgili Öğrenciler**

Geometri dersi üniversiteye hazırlanan her öğrenci için temel derslerden biridir. Yeni sınav sistemi ile beraber bu dersin önemi daha da artmıştır.

Kitaptaki sorular, bu dersi yeni öğrenecek öğrenciler için kolaydan zora doğru hazırlanmıştır. Bir konu içerisinde bulunan tüm soruları öğrenci çözdükten sonra o konu ile ilgili tüm önyargıları kırarak diğer kaynaklardan çok daha rahat bir şekilde çalışmalarını yürütebilecektir. Böylelikle sağlam bir çalışma ile gireceği tüm sınavlarda bu dersle ilgili en yüksek puana ulaşacaktır.

Bu dersin tüm konuları birbiriyle bağlantılıdır. Konuların birbiriyle bağlantısı, soruların birbiriyle bağlantısı ile desteklenmiştir. İlk sorulardan itibaren kullanılan sayılar ve soru kalıpları sonraki konular içerisinde konularına uygun bir şekilde yerleşmiştir. Amacımız öğrencinin zamanla soruları daha hızlı bir şekilde çözmeyi sağlamaktır.

Kitabın bir başka özelliği ise o hafta anlatılan bir konunun bitmemesi durumunda öğrencinin o konu ile ilgili çözebilecek soruları bulabilmesidir. Böylelikle öğrenciler konunun bitmesini beklemeden pratik yapma imkanı bulacaktır. Bunun sonucu olarak öğrencinin dersle kopukluğu önlenecektir.

Bu kitap, geometri dersine yeni başlayanlar için çözülmeli gereken ilk kitaptır. Bu kitapta öğrenciler, tavsiye edilen kitaplarla desteklenmelidir.

Tüm öğrencilerin disiplinli çalışmayı alışkanlık haline getirmelerini ve girecekleri tüm sınavlarda başarılı olmalarını diliyorum.

**Ahmet Demir**

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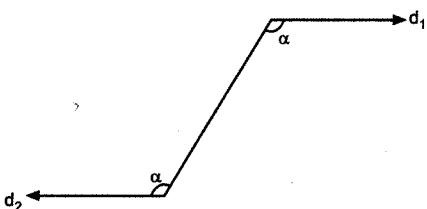
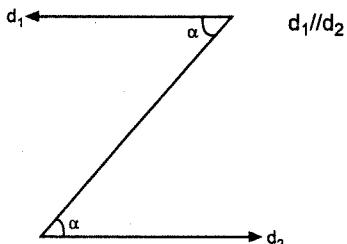
# DOĞRUDA AÇILAR

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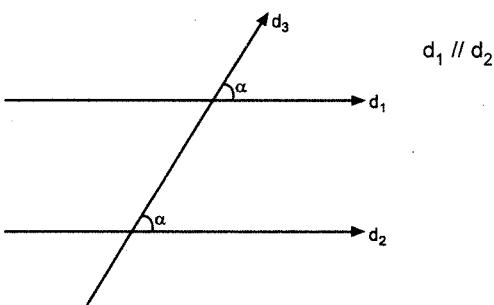


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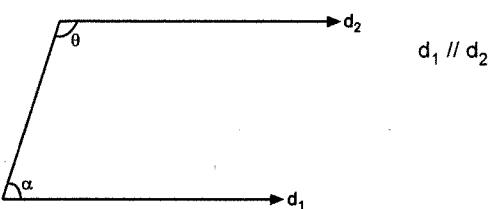
## 1. İç Ters Açı



## 2. Yöndeş Açı

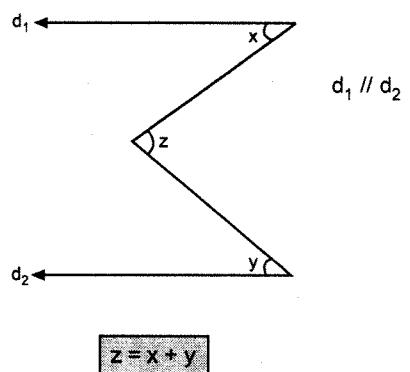


## 3. Karşı Durumlu Açılar



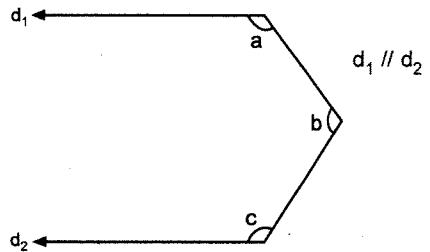
$$\alpha + \theta = 180^\circ$$

## 4.



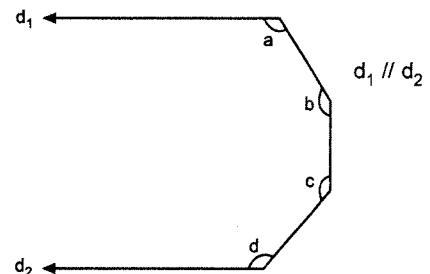
$$z = x + y$$

## 5.



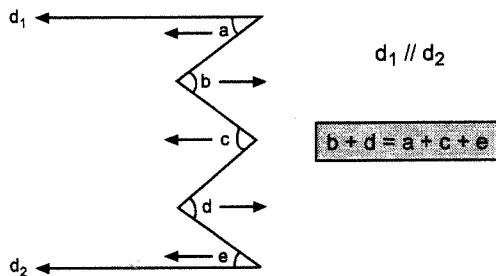
$$a + b + c = 360^\circ$$

## 6.



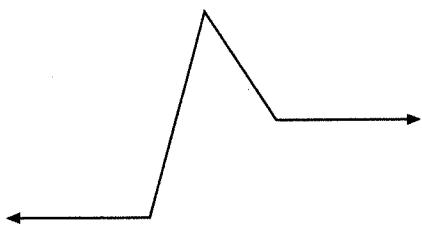
$$a + b + c + d = 540^\circ$$

7.

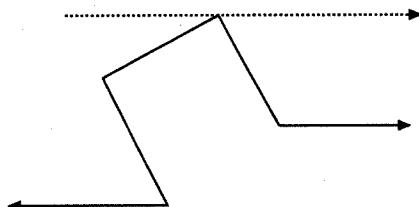


Sorunun orijinali

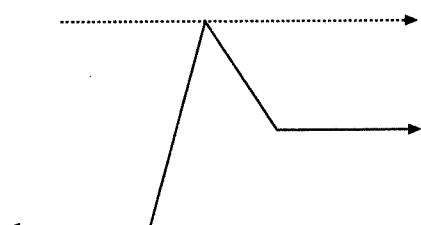
\*



Öğrencinin yapması gerektiği

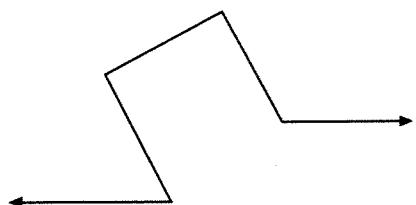


Öğrencinin yapması gerektiği



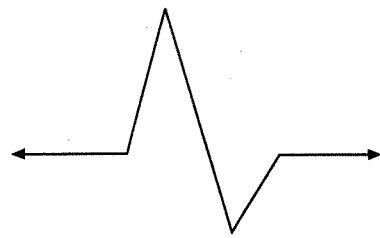
Sorunun orijinali

\*

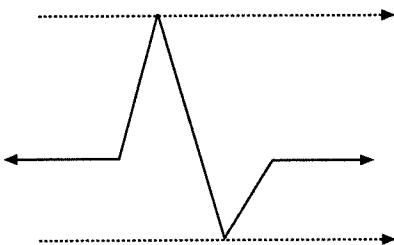


Sorunun orijinali

\*

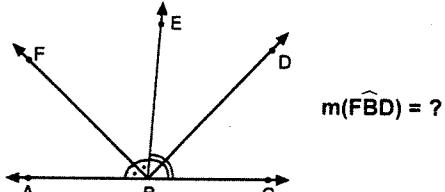


Öğrencinin yapması gerektiği

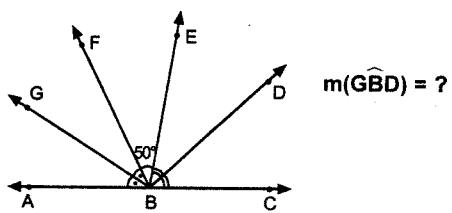


Yukarıdaki şekillerde de görüldüğü gibi köşelerden paralel çizilir ve önceki kurallardan biri elde edilmeye çalışılır. Unutmayın doğruda açılar sorularında ya bu özellikler yardımı ile soru çözülür ya da paralel doğrular uzatılarak bu özelliklerden biri ortaya çıkarılarak sorular çözülür.

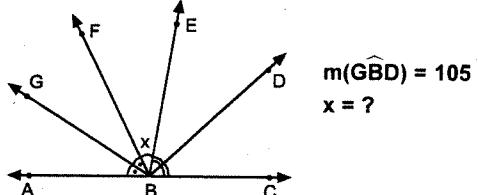
1.

Cevap:  $90^\circ$ 

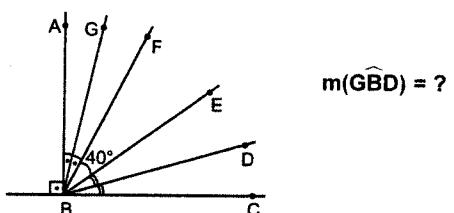
2.

Cevap:  $115^\circ$ 

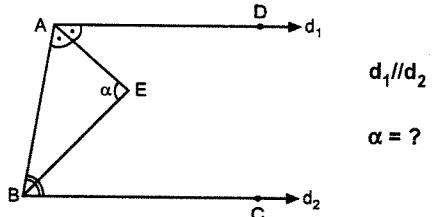
3.

Cevap:  $30^\circ$ 

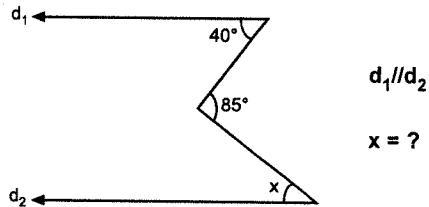
4.

Cevap:  $65^\circ$ 

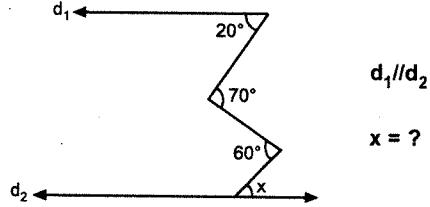
5.

Cevap:  $90^\circ$ 

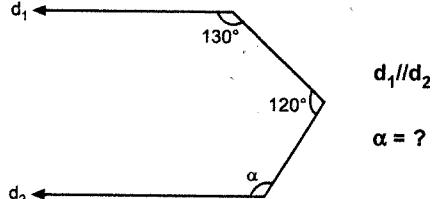
6.

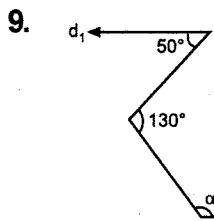
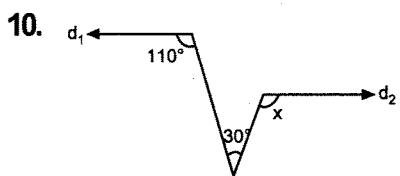
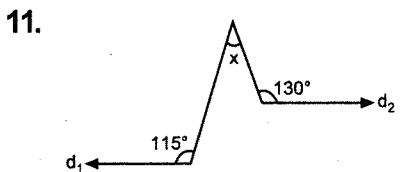
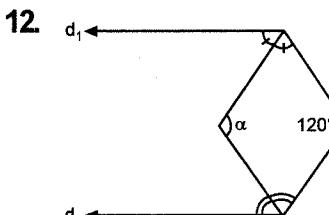
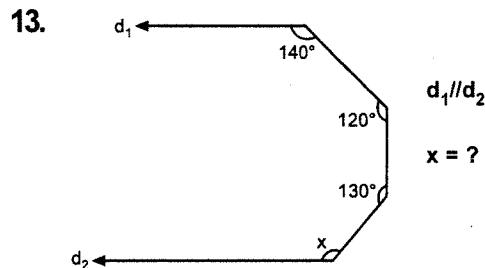
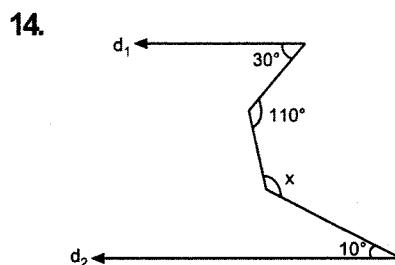
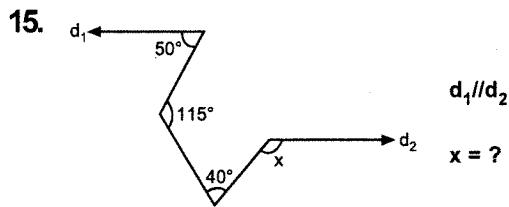
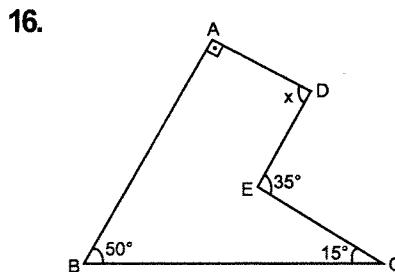
Cevap:  $45^\circ$ 

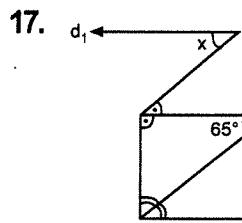
7.

Cevap:  $10^\circ$ 

8.

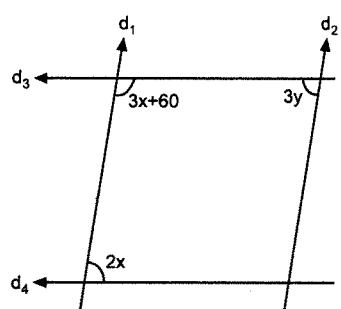
Cevap:  $110^\circ$

 $d_1 \parallel d_2$  $\alpha = ?$ Cevap:  $100^\circ$  $d_1 \parallel d_2$  $x = ?$ Cevap:  $100^\circ$  $d_1 \parallel d_2$  $x = ?$ Cevap:  $65^\circ$  $d_1 \parallel d_2$ Cevap:  $120^\circ$  $d_1 \parallel d_2$  $x = ?$ Cevap:  $150^\circ$  $d_1 \parallel d_2$  $x = ?$ Cevap:  $110^\circ$  $d_1 \parallel d_2$  $x = ?$ Cevap:  $105^\circ$  $x = ?$ Cevap:  $60^\circ$



$d_1 \parallel d_2$

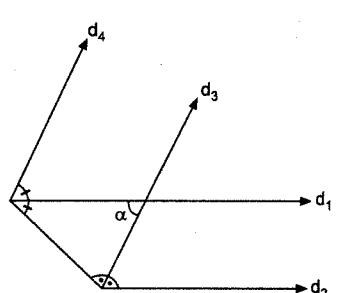
$x = ?$

Cevap:  $50^\circ$ 

$d_1 \parallel d_2$

$d_3 \parallel d_4$

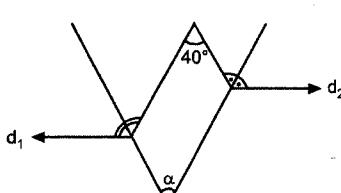
$x + y = ?$

Cevap:  $40^\circ$ 

$d_1 \parallel d_2$

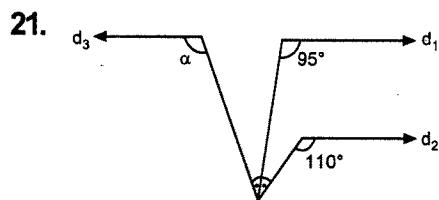
$d_3 \parallel d_4$

$\alpha = ?$

Cevap:  $60^\circ$ 

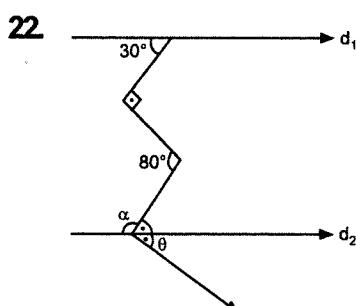
$d_1 \parallel d_2$

$\alpha = ?$

Cevap:  $70^\circ$ 

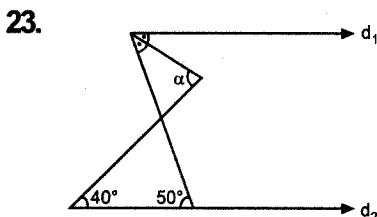
$d_1 \parallel d_2 \parallel d_3$

$\alpha = ?$

Cevap:  $100^\circ$ 

$d_1 \parallel d_2$

$\alpha - \theta = ?$

Cevap:  $140^\circ$ 

$d_1 \parallel d_2$

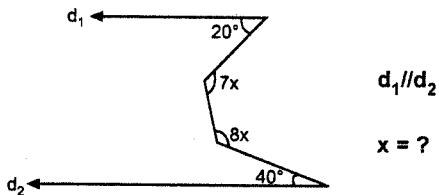
$\alpha = ?$

Cevap:  $65^\circ$ 

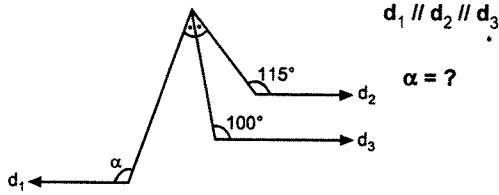
24. Herhangi bir açının tümlerinin bütününe oranı  $\frac{2}{7}$  ise bu açı kaç derecedir?

Cevap:  $54^\circ$

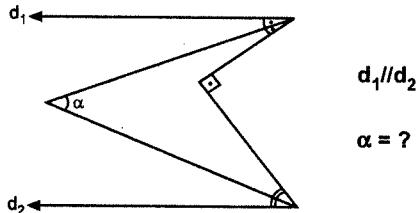
25.

Cevap:  $16^\circ$ 

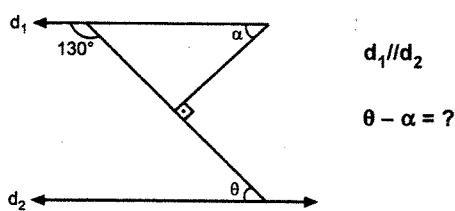
26.

Cevap:  $95^\circ$ 

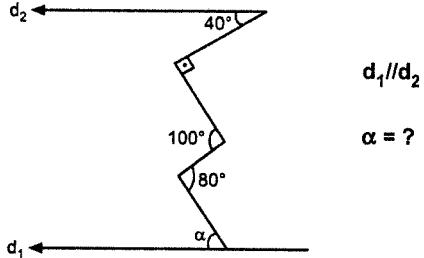
27.

Cevap:  $45^\circ$ 

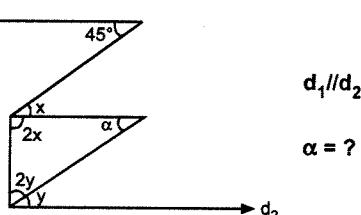
28.

Cevap:  $10^\circ$ 

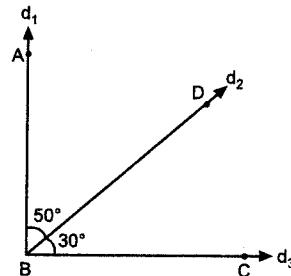
29.

Cevap:  $30^\circ$ 

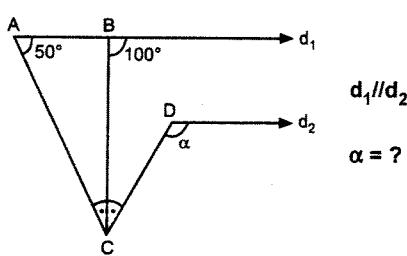
30.

Cevap:  $30^\circ$ 

31.

Cevap:  $15^\circ$ 

32.

Cevap:  $150^\circ$

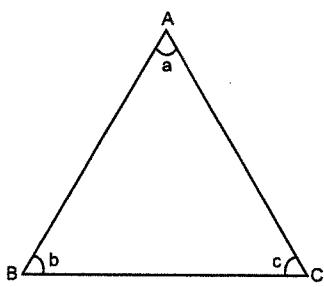
## ÜÇGENDE AÇILAR

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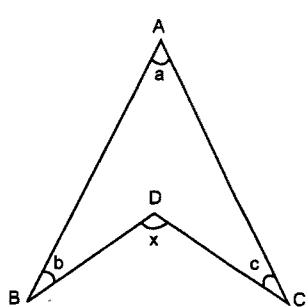
1.



$$a + b + c = 180^\circ$$

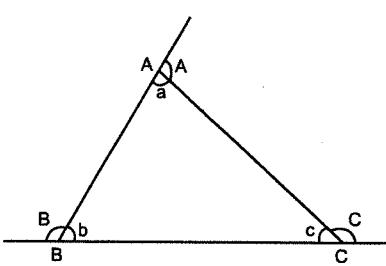
Üçgenin iç açıları toplamı  $180^\circ$  dir.

4.



$$x = a + b + c$$

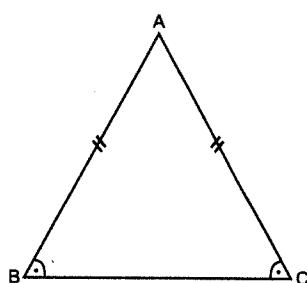
2.



Üçgenin dış açıları toplamı  $360^\circ$  dir.

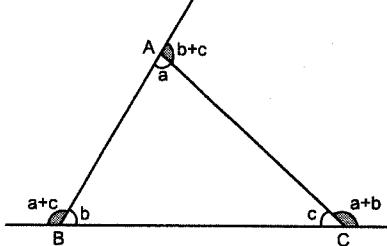
$$A + B + C = 360^\circ$$

5.



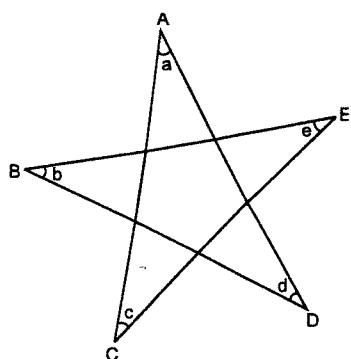
$$|AB| = |AC| \Rightarrow m(\widehat{B}) = m(\widehat{C})$$

3.



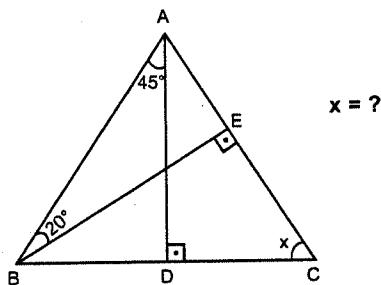
Herhangi bir dış açı, kendisine komşu olmayan iki iç açının toplamına eşittir.

6.

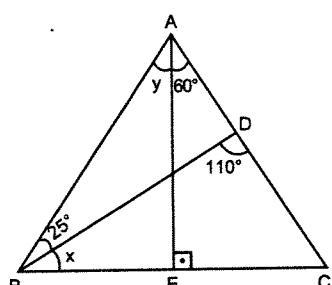


$$a + b + c + d + e = 180^\circ \text{ dir.}$$

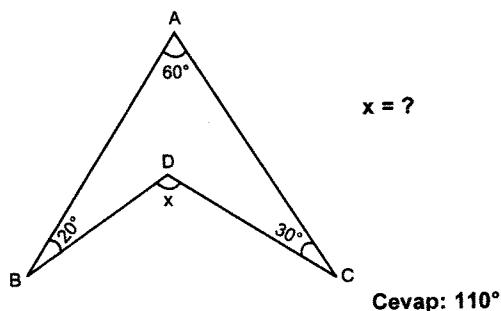
1.

 $x = ?$ Cevap:  $65^\circ$ 

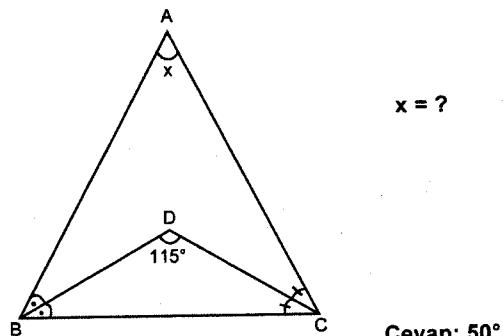
2.

 $x = ?$   
 $y = ?$ Cevap:  $x = 40^\circ$   
 $y = 25^\circ$ 

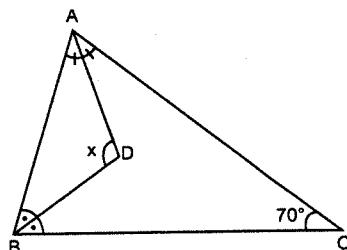
3.

 $x = ?$ Cevap:  $110^\circ$ 

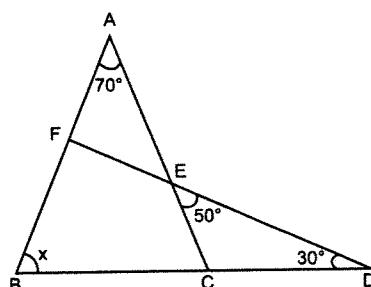
4.

 $x = ?$ Cevap:  $50^\circ$ 

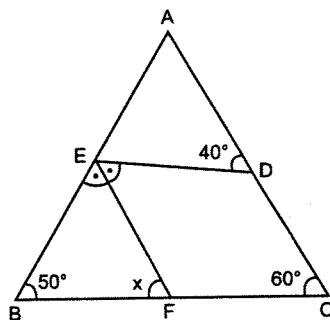
5.

 $x = ?$ Cevap:  $125^\circ$ 

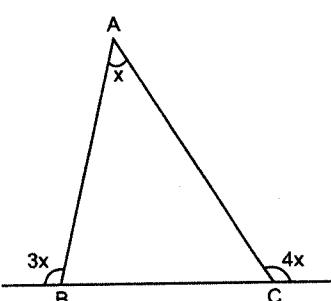
6.

 $x = ?$ Cevap:  $30^\circ$ 

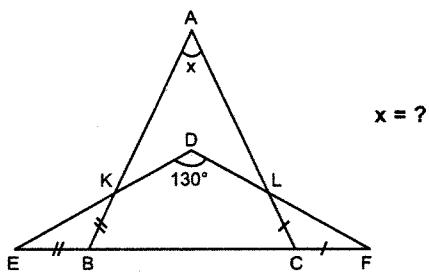
7.

 $x = ?$ Cevap:  $75^\circ$ 

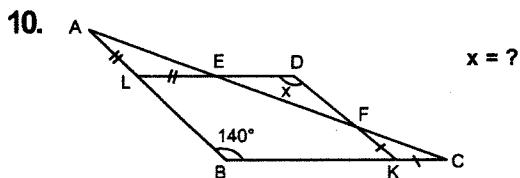
8.

 $x = ?$ Cevap:  $30^\circ$

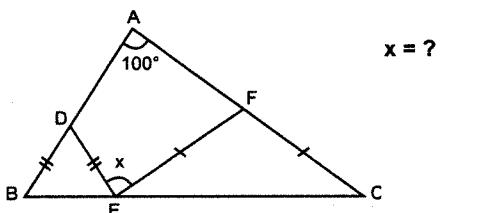
9.

 $x = ?$ Cevap:  $80^\circ$ 

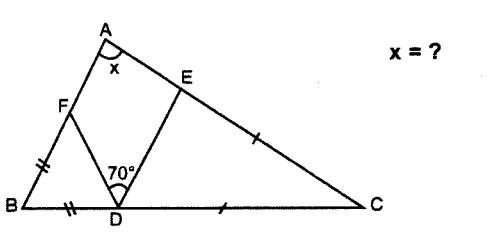
10.

 $x = ?$ Cevap:  $140^\circ$ 

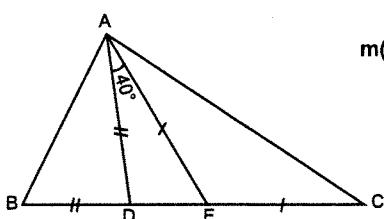
11.

 $x = ?$ Cevap:  $100^\circ$ 

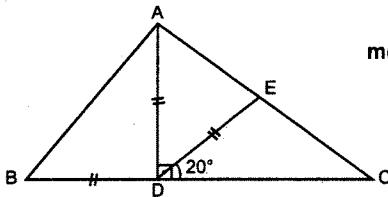
12.

 $x = ?$ Cevap:  $40^\circ$ 

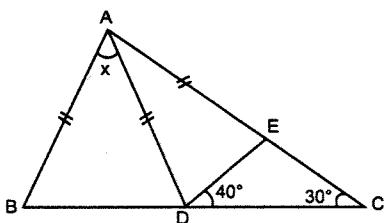
13.

 $m(\widehat{BAC}) = ?$ Cevap:  $110^\circ$ 

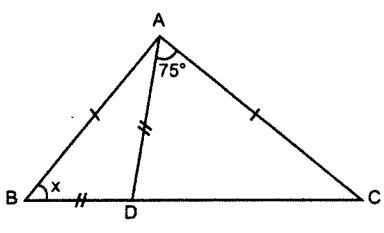
14.

 $m(\widehat{BAC}) = ?$ Cevap:  $100^\circ$ 

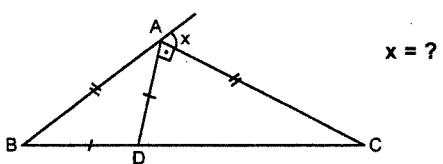
15.

 $x = ?$ Cevap:  $40^\circ$ 

16.

 $x = ?$ Cevap:  $35^\circ$

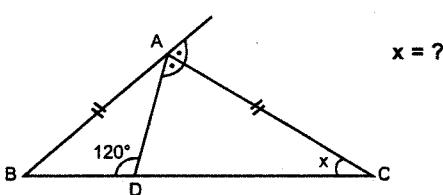
17.



$x = ?$

Cevap:  $60^\circ$ 

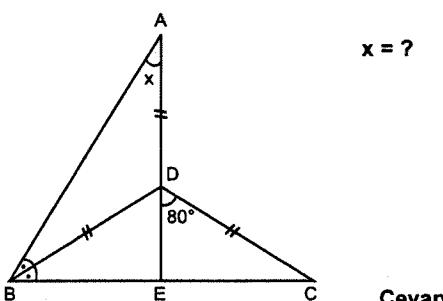
18.



$x = ?$

Cevap:  $40^\circ$ 

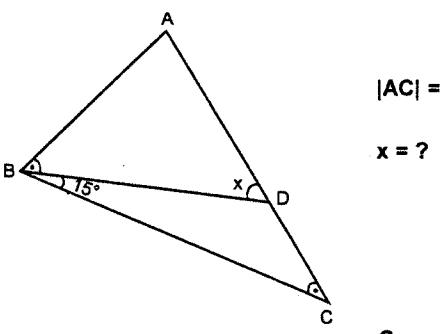
19.



$x = ?$

Cevap:  $25^\circ$ 

20.

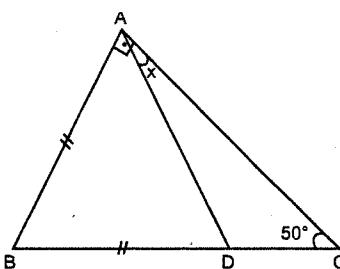


$|AC| = |BC|$

$x = ?$

Cevap:  $65^\circ$ 

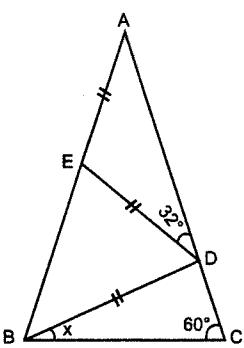
21.



$x = ?$

Cevap:  $20^\circ$ 

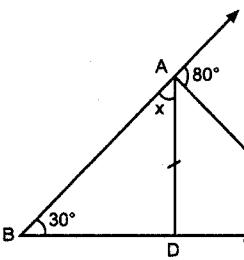
22.



$x = ?$

Cevap:  $24^\circ$ 

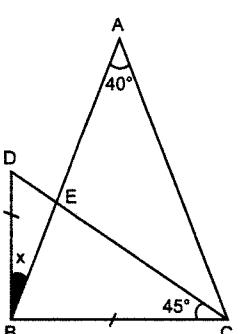
23.



$x = ?$

Cevap:  $50^\circ$ 

24.

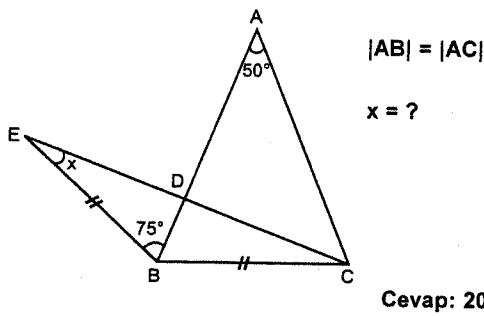


$|AC| = |AB|$

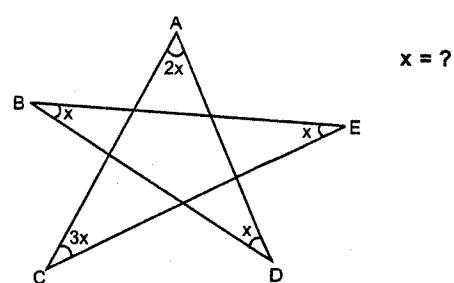
$x = ?$

Cevap:  $20^\circ$

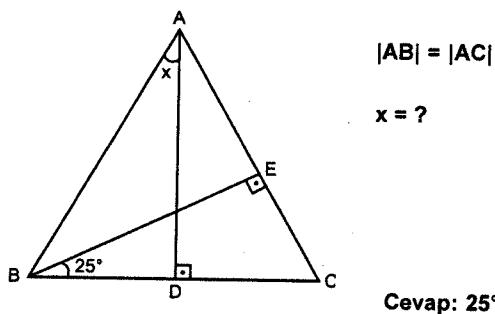
25.

Cevap:  $20^\circ$ 

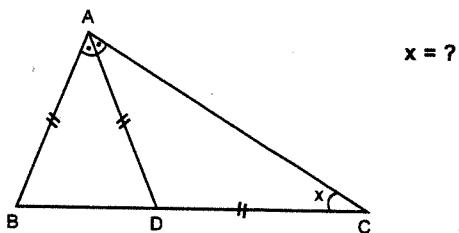
29.

Cevap:  $22,5^\circ$ 

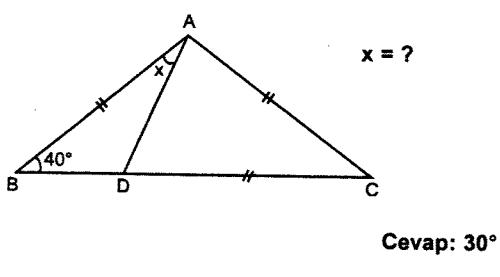
26.

Cevap:  $25^\circ$ 

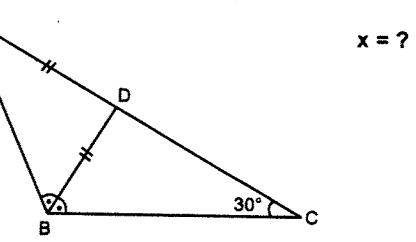
30.

Cevap:  $36^\circ$ 

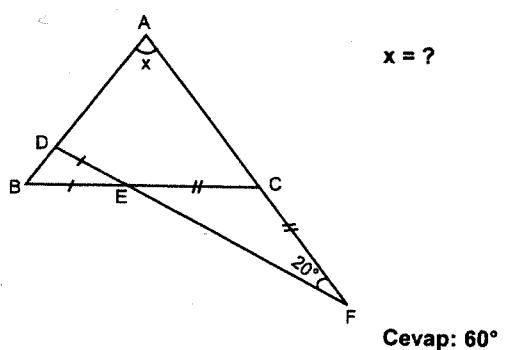
27.

Cevap:  $30^\circ$ 

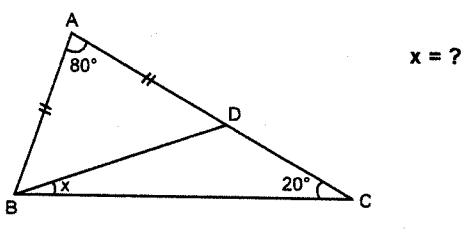
31.

Cevap:  $50^\circ$ 

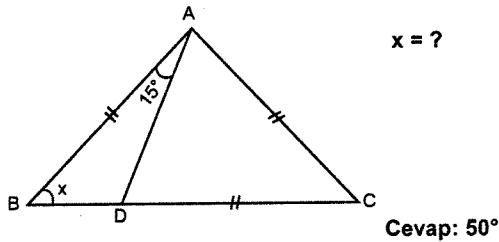
28.

Cevap:  $60^\circ$ 

32.

Cevap:  $30^\circ$

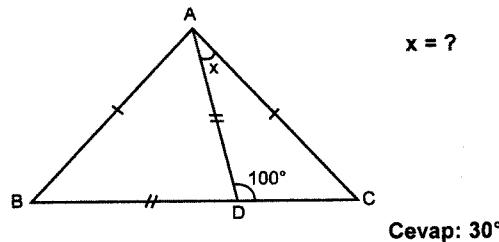
33.



$x = ?$

Cevap:  $50^\circ$ 

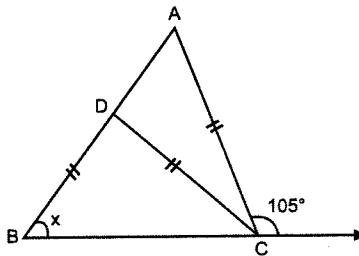
34.



$x = ?$

Cevap:  $30^\circ$ 

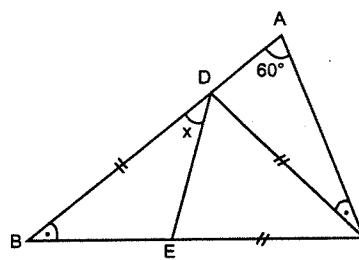
37.



$x = ?$

Cevap:  $35^\circ$ 

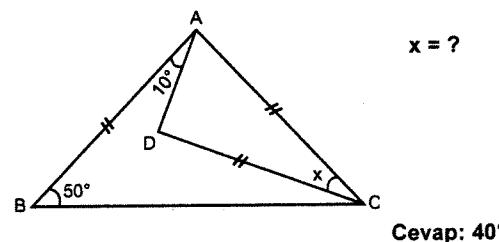
38.



$x = ?$

Cevap:  $30^\circ$ 

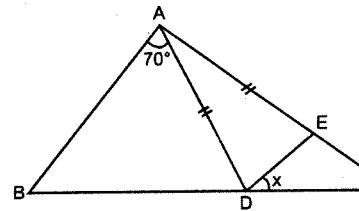
35.



$x = ?$

Cevap:  $40^\circ$ 

39.

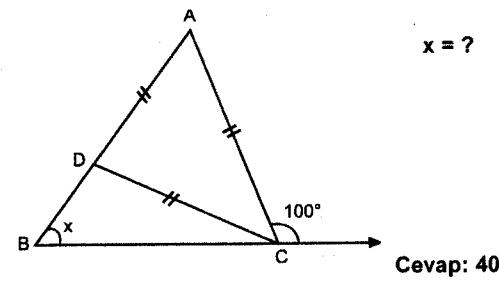


$|AB| = |AC|$

$x = ?$

Cevap:  $35^\circ$ 

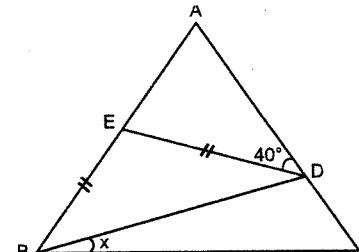
36.



$x = ?$

Cevap:  $40^\circ$ 

40.

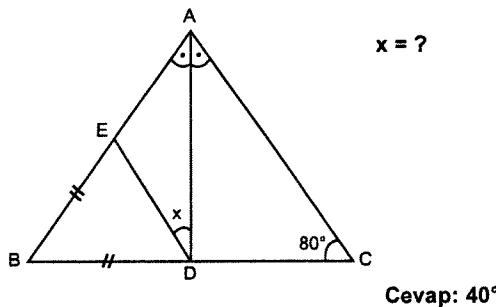


$|AB| = |AC|$

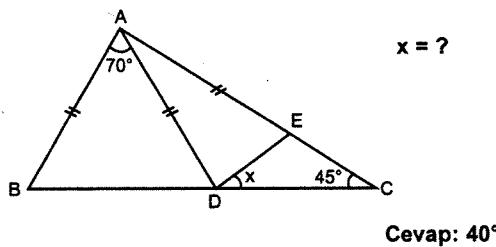
$x = ?$

Cevap:  $20^\circ$

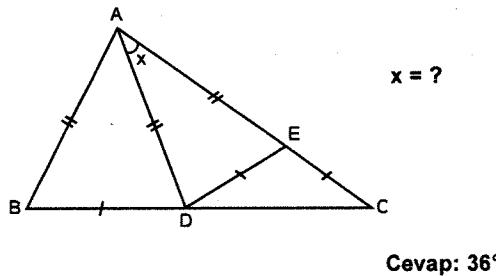
41.



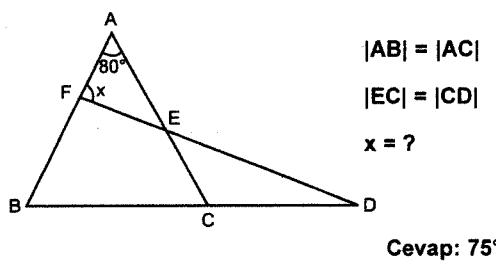
42.



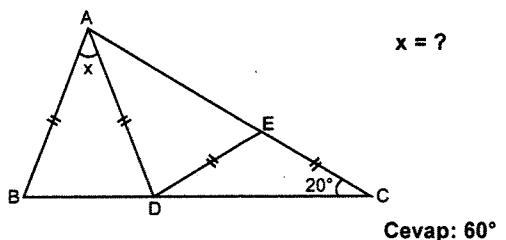
43.



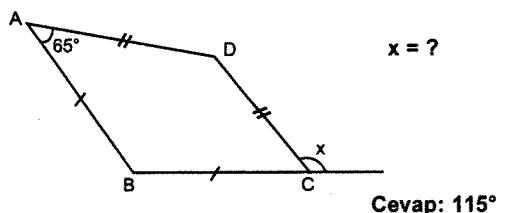
44.



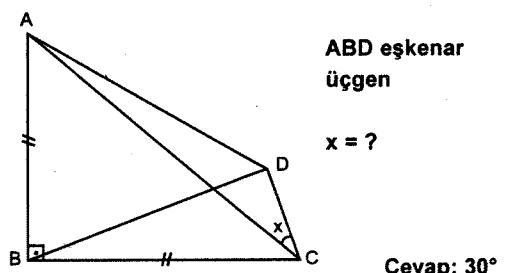
45.



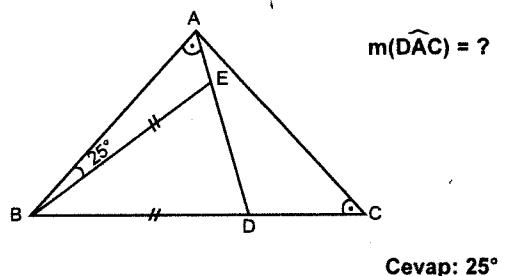
46.



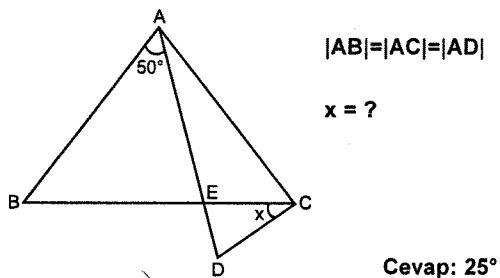
47.



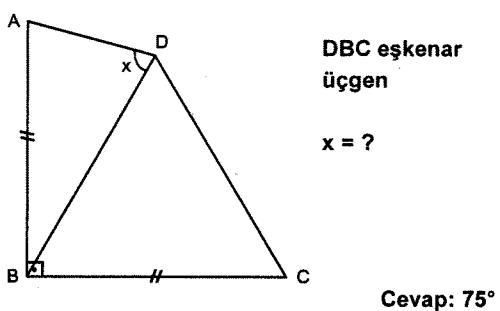
48.



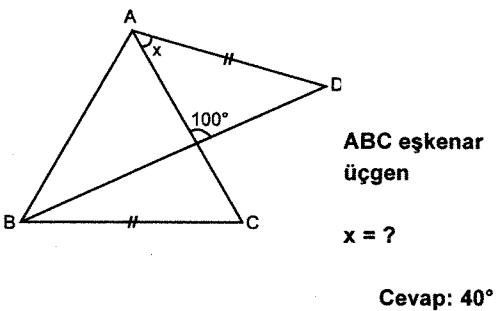
49.

Cevap:  $25^\circ$ 

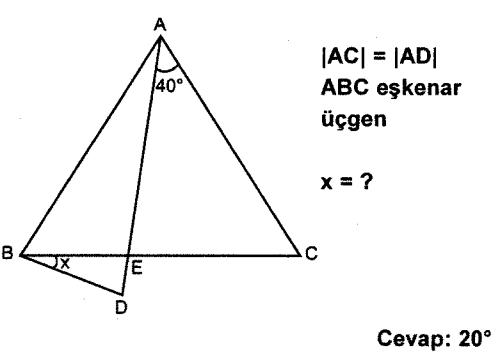
50.

Cevap:  $75^\circ$ 

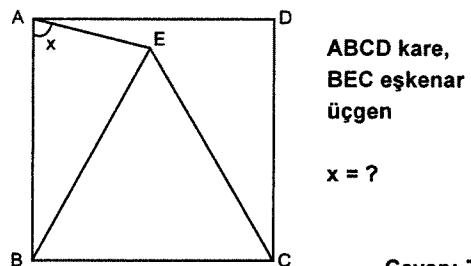
51.

Cevap:  $40^\circ$ 

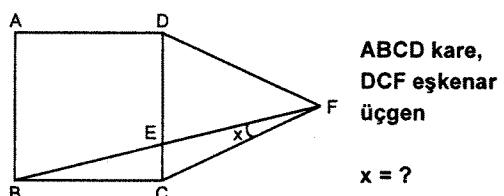
52.

Cevap:  $20^\circ$ 

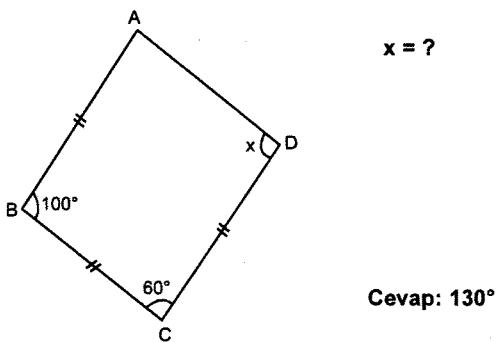
53.

Cevap:  $75^\circ$ 

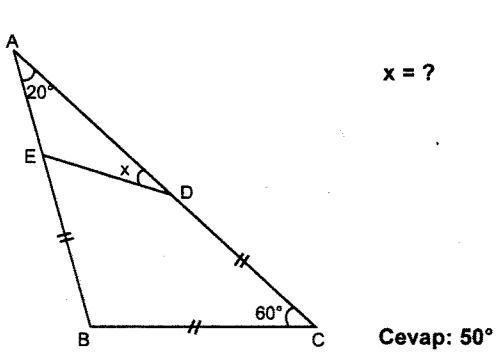
54.

Cevap:  $15^\circ$ 

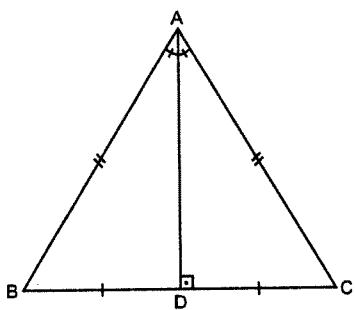
55.

Cevap:  $130^\circ$ 

56.

Cevap:  $50^\circ$

## İKİZKENAR ÜÇGEN

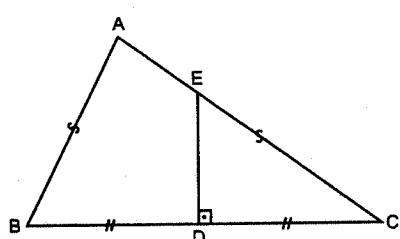


İkizkenar üçgende yükseklik, açıortay ve kenarortay birbirine eşittir.

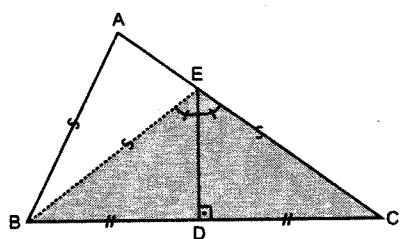
Soruda, ikizkenarlık  
açıortaylık  
yükseklik  
kenarortaylığı

bu dört bilgiden herhangi ikisi veya ikisini çağrıştıran şekiller varsa yukarıdaki şeķile tamamlanır.

1.

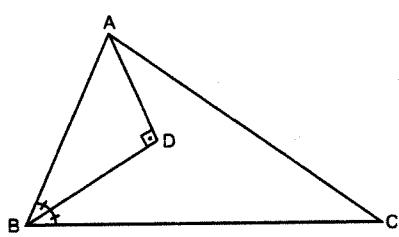


Soruda  
böyle  
verilirse

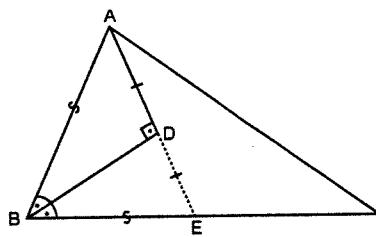


Böyle  
tamam-  
lanır.

2.

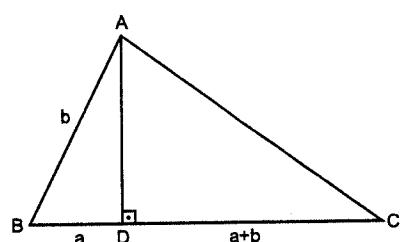


Böyle  
verilirse

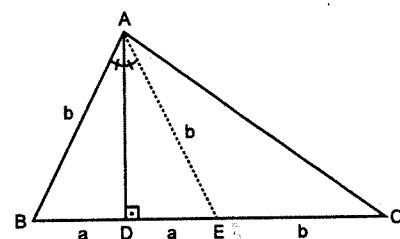


böyle  
tamam-  
lanır.

3.

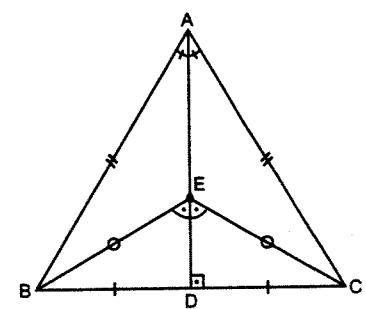


Soruda  
böyle  
verilirse

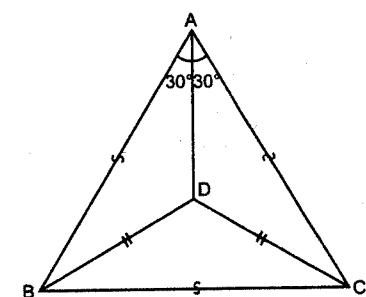


Böyle  
tamam-  
lanır.

\*

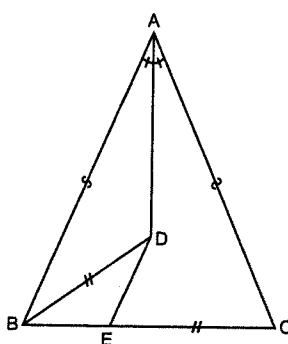


[AD] de bir  
nokta alınır.  
E den B ve  
C ye çizgiler  
uzatılırsa  
 $|EB| = |EC|$   
olur.

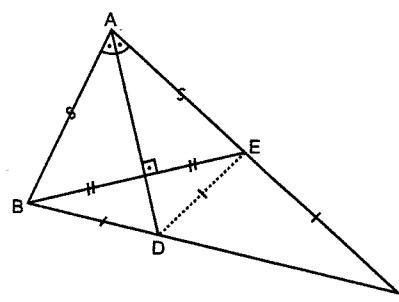


ABC  
eşkenar  
üçgen ve  
 $|BD| = |DC|$   
ise

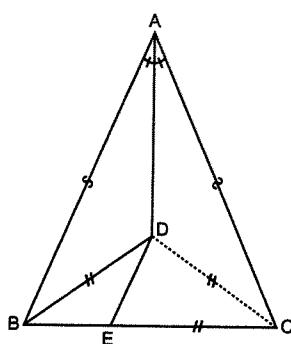
$m(\widehat{BAD}) = m(\widehat{DAC}) = 30^\circ$  olur.



Şekil böyle  
verilirse

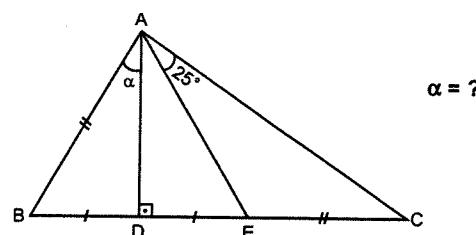


Böyle  
yapılır.



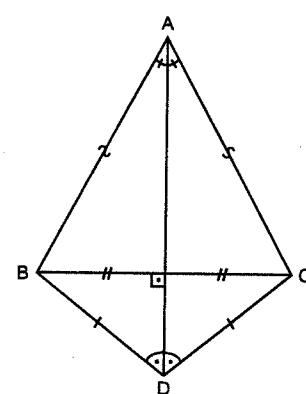
Böyle  
tamamlanır.

Örnek:

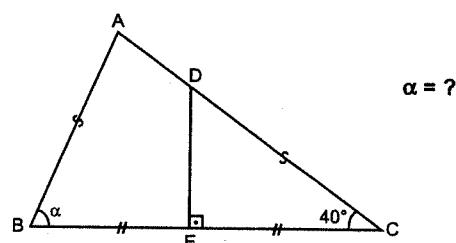


$$\alpha = ?$$

Cevap:  $40^\circ$

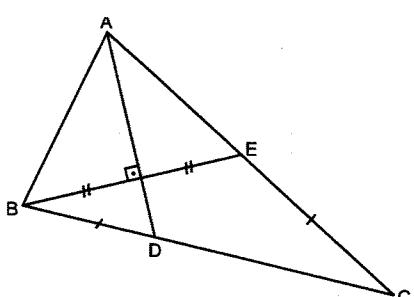


\*  
Şekil  
böyle  
verilirse

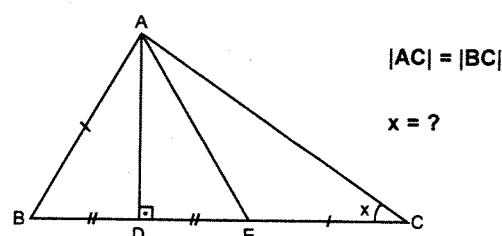


$$\alpha = ?$$

Cevap:  $60^\circ$



Örnek:

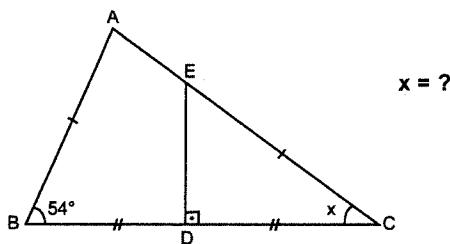


$$|AC| = |BC|$$

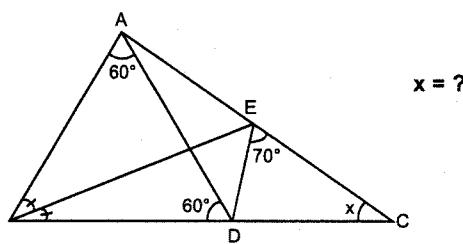
$$x = ?$$

Cevap:  $36^\circ$

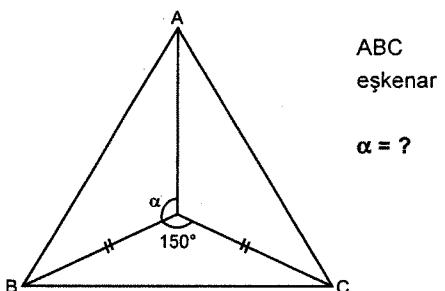
Örnek:

Cevap:  $42^\circ$ 

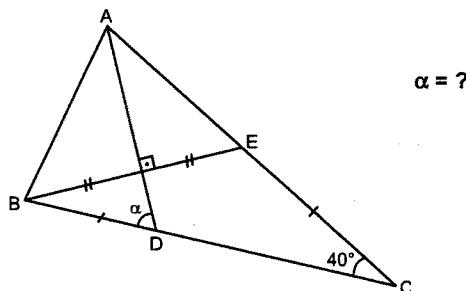
Örnek:

Cevap:  $25^\circ$ 

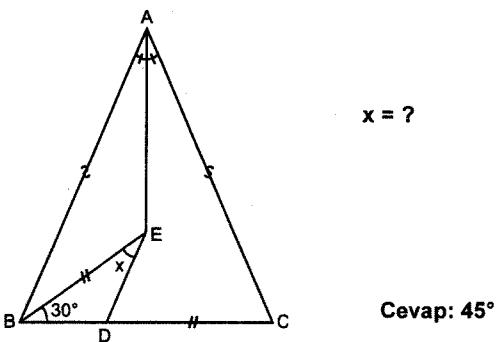
Örnek:

 $\alpha = ?$ Cevap:  $105^\circ$ 

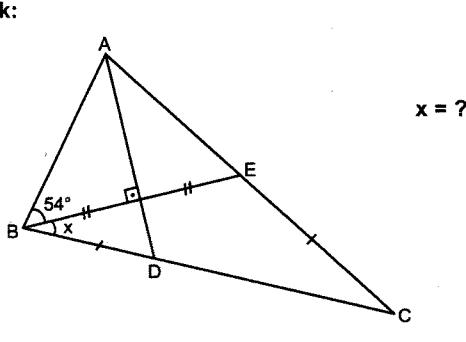
Örnek:

Cevap:  $70^\circ$ 

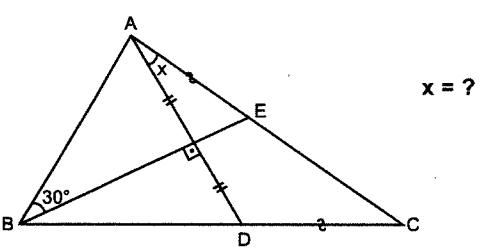
Örnek:

 $x = ?$ Cevap:  $45^\circ$ 

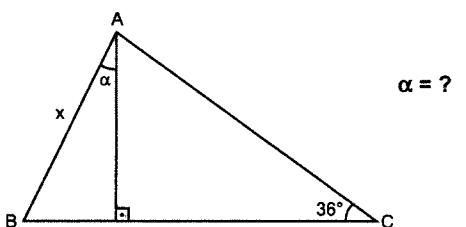
Örnek:

Cevap:  $18^\circ$ 

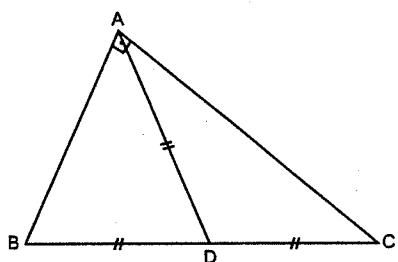
Örnek:

 $x = ?$ Cevap:  $20^\circ$ 

Örnek:

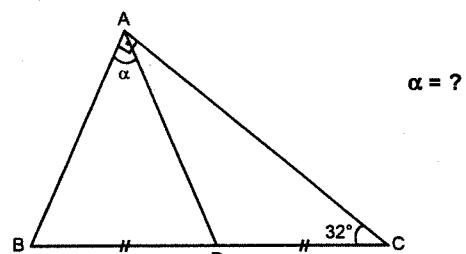
 $\alpha = ?$ Cevap:  $18^\circ$

## MUHTEŞEM ÜÇLÜ



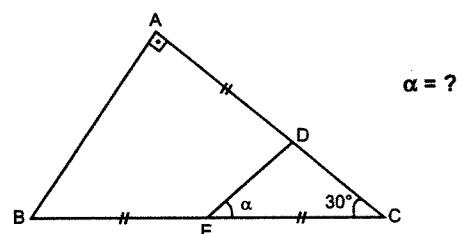
Hipotenüse ait kenarortay ayırdığı parçalardan birine eşittir.

Örnek:



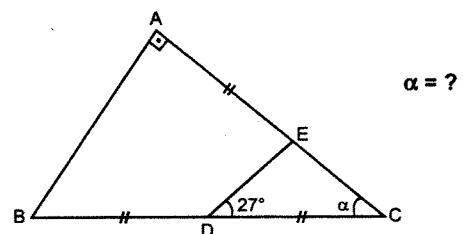
Cevap:  $58^\circ$

Örnek:



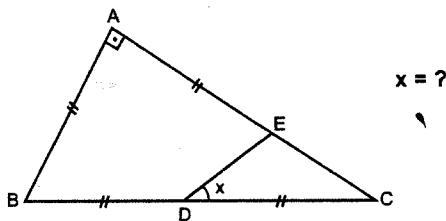
Cevap:  $45^\circ$

Örnek:



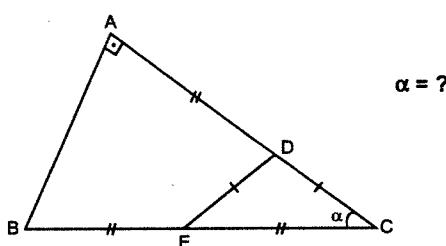
Cevap:  $42^\circ$

Örnek:



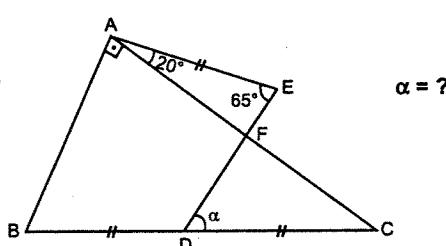
Cevap:  $45^\circ$

Örnek:



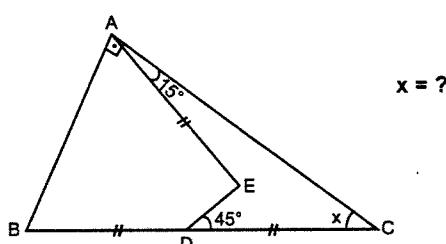
Cevap:  $36^\circ$

Örnek:



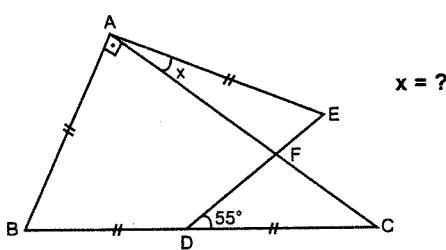
Cevap:  $55^\circ$

Örnek:



Cevap:  $25^\circ$

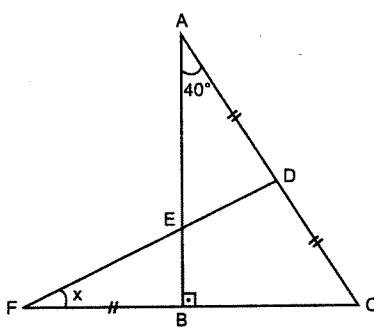
Örnek:



$x = ?$

Cevap:  $20^\circ$ 

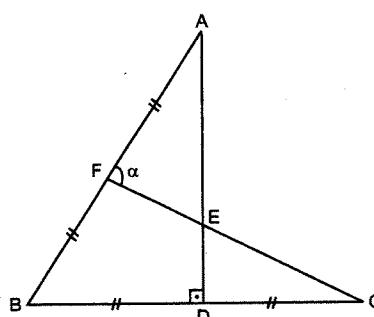
Örnek:



$x = ?$

Cevap:  $25^\circ$ 

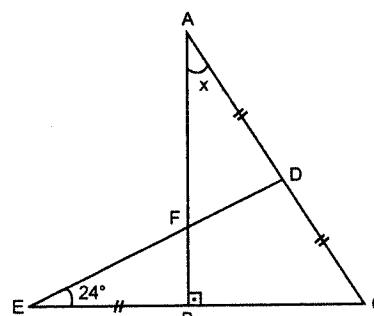
Örnek:



$\alpha = ?$

Cevap:  $90^\circ$ 

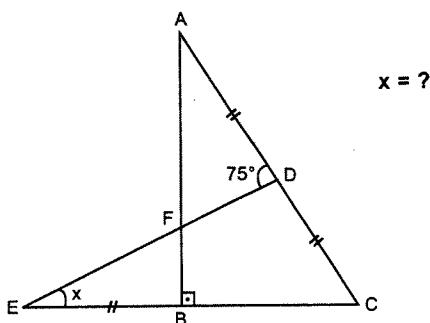
Örnek:



$x = ?$

Cevap:  $42^\circ$ 

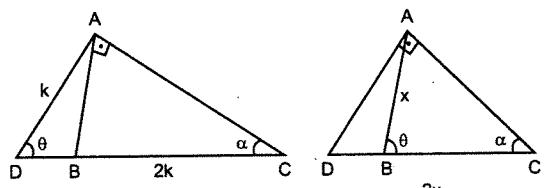
Örnek:



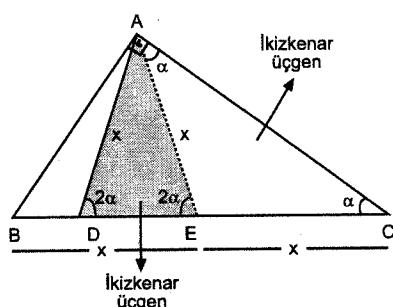
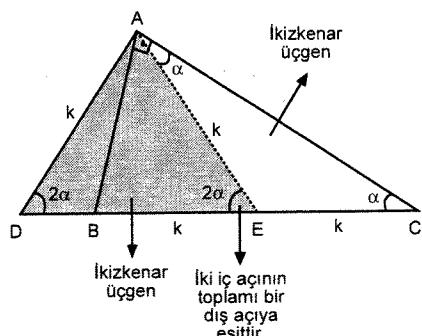
$x = ?$

Cevap:  $25^\circ$ 

NOT:

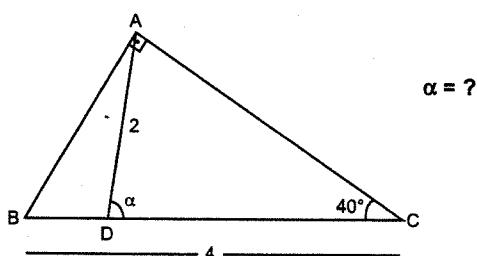


Yukarıdaki iki şekilde  $90^\circ$  nin içinden geçen çizgi veya  $90^\circ$  nin yanındaki çizgi hipotenüsün yarısına eşittir. Bu sorularda hipotenüse ait kenarortay çizilir. Yani muhtemel üçlü oluşturulur.



şeklinde yapılır.

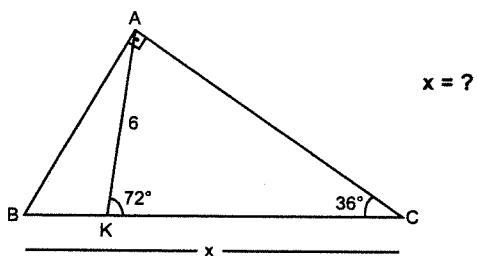
Örnek:



$\alpha = ?$

Cevap:  $80^\circ$ 

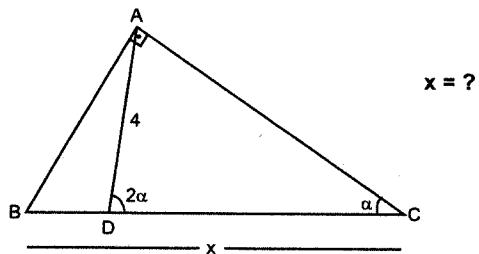
Örnek:



$x = ?$

Cevap: 12

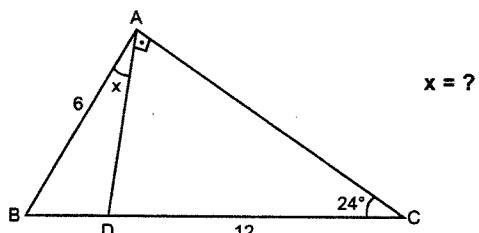
Örnek:



$x = ?$

Cevap: 8

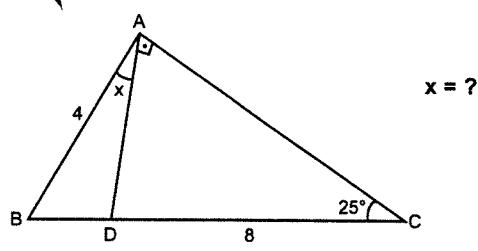
Örnek:



$x = ?$

Cevap:  $18^\circ$ 

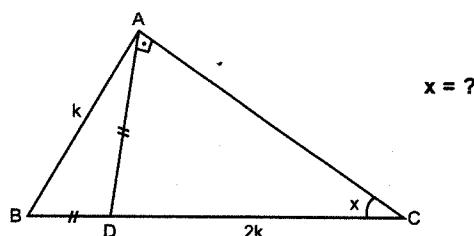
Örnek:



$x = ?$

Cevap:  $15^\circ$ 

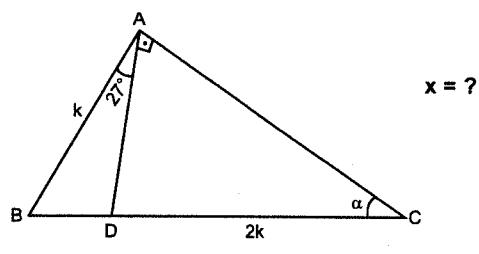
Örnek:



$x = ?$

Cevap:  $18^\circ$ 

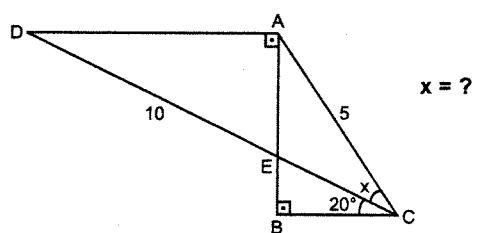
Örnek:



$x = ?$

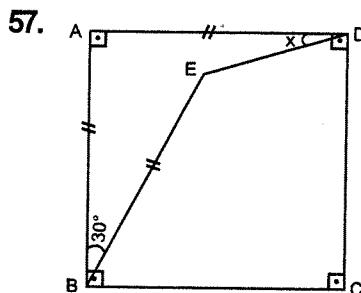
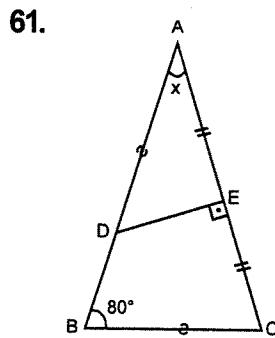
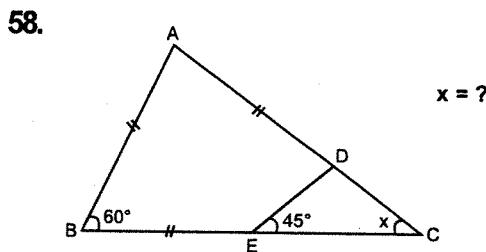
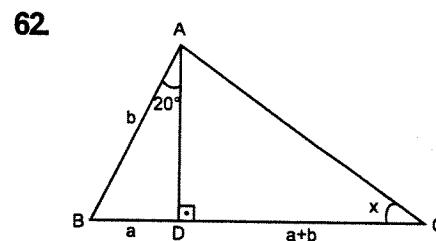
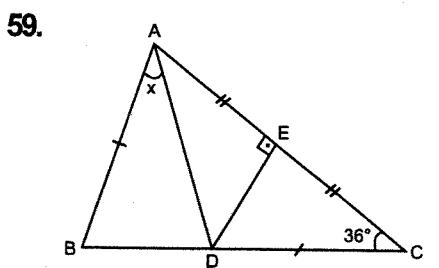
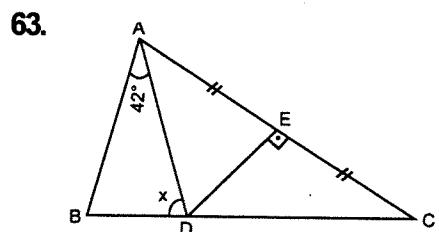
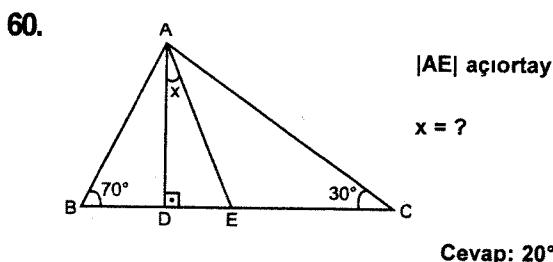
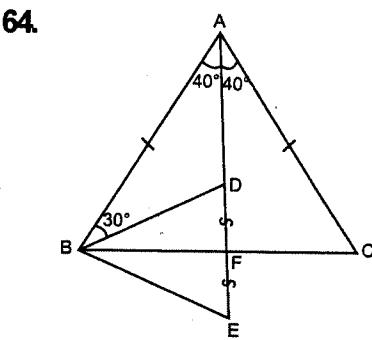
Cevap:  $21^\circ$ 

Örnek:

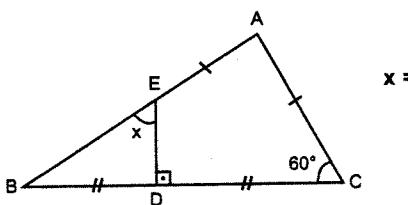


$x = ?$

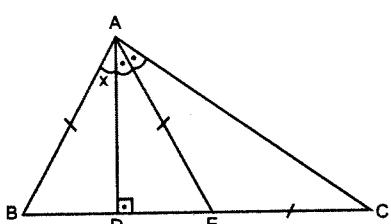
Cevap:  $40^\circ$

 $x = ?$ Cevap:  $15^\circ$  $x = ?$ Cevap:  $40^\circ$  $x = ?$ Cevap:  $30^\circ$  $x = ?$ Cevap:  $35^\circ$  $x = ?$ Cevap:  $36^\circ$  $|AC| = |BC|$  $x = ?$ Cevap:  $64^\circ$  $|AE| \text{ açıortay}$  $x = ?$ Cevap:  $20^\circ$  $m(\widehat{AEB}) = ?$ Cevap:  $70^\circ$

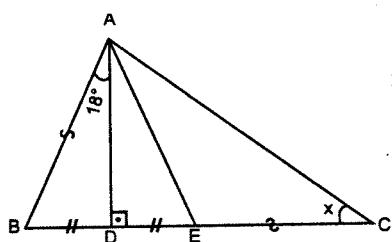
65.

 $x = ?$ Cevap:  $70^\circ$ 

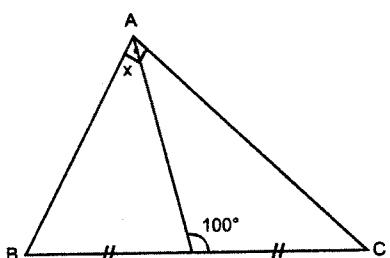
66.

 $x = ?$ Cevap:  $30^\circ$ 

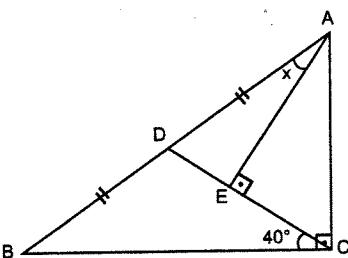
67.

 $x = ?$ Cevap:  $36^\circ$ 

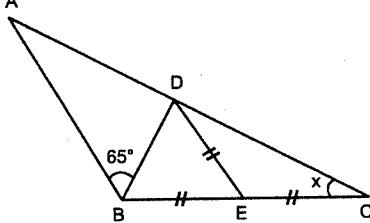
68.

 $x = ?$ Cevap:  $50^\circ$ 

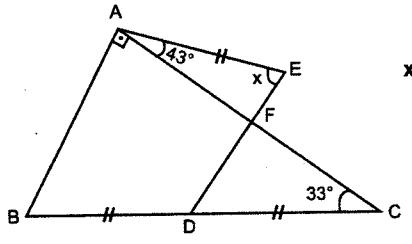
69.

 $x = ?$ Cevap:  $10^\circ$ 

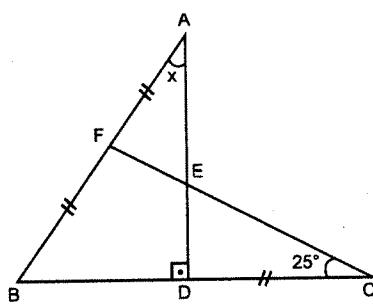
70.

 $|DE| // |AB|$  $x = ?$ Cevap:  $25^\circ$ 

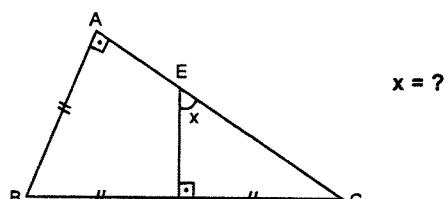
71.

 $x = ?$ Cevap:  $52^\circ$ 

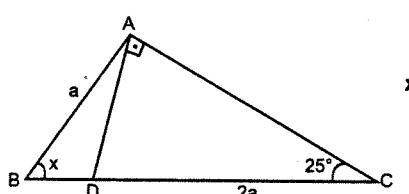
72.

 $x = ?$ Cevap:  $40^\circ$

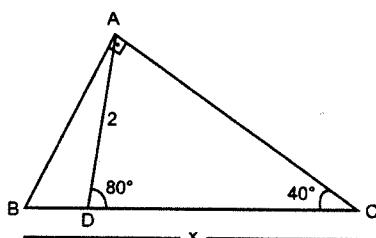
73.

 $x = ?$ Cevap:  $60^\circ$ 

74.

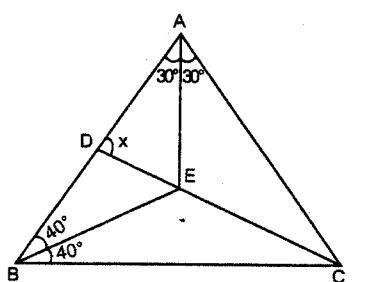
 $x = ?$ Cevap:  $50^\circ$ 

75.

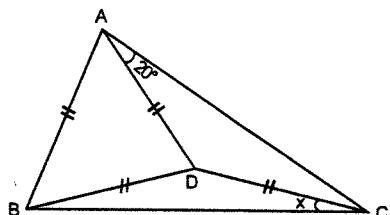
 $x = ?$ 

Cevap: 4

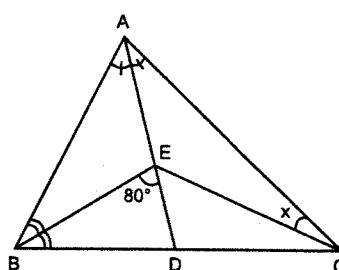
76.

 $x = ?$ Cevap:  $100^\circ$ 

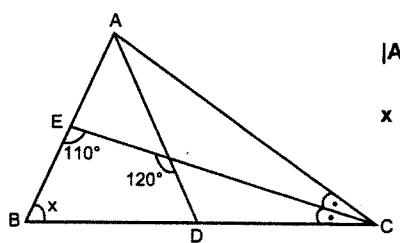
77.

 $x = ?$ Cevap:  $10^\circ$ 

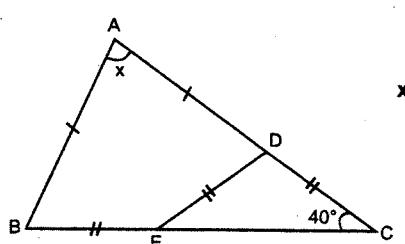
78.

 $x = ?$ Cevap:  $10^\circ$ 

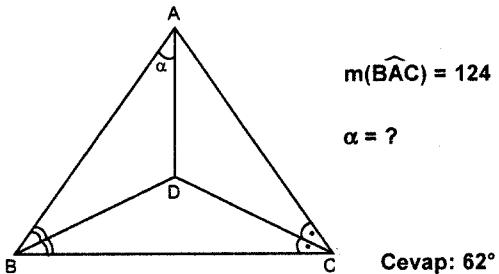
79.

 $|AD| = |DC|$  $x = ?$ Cevap:  $50^\circ$ 

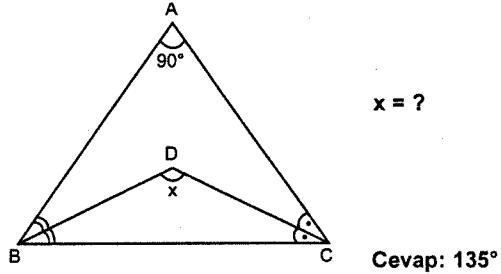
80.

 $x = ?$ Cevap:  $60^\circ$

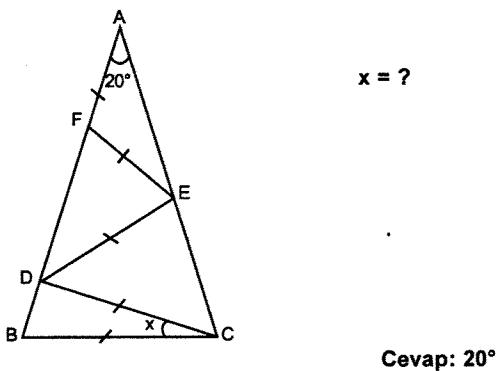
81.



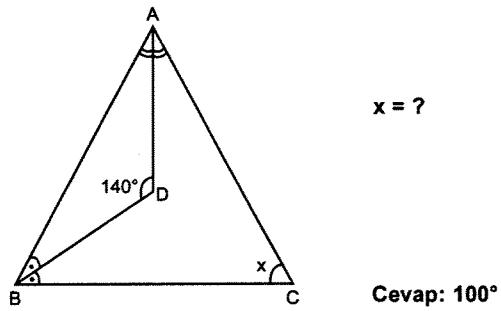
85.



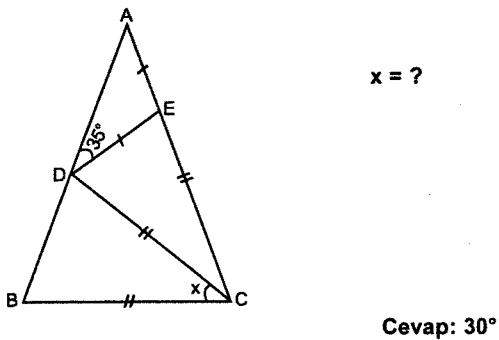
82.



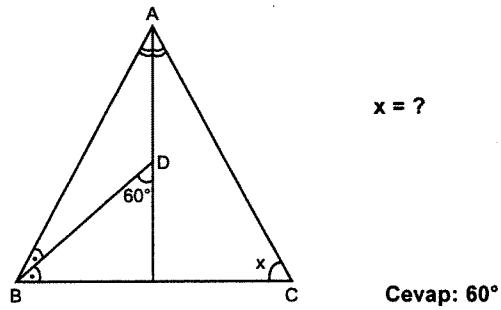
86.



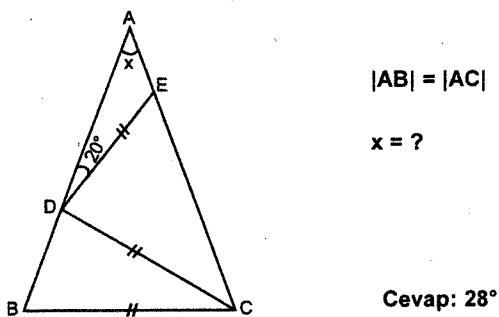
83.



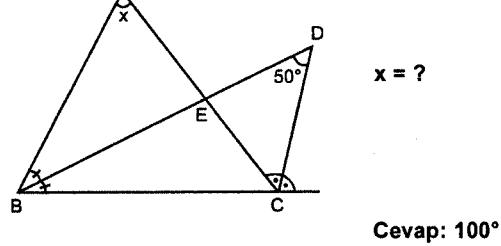
87.



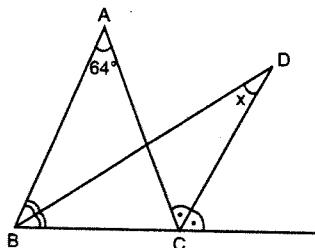
84.



88.



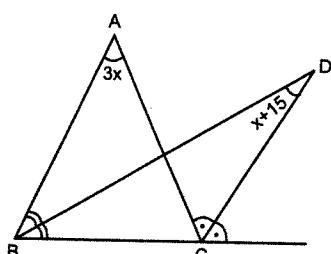
98.



$x = ?$

Cevap:  $32^\circ$ 

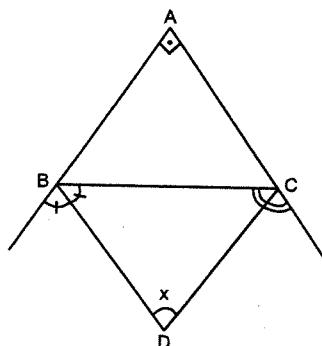
90.



$x = ?$

Cevap:  $30^\circ$ 

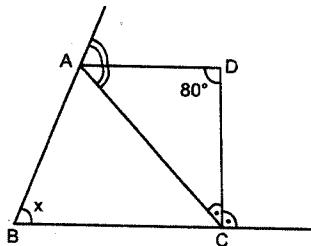
91.



$x = ?$

Cevap:  $45^\circ$ 

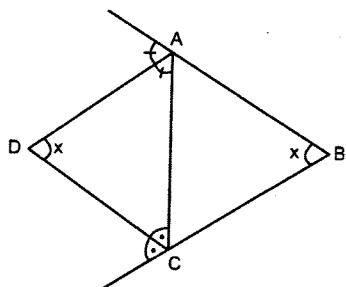
92.



$x = ?$

Cevap:  $20^\circ$ 

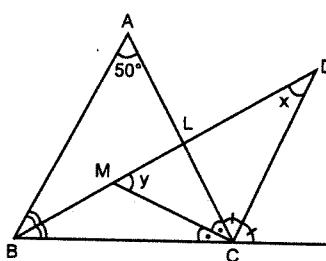
93.



$x = ?$

Cevap:  $60^\circ$ 

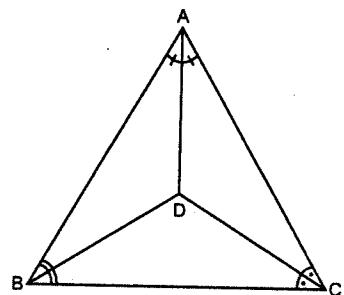
94.



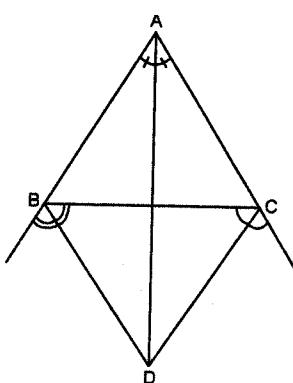
$y - x = ?$

Cevap:  $40^\circ$ 

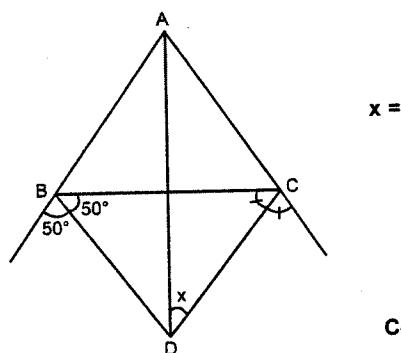
- Üçgenin iç açıortayları bir noktada kesişir. Bu iç açıortaylarından herhangi ikisi verilirse öğrenci üçüncüsünün açıortay olduğunu anlamak zorundadır.



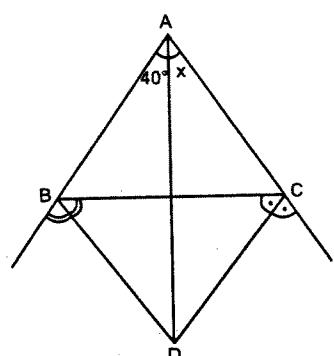
- D: noktası ABC üçgeninin dış açıortaylarının kesim noktasıdır. D noktasına gelen [CD], [AD] ve [BD] açıortaylarının herhangi ikisi soruda verilmişse öğrenci üçüncüün açıortay olduğunu anlamak zorundadır.



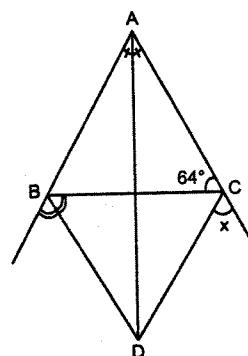
95.

 $x = ?$ Cevap:  $40^\circ$ 

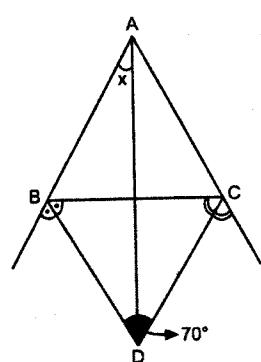
96.

 $x = ?$ Cevap:  $40^\circ$ 

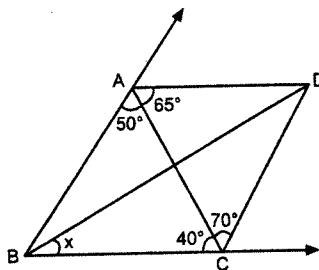
97.

 $x = ?$ Cevap:  $58^\circ$ 

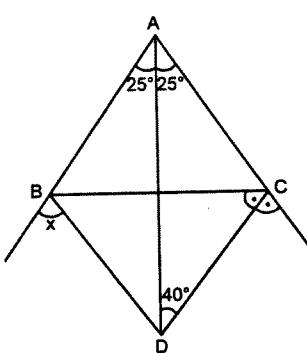
98.

 $x = ?$ Cevap:  $20^\circ$ 

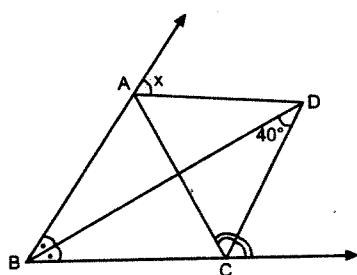
99.

 $x = ?$ Cevap:  $45^\circ$ 

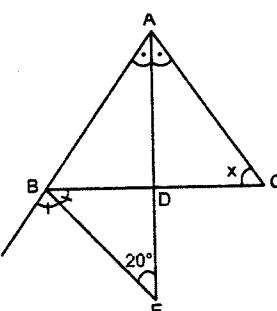
100.

 $x = ?$ Cevap:  $50^\circ$ 

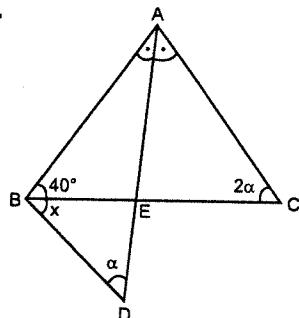
101.

 $x = ?$ Cevap:  $50^\circ$ 

102.

 $x = ?$ Cevap:  $40^\circ$

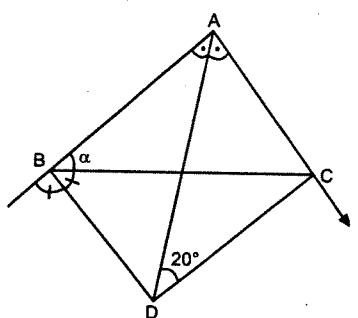
103.



$x = ?$

Cevap:  $70^\circ$ 

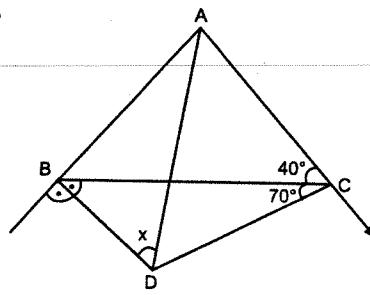
104.



$\alpha = ?$

Cevap:  $40^\circ$ 

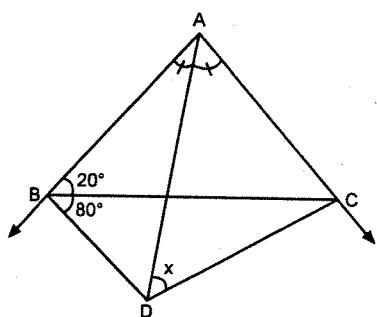
105.



$x = ?$

Cevap:  $20^\circ$ 

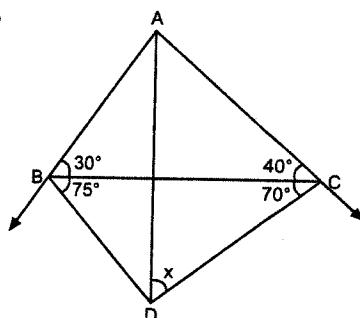
106.



$x = ?$

Cevap:  $10^\circ$ 

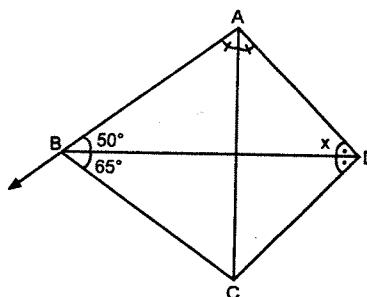
107.



$x = ?$

Cevap:  $15^\circ$ 

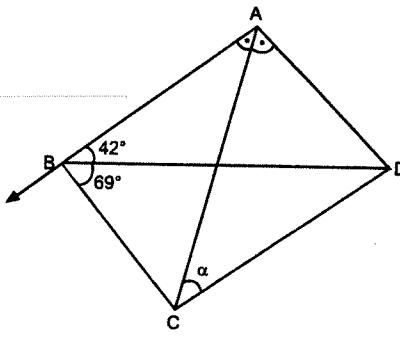
108.



$x = ?$

Cevap:  $60^\circ$ 

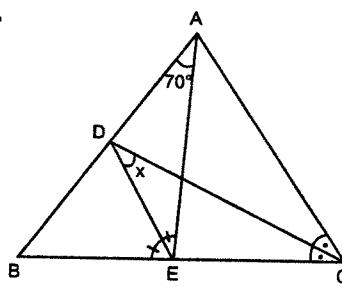
109.



$\alpha = ?$

Cevap:  $21^\circ$ 

110.

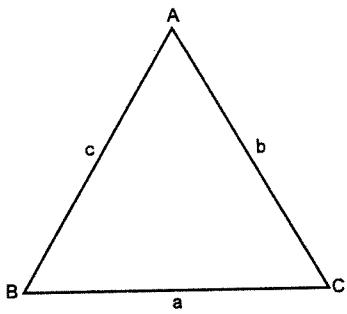


$x = ?$

Cevap:  $20^\circ$

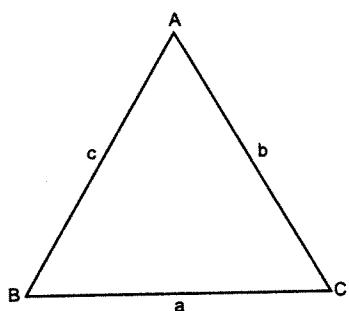
## AÇI - KENAR - BAĞINTILARI

1. Herhangi bir kenar, diğer iki kenarın toplamı ile farkı arasındadır.



$$\begin{aligned} b - c &< a < b + c \\ a - c &< b < a + c \\ a - b &< c < a + b \end{aligned}$$

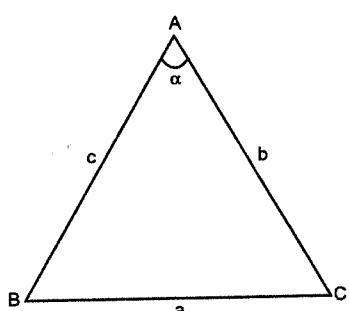
2.



$$a > b > c \Rightarrow m(\widehat{A}) > m(\widehat{B}) > m(\widehat{C})$$

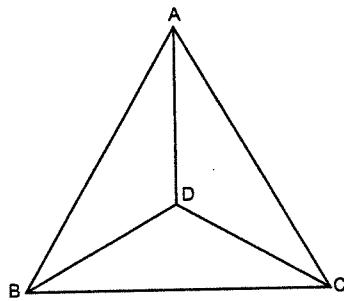
Büyük açının karşısında büyük kenar, küçük açının karşısında küçük kenar bulunur.

3.



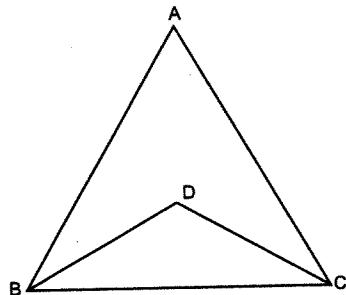
$$\begin{aligned} \alpha = 90^\circ &\Rightarrow a^2 = b^2 + c^2 \\ \alpha > 90^\circ &\Rightarrow a^2 > b^2 + c^2 \\ \alpha < 90^\circ &\Rightarrow a^2 < b^2 + c^2 \text{ dir.} \end{aligned}$$

4.



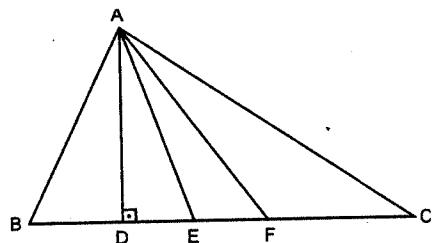
$$\frac{\text{Çevre } (\widehat{ABC})}{2} < |AD| + |DB| + |DC| < \zeta(\widehat{ABC})$$

5.



$$|BC| < |BD| + |DC| < |AB| + |AC|$$

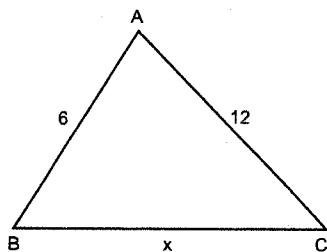
6.



$$\begin{aligned} |AD| &= h_a \rightarrow \text{yükseklik} \\ |AE| &= n_a \rightarrow \text{açıortay} \\ |AF| &= v_a \rightarrow \text{kenarortay ise} \end{aligned}$$

$h_a < n_a < v_a$  ilişkisi vardır.

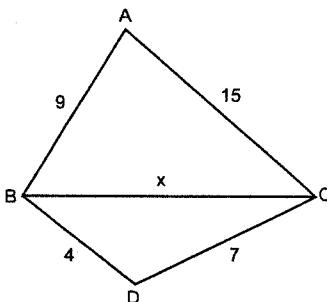
1.



$x$  in alabileceği kaç tane tam-sayı değeri vardır?

Cevap: 11

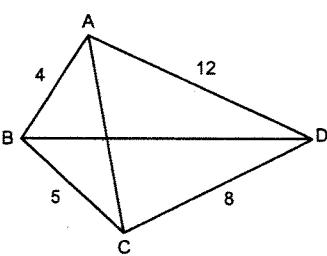
2.



$x$  in alibileceği kaç tane tam-sayı değeri vardır?

Cevap: 4

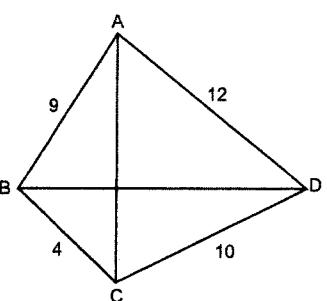
3.



$|AC|, |BD| \in \mathbb{Z}$   
 $|AC| + |BD|$  in en büyük değeri kaçtır?

Cevap: 20

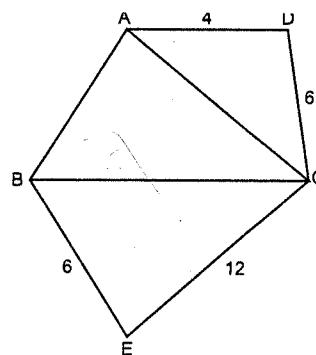
4.



$|AC| + |BD|$  toplamının en büyük tam-sayı değeri kaçtır?

Cevap: 26

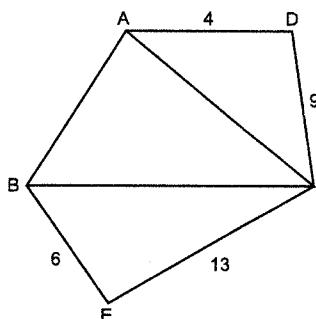
5.



$|AB| \in \mathbb{Z}^+$   
ABC eşkenar üçgenin çevresinin en büyük değeri kaçtır?

Cevap: 27

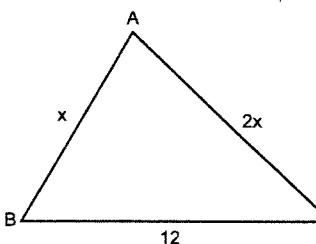
6.



ABC eşkenar üçgenin çevresinin en küçük değeri kaçtır?

Cevap: 22

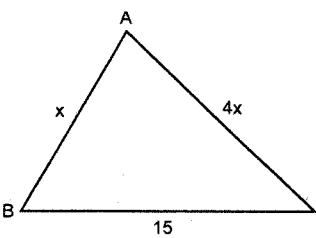
7.



$x \in \mathbb{Z}$   
 $\mathcal{C}(ABC)$  nin en büyük değeri ile en küçük değerinin toplamı kaçtır?

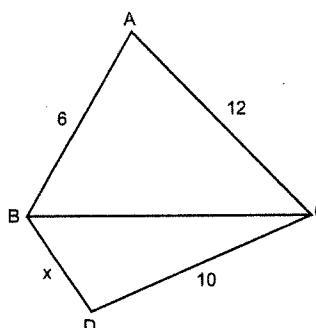
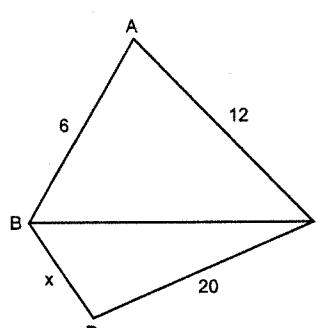
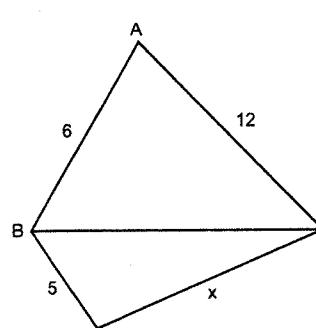
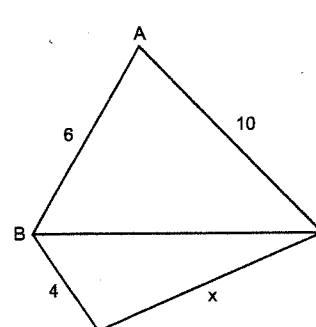
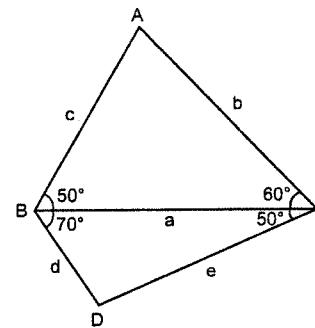
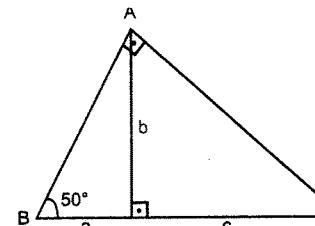
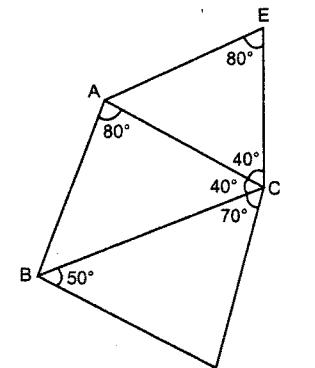
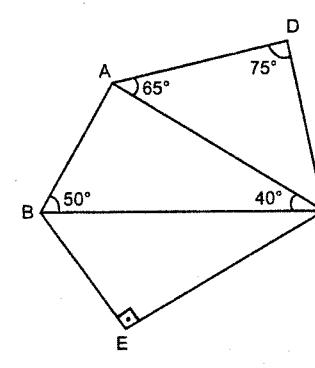
Cevap: 72

8.

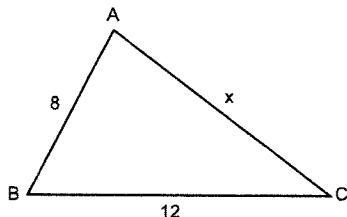


$\mathcal{C}(ABC)$  nin en büyük tamsayı değeri ile en küçük tamsayı değeri farkı kaçtır?

Cevap: 8

- 9.**   $x$  in en küçük tamsayı değeri kaçtır?
- Cevap: 1
- 10.**   $x$  in en küçük tamsayı değeri kaçtır?
- Cevap: 3
- 11.**   $x$  in en büyük tamsayı değeri kaçtır?
- Cevap: 22
- 12.**   $x$  in en büyük tamsayı değeri kaçtır?
- Cevap: 19
- 13.**  Şekildeki en büyük kenar hangisidir?
- Cevap: e
- 14.**  a, b, c arasındaki sıralamayı bulunuz?
- Cevap:  $c > b > a$
- 15.**  En büyük kenar hangisidir?
- Cevap:  $|BD|$
- 16.**  En uzun kenar hangisidir?
- Cevap:  $|BC|$

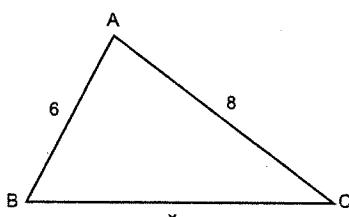
17.



$m(\widehat{A}) > m(\widehat{B}) \Rightarrow x$  in  
kaç tamsayı değeri vardır?

Cevap: 7

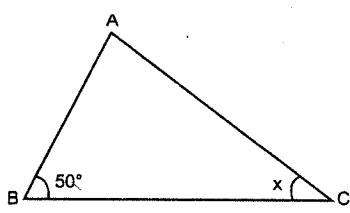
18.



$m(\widehat{A}) > m(\widehat{B}) > m(\widehat{C})$   
x in kaç tamsayı değeri vardır?

Cevap: 5

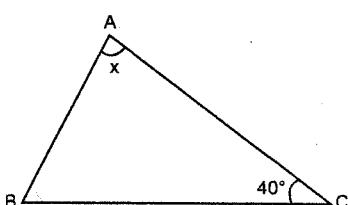
19.



$|BC| > |AC|$  ise  
x in en büyük tamsayı değeri kaçtır?

Cevap: 79

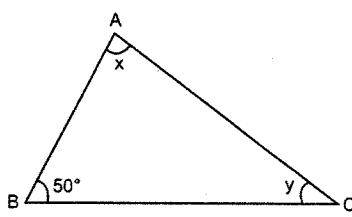
20.



$|BC| > |AC|$  ise  
x in en büyük tamsayı değeri kaçtır?

Cevap: 139

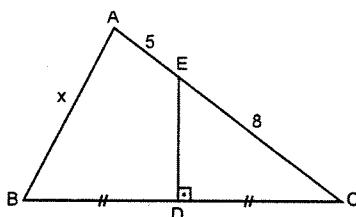
21.



$|BC| > |AC| > |AB|$  ise  
x in en büyük değeri ile en küçük değeri toplamı kaçtır?

Cevap: 210

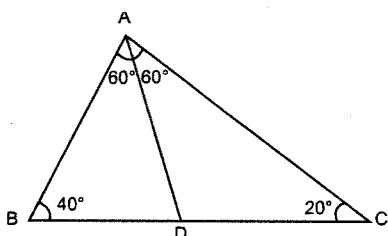
22.



x in alabileceği tamsayı değerleri toplamı kaçtır?

Cevap: 72

23.

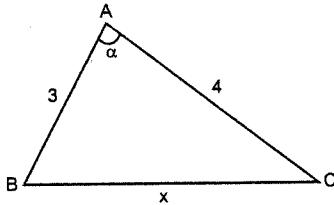


Aşağıdakilerden kaç tanesi doğrudur?

- $|AC| > |AB|$
- $|DC| > |AD|$
- $|BD| > |AD|$
- $|AB| > |BD|$
- $|BC| > |AD|$
- $|AC| > |AB|$
- $|DC| > |BD|$

Cevap: 7

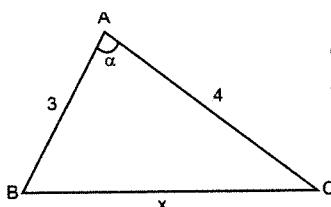
24.



$\alpha > 90^\circ$   
 $x \in \mathbb{Z}^+$   
 $x$  in değeri kaçtır?

Cevap: 6

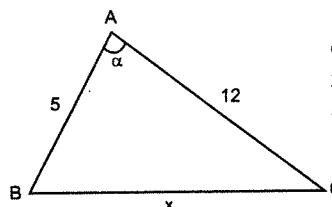
25.



$\alpha < 90^\circ$   
 $x$  in kaç tamsayı değeri vardır?

Cevap: 3

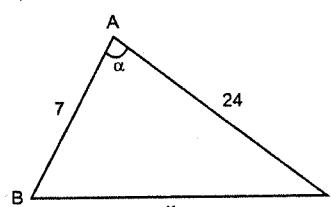
26.



$\alpha > 90^\circ$   
 $x$  in kaç tamsayı değeri vardır?

Cevap: 3

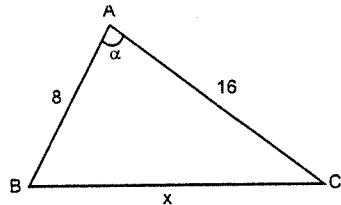
27.



$\alpha < 90^\circ$   
 $x$  in kaç tamsayı değeri vardır?

Cevap: 7

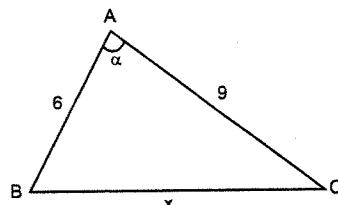
28.



$\alpha = 90^\circ$   
 $x = ?$

Cevap:  $8\sqrt{5}$ 

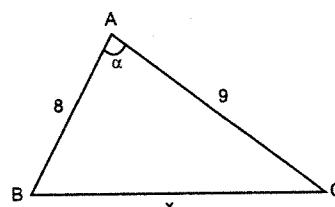
29.



$\alpha < 90^\circ$   
 $x$  in en büyük tamsayı değeri kaçtır?

Cevap: 10

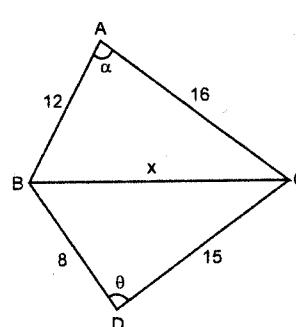
30.



$\alpha > 90^\circ$   
 $x$  in en küçük tamsayı değeri kaçtır?

Cevap: 13

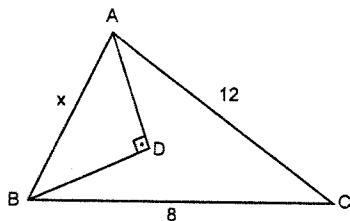
31.



$\alpha < 90^\circ$   
 $\theta > 90^\circ$   
 $x$  in alabileceği tam sayı değerleri toplamı kaçtır?

Cevap: 37

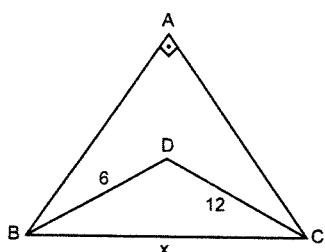
32.



$x$  in en büyük tamsayı değeri kaçtır?

Cevap: 14

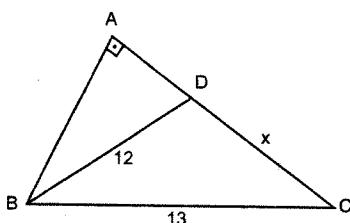
33.



$x$  in en küçük tamsayı değeri kaçtır?

Cevap: 14

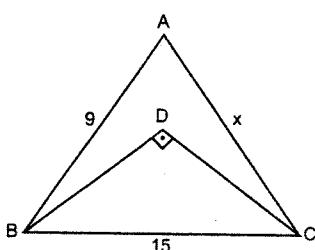
34.



$x$  in alabileceği tamsayı değerleri kaç tanedir?

Cevap: 3

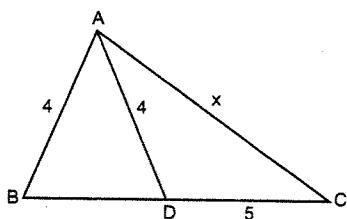
35.



$x$  in alabileceği kaç tamsayı değeri vardır?

Cevap: 11

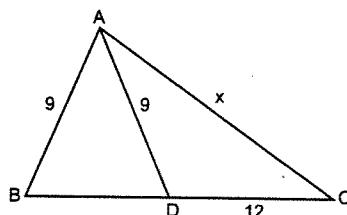
36.



$x$  in en küçük tamsayı değeri kaçtır?

Cevap: 7

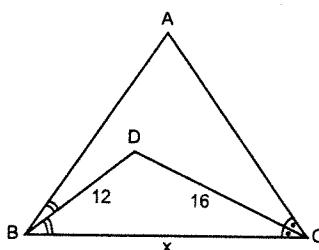
37.



$x$  in kaç tam sayı değeri vardır?

Cevap: 5

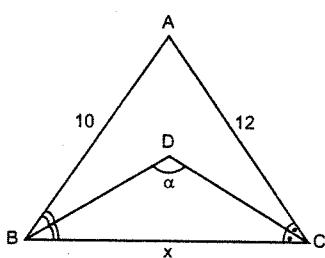
38.



$x$  in kaç tamsayı değeri vardır?

Cevap: 7

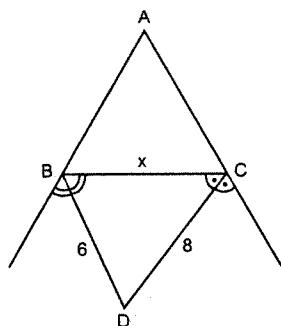
39.



$\alpha > 135$   
 $x$  in en küçük tamsayı değeri kaçtır?

Cevap: 16

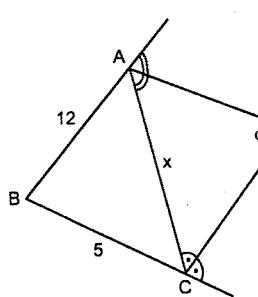
40.



$x$  in alabileceği tamsayı değerleri kaç tanedir?

Cevap: 4

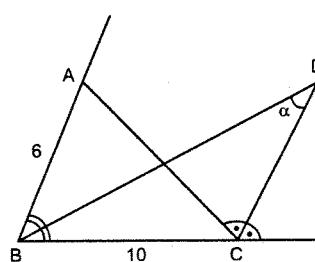
41.



$\alpha < 45^\circ$   
 $x$  in en küçük tam sayı değeri kaçtır?

Cevap: 14

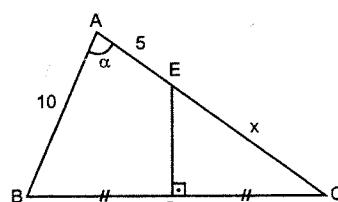
42.



$\alpha > 45^\circ$   
 $|AC|$  nin alabileceği tamsayı değerleri kaç tanedir?

Cevap: 3

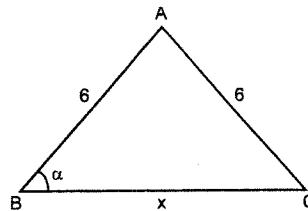
43.



$\alpha > 90^\circ$   
 $x$  in en küçük tam sayı değeri kaçtır?

Cevap: 12

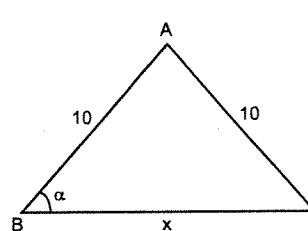
44.



$\alpha < 45^\circ$   
 $x$  in alabileceği en küçük tam sayı değeri kaçtır?

Cevap: 9

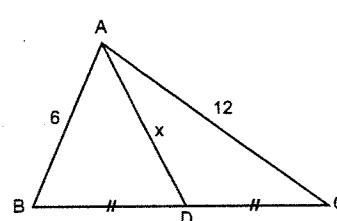
45.



$\alpha > 45^\circ$   
 $x$  in alabileceği en büyük tam sayı değeri kaçtır?

Cevap: 14

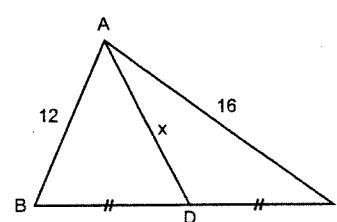
46.



$x$  in kaç tam sayı değeri vardır?

Cevap: 5

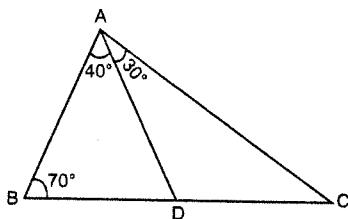
47.



$m(\widehat{A}) > 90^\circ$   
 $x$  in kaç tam sayı değeri vardır?

Cevap: 7

48.

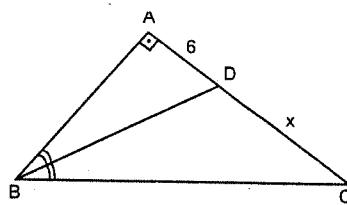


Aşağıdakilerden kaç tanesi yanlışır?

1.  $|AB| = |AD|$
2.  $|BC| > |AD|$
3.  $|AC| > |AD|$
4.  $|AC| = |BC|$
5.  $|DC| > |AB|$
6.  $|BD| < |AD|$

Cevap: 1

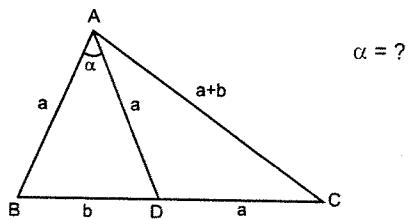
51.



x in en küçük tam sayı değeri kaçtır?

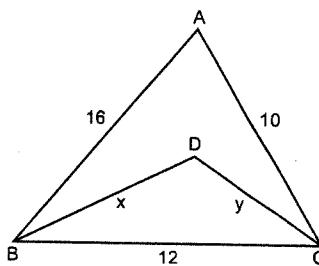
Cevap: 7

49.

 $\alpha = ?$ 

Cevap: 36

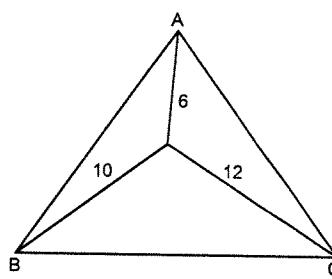
52.



x+y nin en küçük ve en büyük tam sayı değerleri toplamı kaçtır?

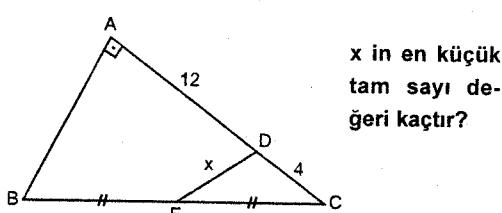
Cevap: 38

53.

Çevre  $(\widehat{ABC})$  nin en büyük tamsayı değeri kaçtır?

Cevap: 55

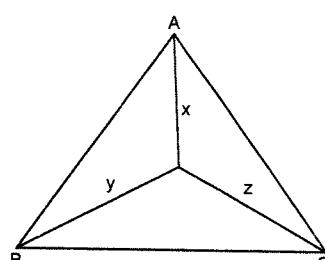
50.



x in en küçük tam sayı değeri kaçtır?

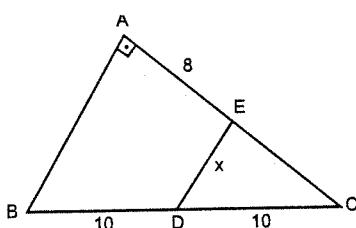
Cevap: 5

54.

 $\widehat{C(ABC)} = 30 \text{ cm}$  ise  $x+y+z$  nin en büyük ve en küçük tamsayı değerleri toplamı kaçtır?

Cevap: 45

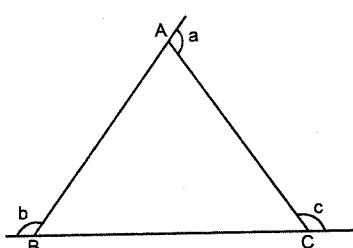
55.



$x$  in alabileceği en büyük tam sayı değeri kaçtır?

Cevap: 9

56.



$a + c > 2b$  ise  $b$  nin en büyük tam sayı değeri kaçtır?

Cevap: 119

57.  $a > b > c$  ise

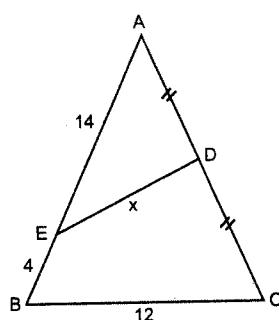
yardımcı elemanları arasındaki sıralama yukarıdaki eşitsizliğin tam tersidir.

Bu bilgiye göre, aşağıdakilerden kaç tanesi doğrudur?

- I.  $h_a < h_b < h_c$  Yükseklik
- II.  $v_a < v_b < v_c$  Kenarortay
- III.  $n_a < n_b < n_c$  Açıortay
- IV.  $\frac{1}{h_a} > \frac{1}{h_b} > \frac{1}{h_c}$
- V.  $h_a < v_a < v_a$

Cevap: 5

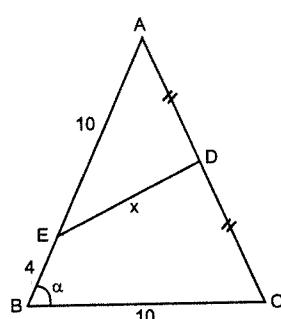
58.



$x$  in kaç tam sayı değeri vardır?

Cevap: 9

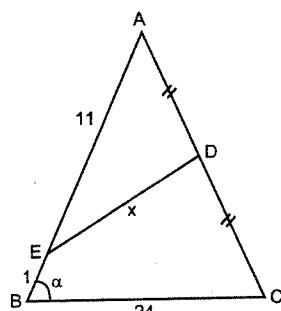
59.



$\alpha < 90^\circ$   
 $x$  in en küçük tam sayı değeri kaçtır?

Cevap: 6

60.



$\alpha < 90^\circ$   
 $x$  in en küçük tam sayı değeri kaçtır?

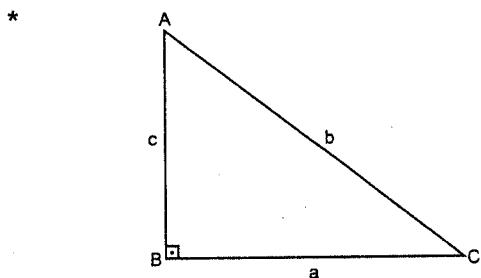
Cevap: 14

## ÖZEL ÜÇGENLER

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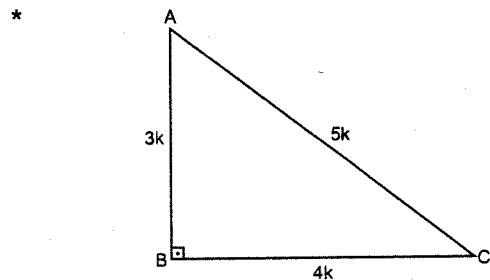


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**Pisagor Bağıntısı**

$$b^2 = a^2 + c^2$$



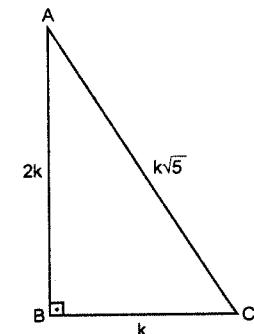
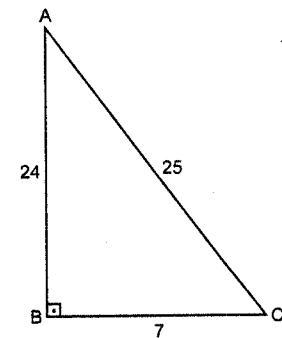
$k = 1 \Rightarrow 3 - 4 - 5$  üçgeni

$k = 2 \Rightarrow 6 - 8 - 10$  üçgeni

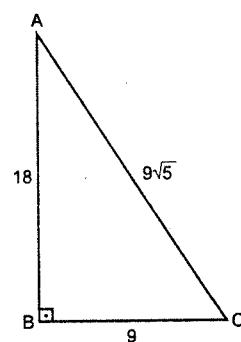
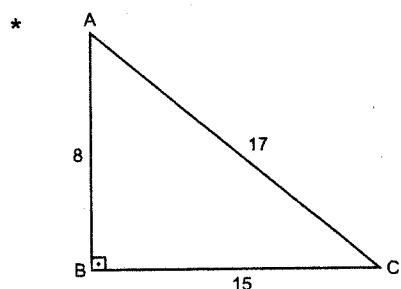
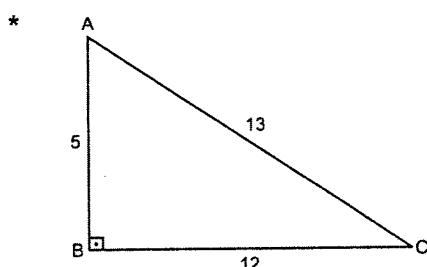
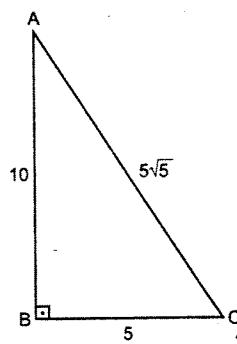
$k = 3 \Rightarrow 9 - 12 - 15$  üçgeni

$k = 4 \Rightarrow 12 - 16 - 20$  üçgeni

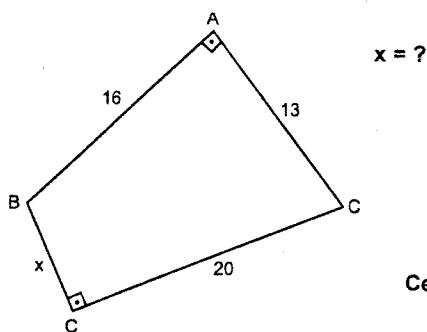
$k = 5 \Rightarrow 15 - 20 - 25$  üçgeni



**Örnek:**



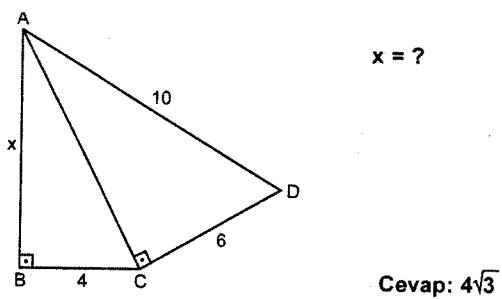
1.



$x = ?$

Cevap: 5

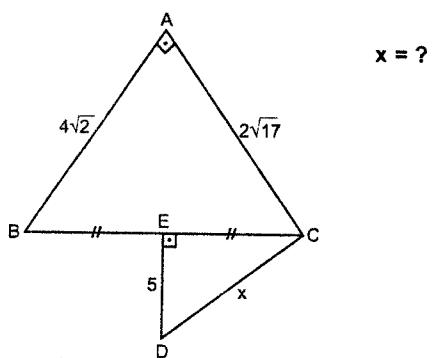
2.



$x = ?$

Cevap:  $4\sqrt{3}$ 

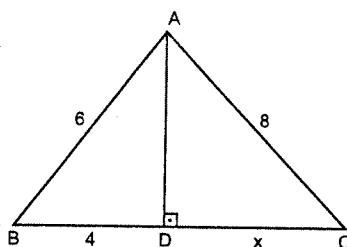
3.



$x = ?$

Cevap:  $5\sqrt{2}$ 

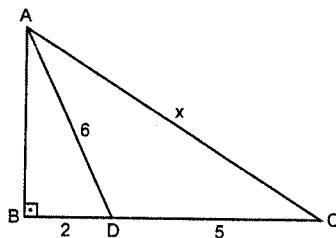
4.



$x = ?$

Cevap:  $2\sqrt{11}$ 

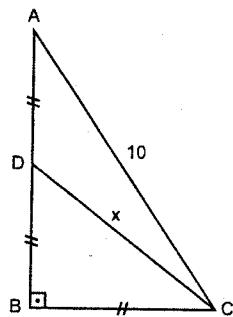
5.



$x = ?$

Cevap: 9

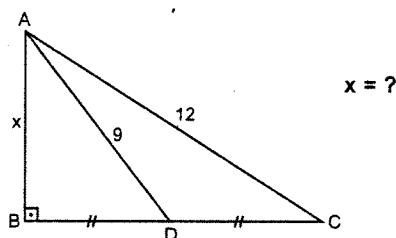
6.



$x = ?$

Cevap:  $2\sqrt{10}$

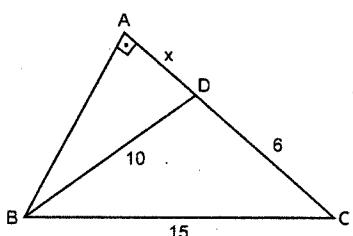
7.



$x = ?$

$\text{Cevap: } 2\sqrt{15}$

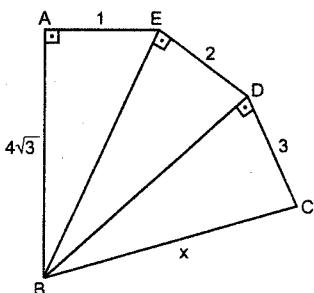
8.



$x = ?$

$\text{Cevap: } \frac{89}{12}$

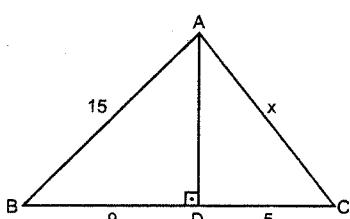
9.



$x = ?$

$\text{Cevap: } \sqrt{62}$

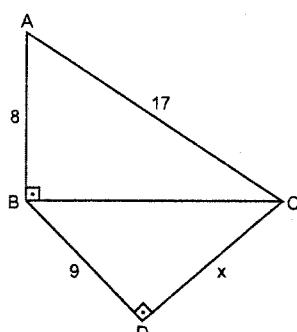
10.



$x = ?$

$\text{Cevap: } 13$

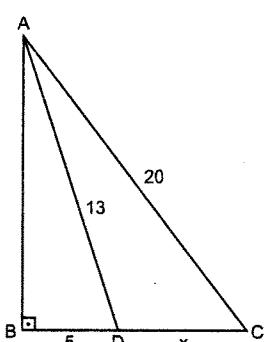
11.



$x = ?$

$\text{Cevap: } 12$

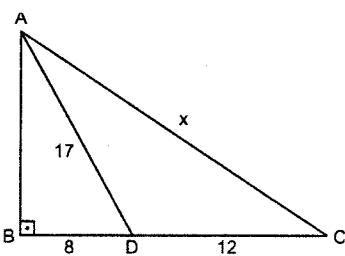
12.



$x = ?$

$\text{Cevap: } 11$

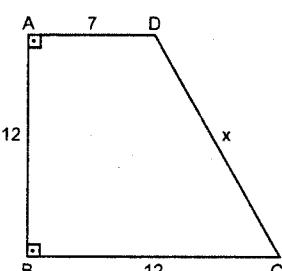
13.



$x = ?$

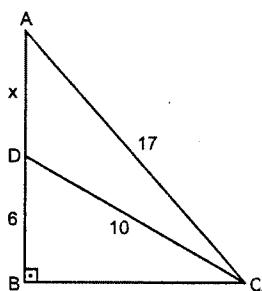
$\text{Cevap: } 25$

14.



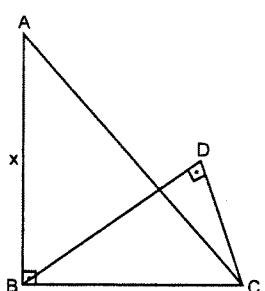
$x = ?$

$\text{Cevap: } 13$

**15.**

$x = ?$

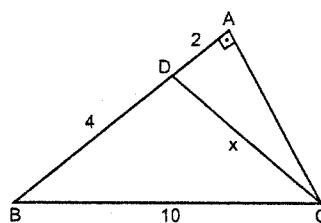
Cevap: 9

**16.**

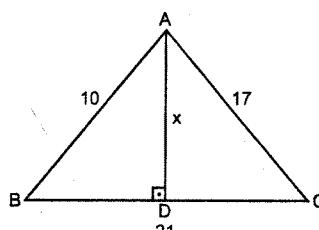
$$\begin{aligned}|BD| &= 12 \\ |DC| &= 9 \\ |AC| &= 17\end{aligned}$$

$x = ?$

Cevap: 8

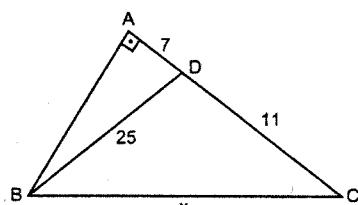
**19.**

$x = ?$

Cevap:  $2\sqrt{17}$ **20.**

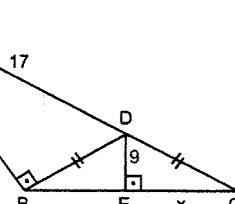
$x = ?$

Cevap: 8

**17.**

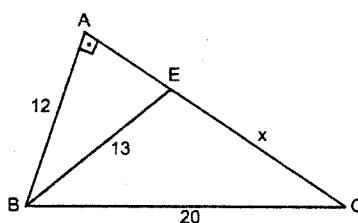
$x = ?$

Cevap: 30

**21.**

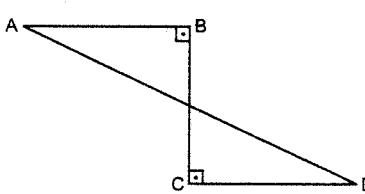
$x = ?$

Cevap: 12

**18.**

$x = ?$

Cevap: 11

**22.**

$|AB| = 7$

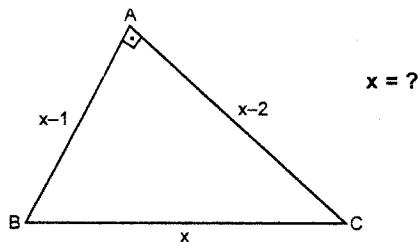
$|BC| = 5$

$|CD| = 5$

$|AD| = ?$

Cevap: 13

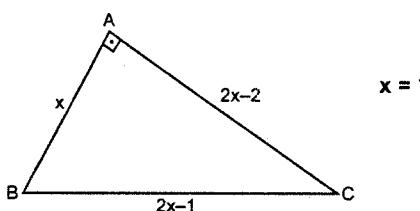
23.



$x = ?$

Cevap: 5

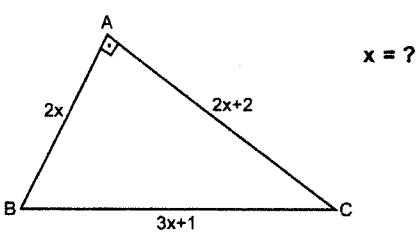
24.



$x = ?$

Cevap: 3

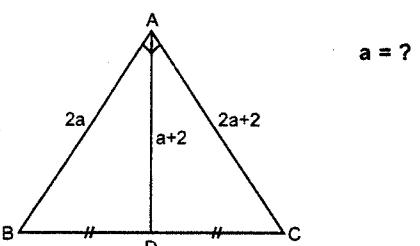
25.



$x = ?$

Cevap: 3

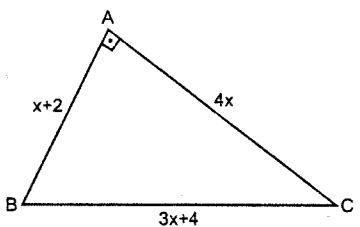
26.



$a = ?$

Cevap: 3

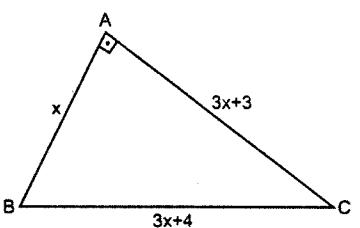
27.



$x = ?$

Cevap: 3

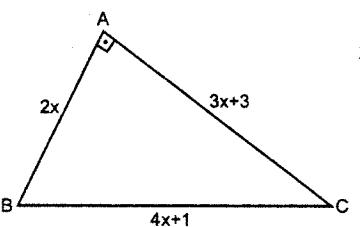
28.



$x = ?$

Cevap: 7

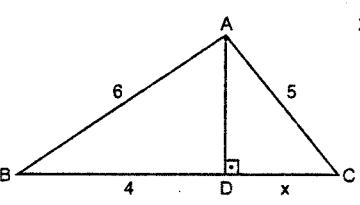
29.



$x = ?$

Cevap: 4

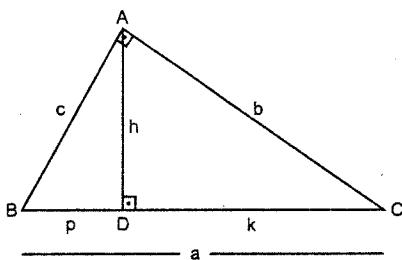
30.



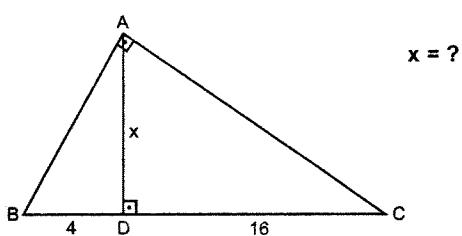
$x = ?$

Cevap:  $\sqrt{5}$

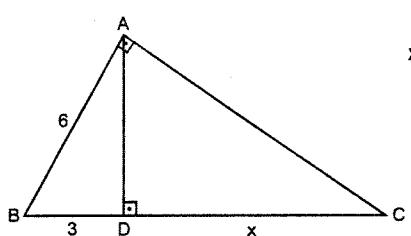
## ÖKLİD BAĞINTILARI



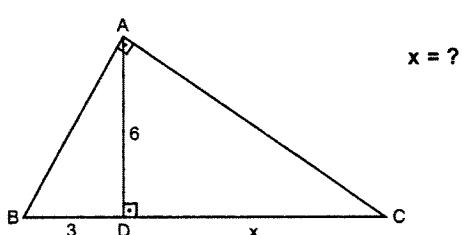
1.  $h^2 = P \cdot k$
2.  $c^2 = P \cdot a$
3.  $b^2 = k \cdot a$
4.  $a \cdot h = b \cdot c$

**31.**

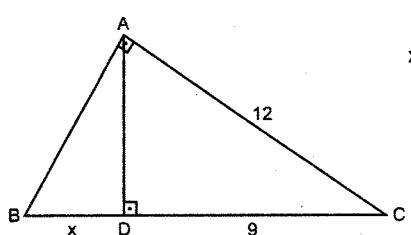
Cevap: 8

**34.**

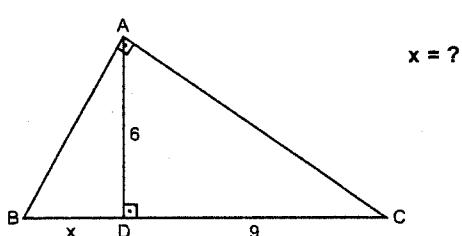
Cevap: 9

**32.**

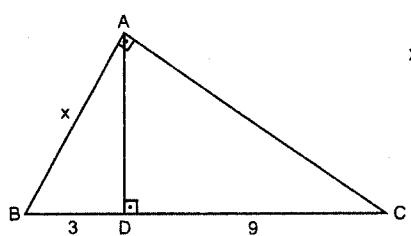
Cevap: 12

**35.**

Cevap: 7

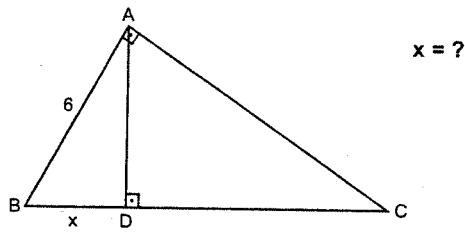
**33.**

Cevap: 4

**36.**

Cevap: 6

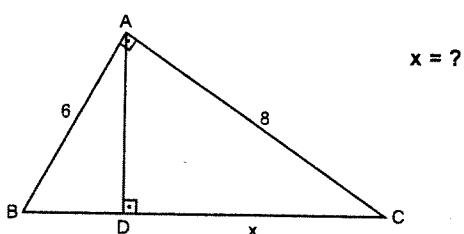
37.



$x = ?$

Cevap: 3,6

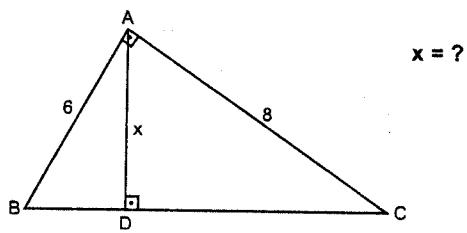
38.



$x = ?$

Cevap: 6,4

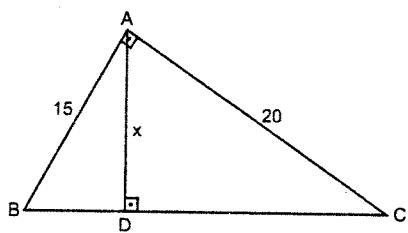
39.



$x = ?$

Cevap: 4,8

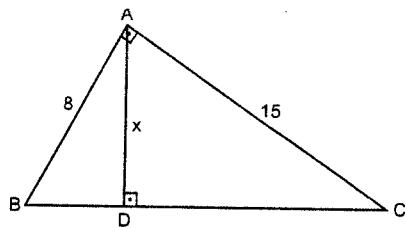
40.



$x = ?$

Cevap: 12

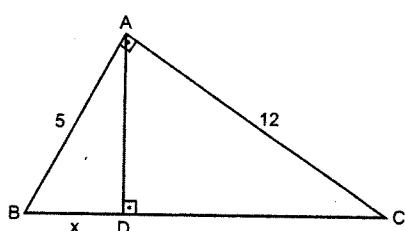
41.



$x = ?$

Cevap:  $\frac{120}{17}$ 

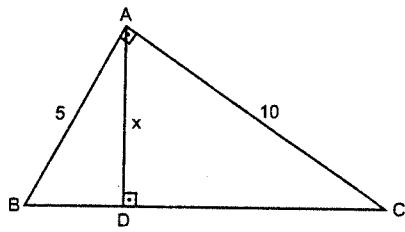
42.



$x = ?$

Cevap:  $\frac{25}{13}$ 

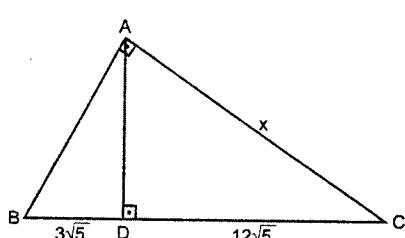
43.



$x = ?$

Cevap:  $2\sqrt{5}$ 

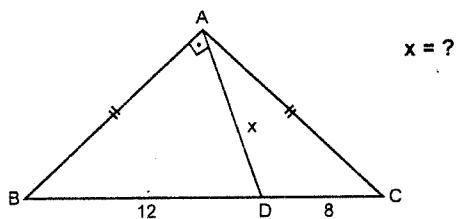
44.



$x = ?$

Cevap: 30

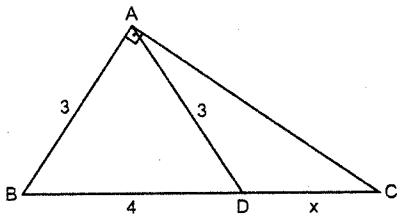
45.



$x = ?$

Cevap:  $2\sqrt{6}$ 

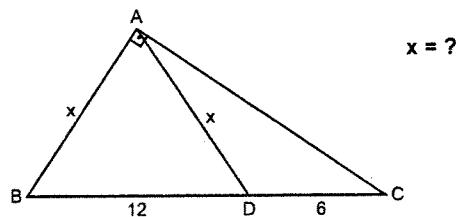
49.



$x = ?$

Cevap:  $\frac{1}{2}$ 

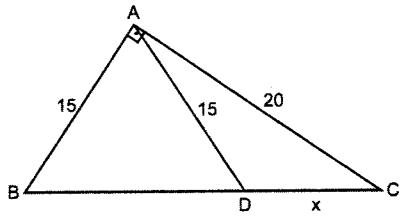
46.



$x = ?$

Cevap:  $6\sqrt{3}$ 

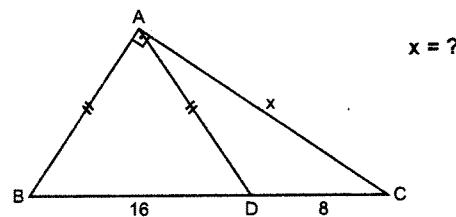
50.



$x = ?$

Cevap: 7

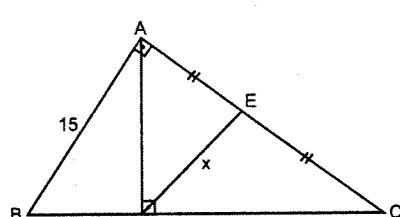
47.



$x = ?$

Cevap:  $8\sqrt{6}$ 

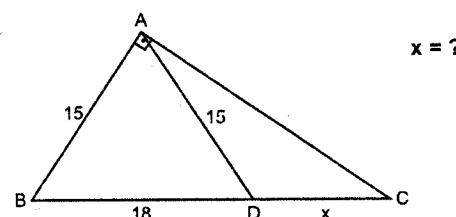
51.



$x = ?$

Cevap: 10

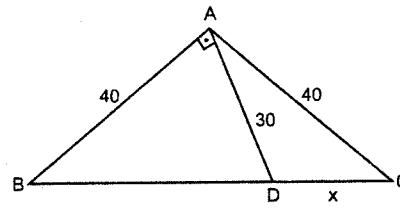
48.



$x = ?$

Cevap: 7

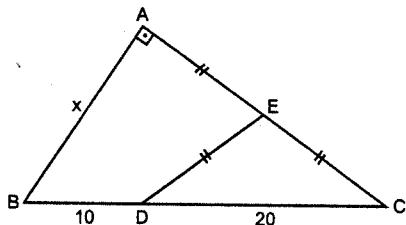
52.



$x = ?$

Cevap: 14

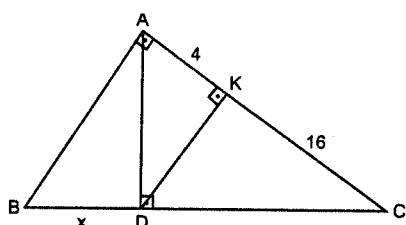
53.



$x = ?$

Cevap:  $10\sqrt{3}$ 

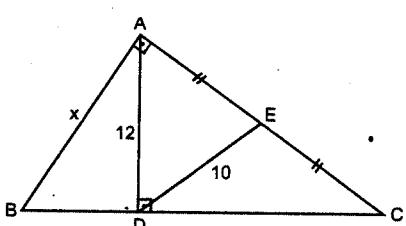
57.



$x = ?$

Cevap:  $2\sqrt{5}$ 

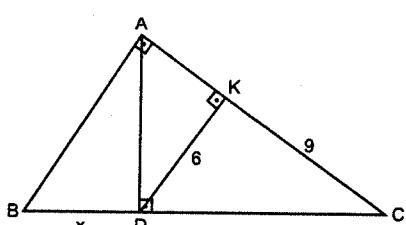
54.



$x = ?$

Cevap: 15

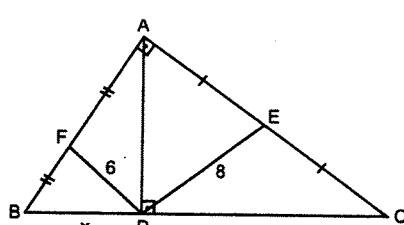
58.



$x = ?$

Cevap:  $\frac{4\sqrt{13}}{3}$ 

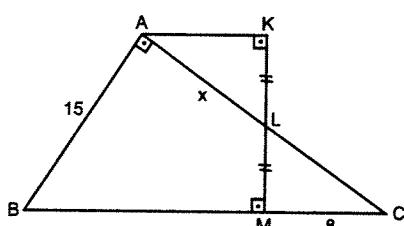
55.



$x = ?$

Cevap: 7,2

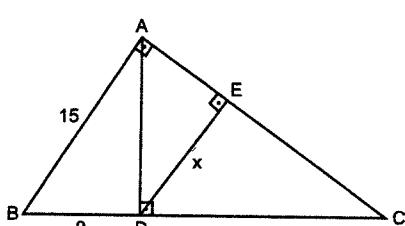
59.



$x = ?$

Cevap: 10

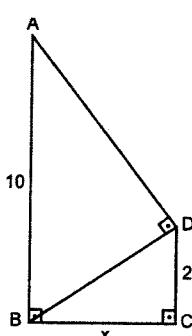
56.



$x = ?$

Cevap: 9,6

60.

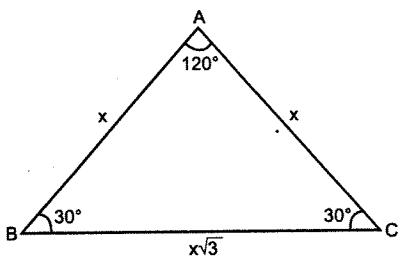
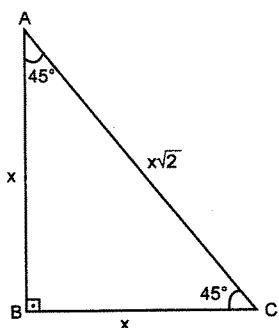
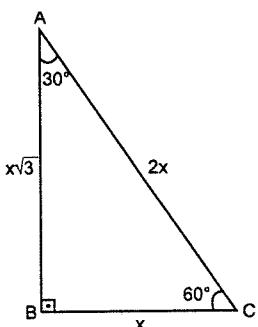


$x = ?$

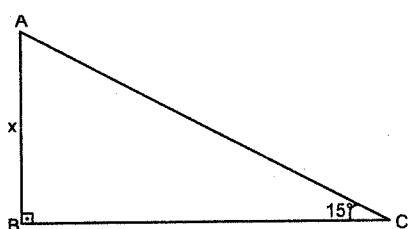
Cevap: 4

## Açılarına Göre Özel Üçgenler

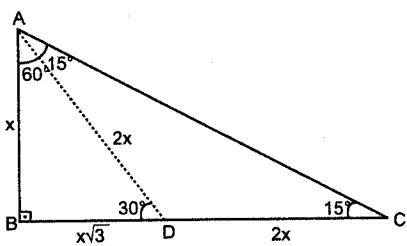
\*



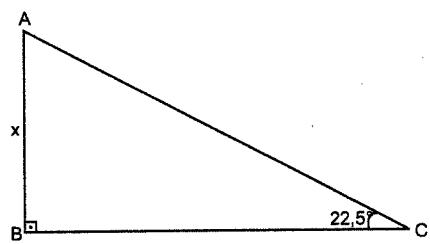
\*



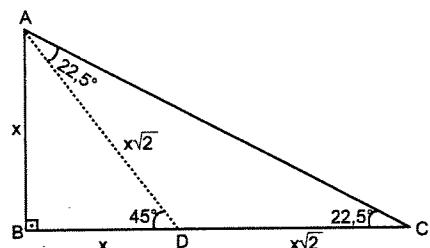
15° lik açı alınırsa



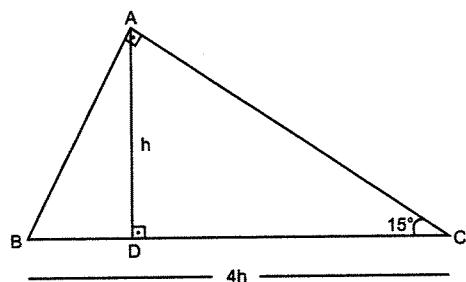
\*



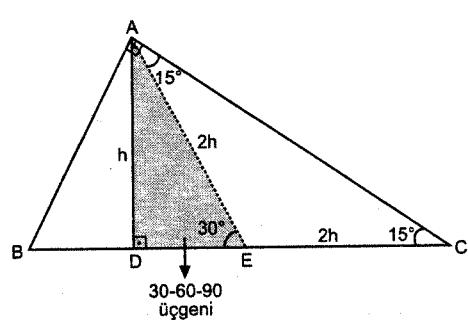
22.5° lik açı alınırsa



\*



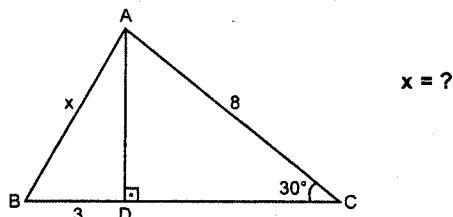
15 – 75 – 90 üçgeninde yükseklik, hipotenüsün 4'te birine eşittir.



|AE| = |EC| = |BE| = 2h

|BC| = 4h olur.

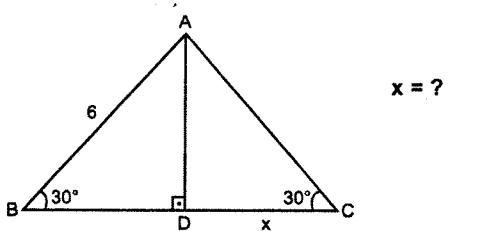
61.



$x = ?$

Cevap: 5

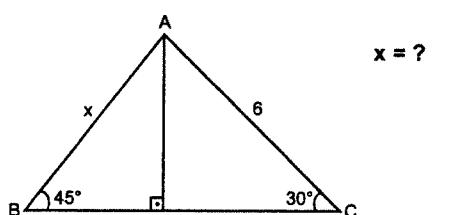
62.



$x = ?$

Cevap:  $3\sqrt{3}$ 

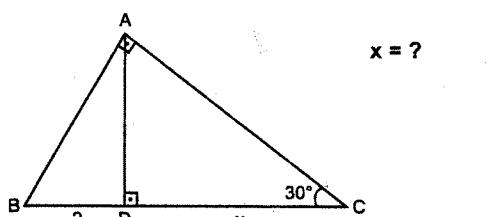
63.



$x = ?$

Cevap:  $3\sqrt{2}$ 

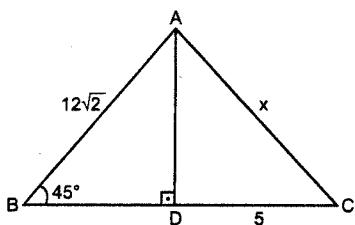
64.



$x = ?$

Cevap: 6

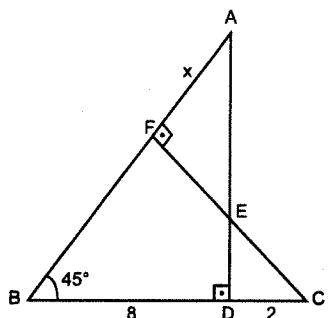
65.



$x = ?$

Cevap: 13

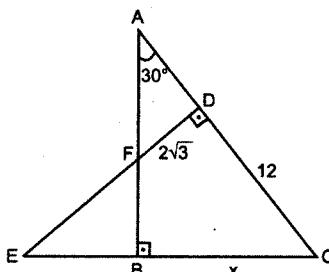
66.



$x = ?$

Cevap:  $3\sqrt{2}$ 

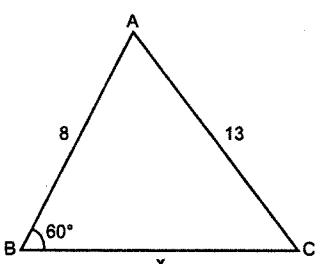
67.



$x = ?$

Cevap: 9

68.

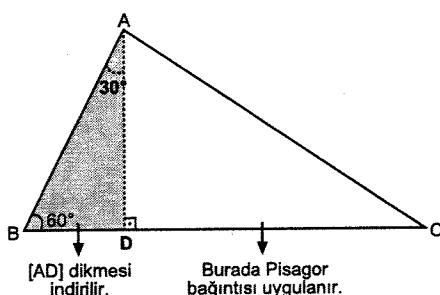
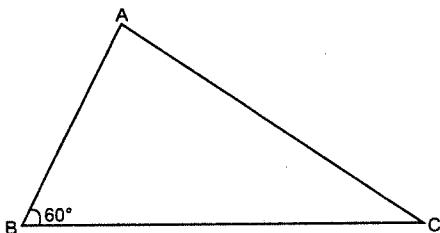


$x = ?$

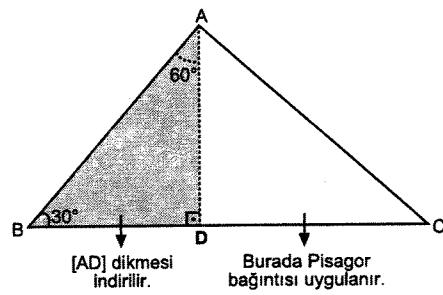
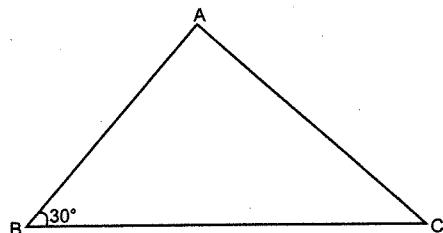
Cevap: 15

Bir üçgenin açılarından herhangi biri ( $30^\circ$ ,  $45^\circ$ ,  $60^\circ$ ) ise bu açıların karşısına bir dik indirelerek ( $30-60-90$ ) veya ( $45-45-90$ ) üçgenleri elde edilir.

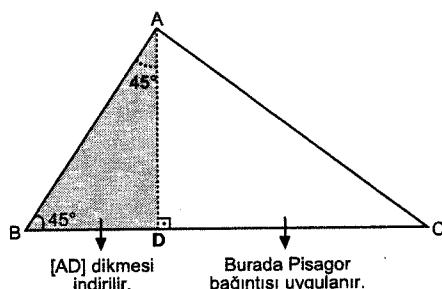
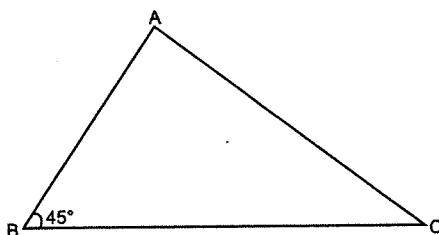
- \* Sorunun orjinali böyle ise;



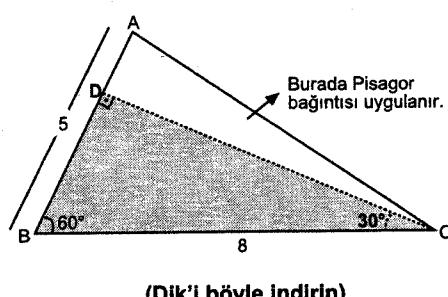
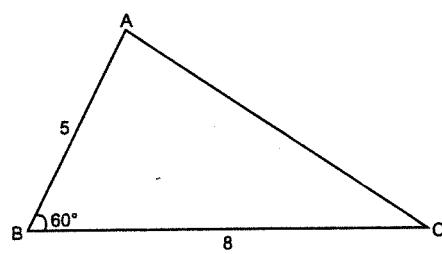
- \* Sorunun orjinali böyle ise;



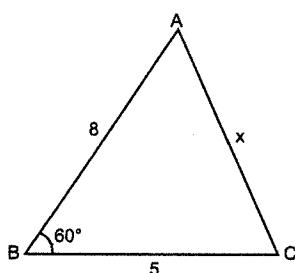
- \* Sorunun orjinali böyle ise;



- \* Yalnız dik indirirken hipotenüsün çift sayı olması na dikkat ediniz.

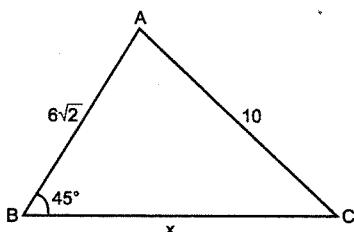


69.

 $x = ?$ 

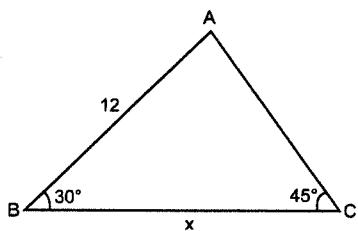
Cevap: 7

70.

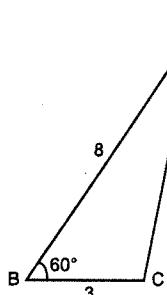
 $x = ?$ 

Cevap: 14

71.

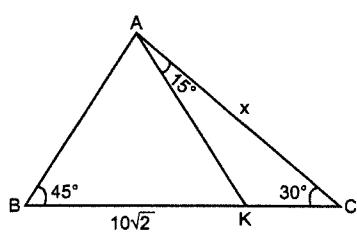
 $x = ?$ Cevap:  $6 + 6\sqrt{3}$ 

72.

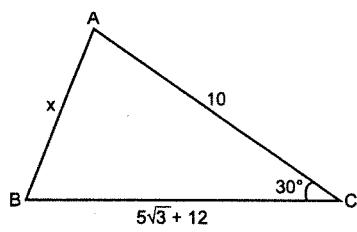
 $x = ?$ 

Cevap: 7

73.

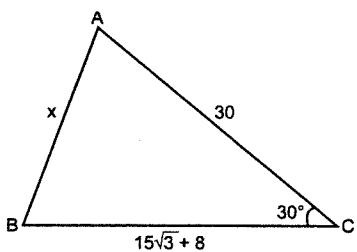
 $x = ?$ Cevap:  $10\sqrt{2}$ 

74.

 $x = ?$ 

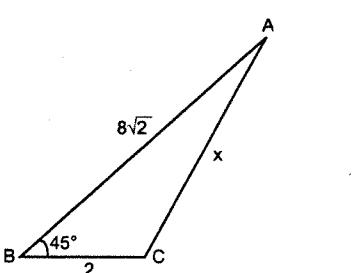
Cevap: 13

75.

 $x = ?$ 

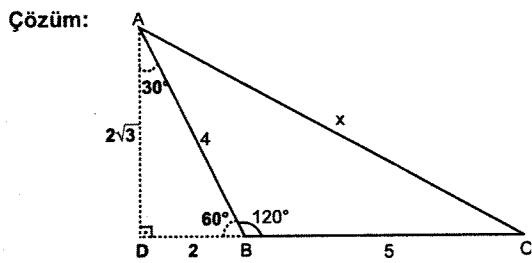
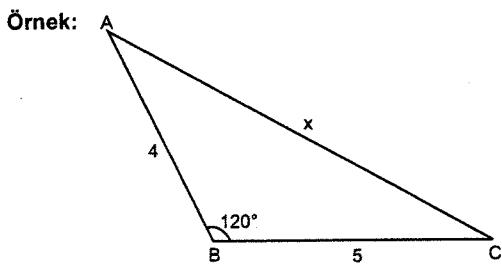
Cevap: 17

76.

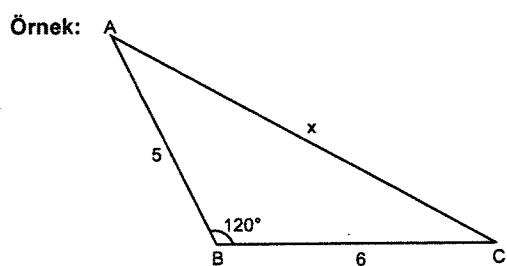
 $x = ?$ 

Cevap: 10

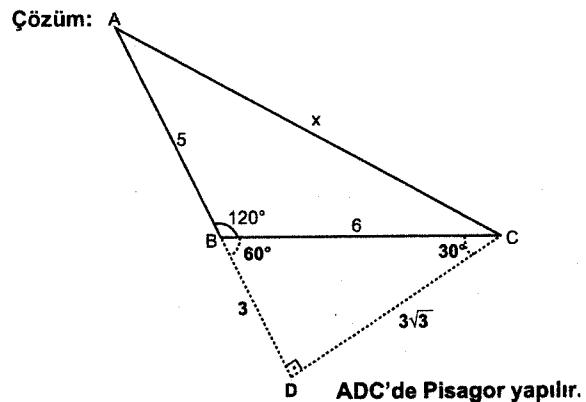
Bir üçgenin açılarından herhangi biri ( $120^\circ, 135^\circ, 150^\circ$ ) ise bu açıların dışına doğru bir dik indirerek ( $30^\circ-60^\circ-90^\circ$ ), veya ( $45^\circ-45^\circ-90^\circ$ ) üçgeni elde ederiz. Sonra büyük üçgende PİSAGOR bağıntısı ile soruyu çözeriz.



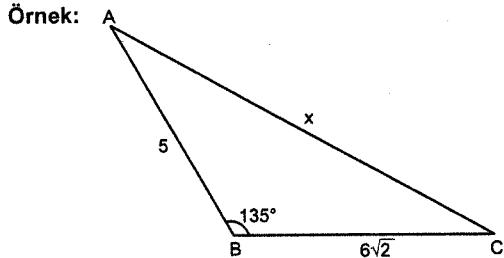
**ADC'de Pisagor yapılır.**



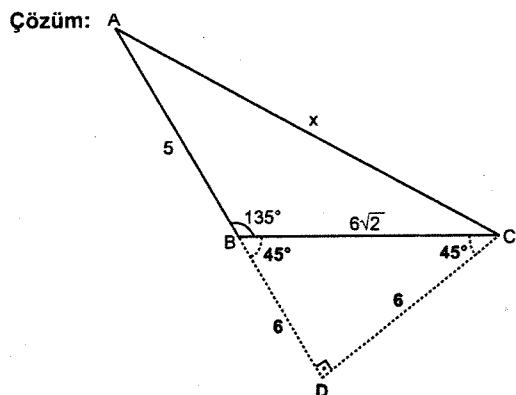
**(Dikkat! Çift sayıya doğru dik indiriniz)**



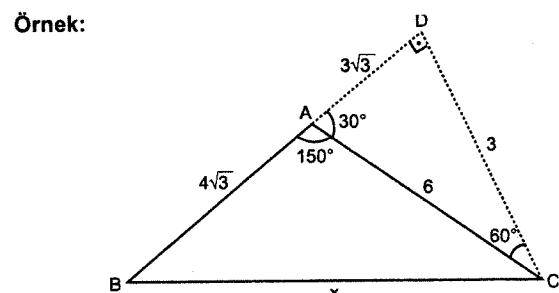
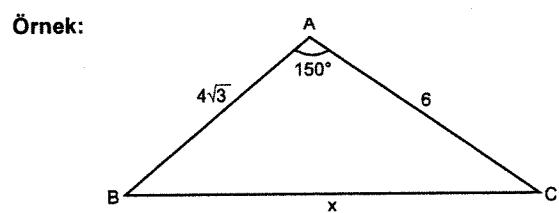
**ADC'de Pisagor yapılır.**



**(\sqrt{2} li sayıya doğru dik indiriniz)**

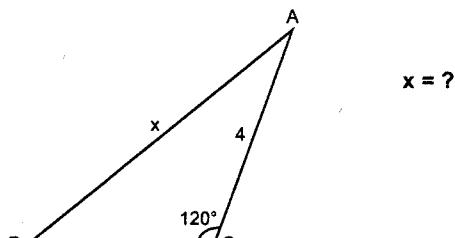


**ADC'de Pisagor yapılır.**

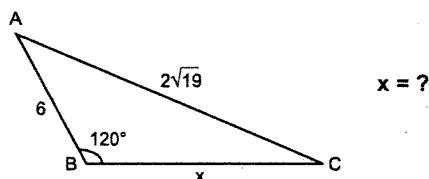


**BDC de Pisagor yapılır.**

77.

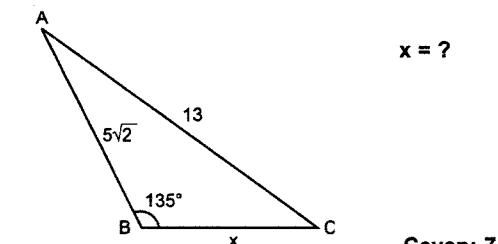
 $x = ?$ Cevap:  $2\sqrt{7}$ 

78.

 $x = ?$ 

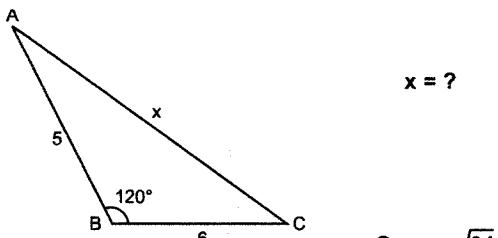
Cevap: 4

79.

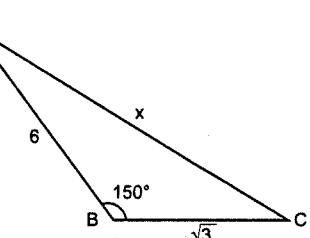
 $x = ?$ 

Cevap: 7

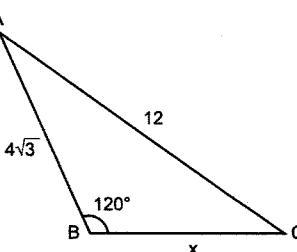
80.

 $x = ?$ Cevap:  $\sqrt{91}$ 

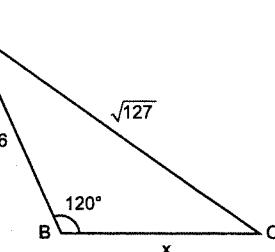
81.

 $x = ?$ Cevap:  $\sqrt{57}$ 

82.

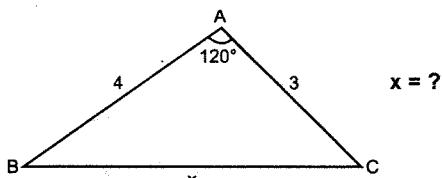
 $x = ?$ Cevap:  $4\sqrt{3}$ 

83.

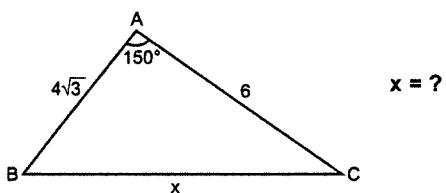
 $x = ?$ 

Cevap: 7

84.

 $x = ?$ Cevap:  $\sqrt{37}$

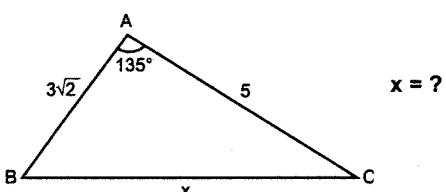
85.



$x = ?$

Cevap:  $2\sqrt{39}$ 

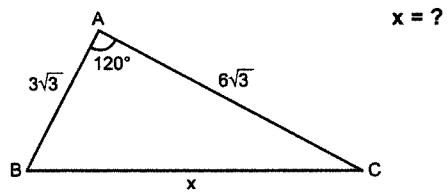
86.



$x = ?$

Cevap:  $\sqrt{73}$ 

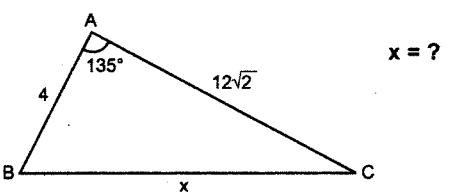
87.



$x = ?$

Cevap:  $3\sqrt{21}$ 

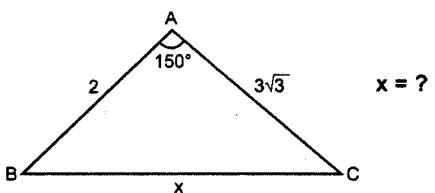
88.



$x = ?$

Cevap: 20

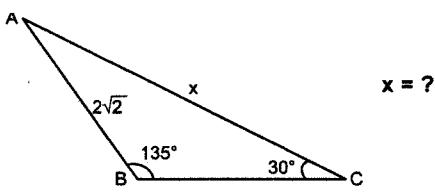
89.



$x = ?$

Cevap: 7

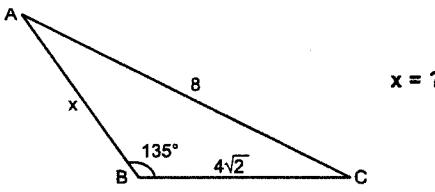
90.



$x = ?$

Cevap: 4

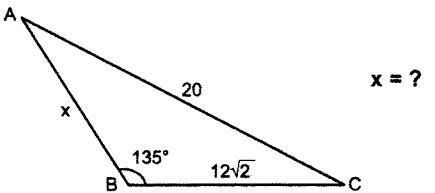
91.



$x = ?$

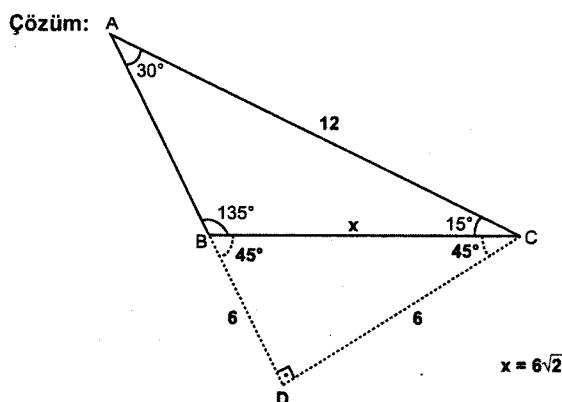
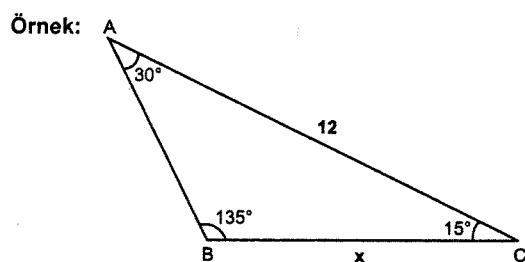
Cevap:  $4\sqrt{5} - 4$ 

92.



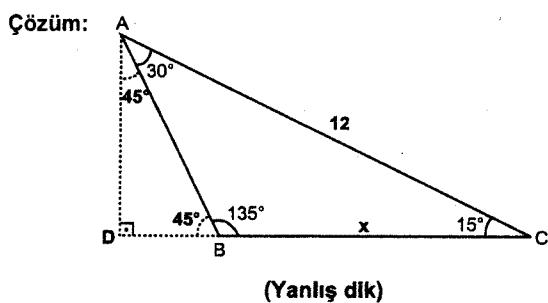
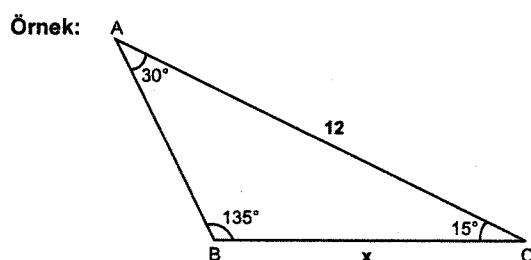
$x = ?$

Cevap: 4

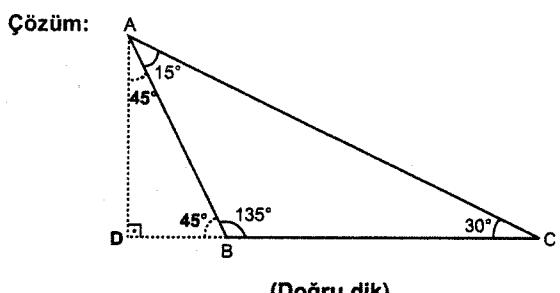
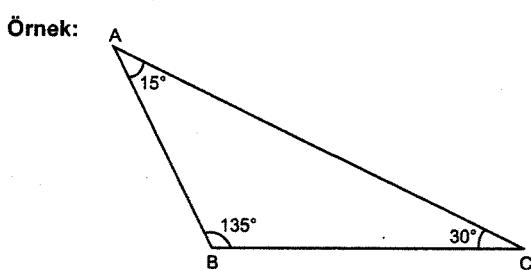
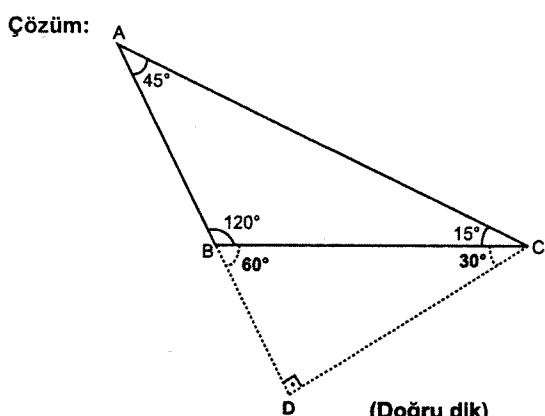
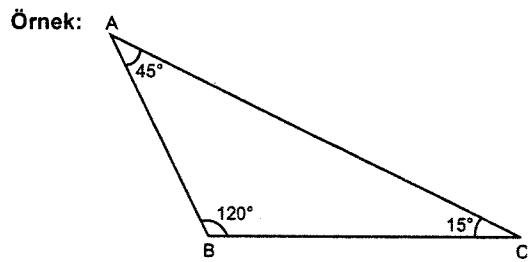


Bu tip sorularda arkada oluşan üçgen ile büyük üçgen (30-60-90 ve 45-45-90) çıkıyorsa doğru yere dik indirdik demektir.

15-75-90 üçgeni çıkıyorsa yanlış yere dik indirdik demektir.

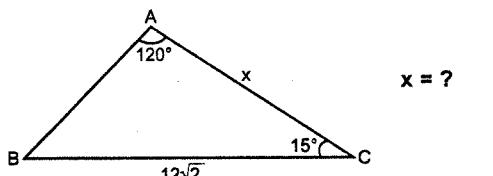


(Yanlış dik)



(Doğru dik)

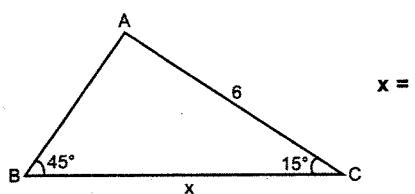
93.



$x = ?$

Cevap:  $8\sqrt{3}$ 

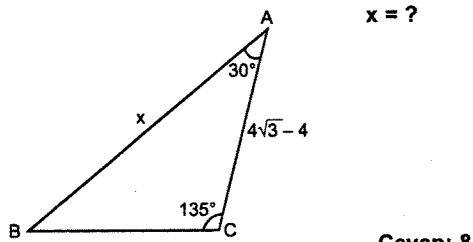
94.



$x = ?$

Cevap:  $3\sqrt{6}$ 

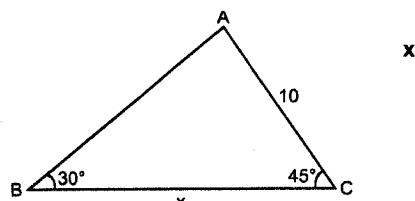
95.



Cevap: 8

$x = ?$

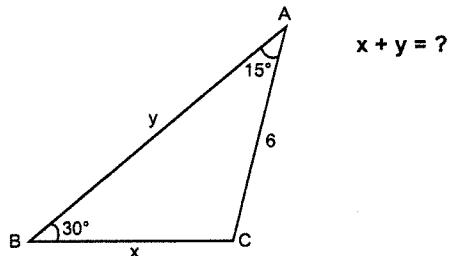
96.



$x = ?$

Cevap:  $5\sqrt{6} + 5\sqrt{2}$ 

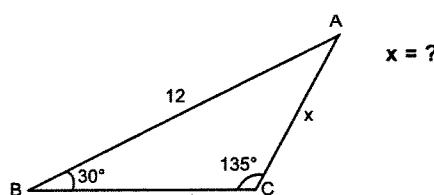
97.



$x + y = ?$

Cevap:  $3\sqrt{2} + 3\sqrt{6}$ 

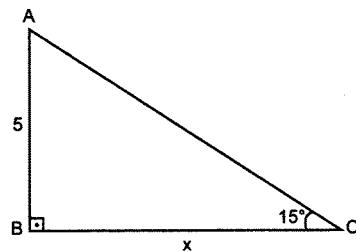
98.



$x = ?$

Cevap:  $6\sqrt{2}$ 

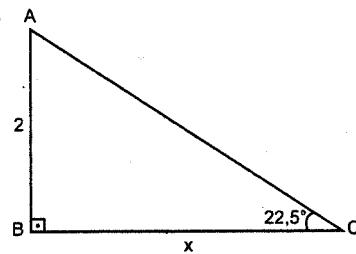
99.



$x = ?$

Cevap:  $5\sqrt{3} + 10$ 

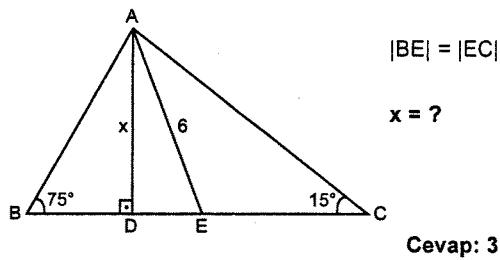
100.



$x = ?$

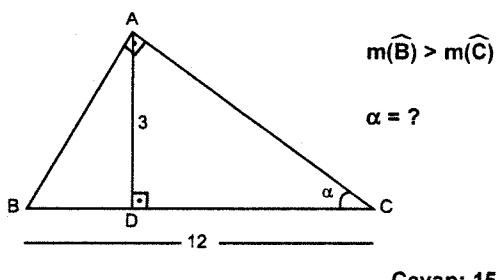
Cevap:  $2 + 2\sqrt{2}$

101.



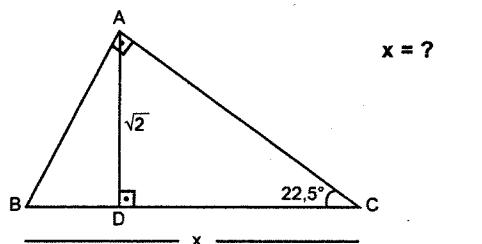
Cevap: 3

102.



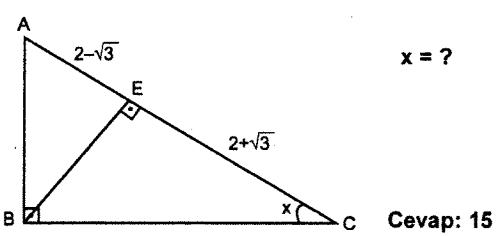
Cevap: 15

103.



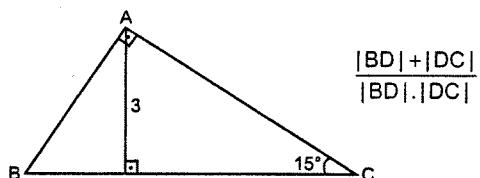
Cevap: 4

104.

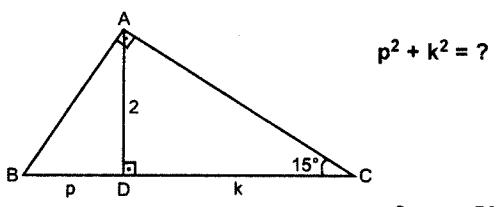


Cevap: 15

105.

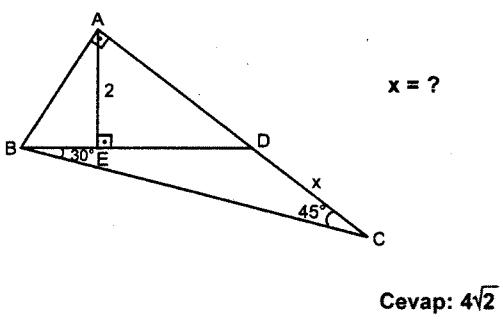
Cevap:  $\frac{4}{3}$ 

106.

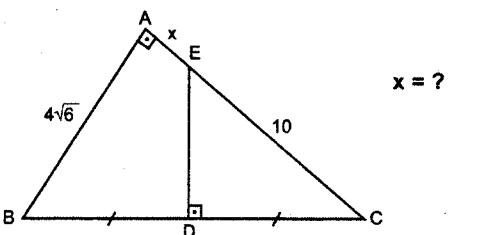


Cevap: 56

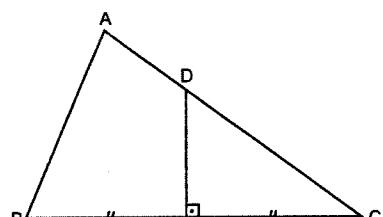
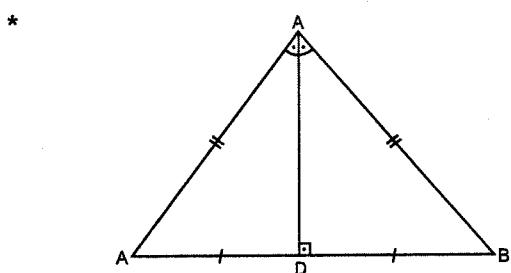
107.

Cevap:  $4\sqrt{2}$ 

108.

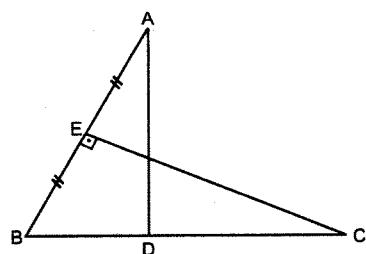
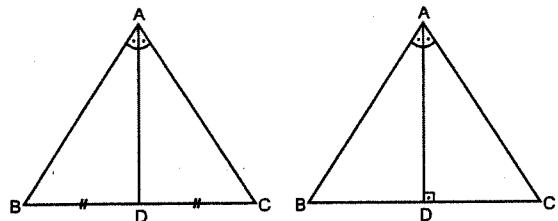


Cevap: 2



(B ile D birleştirilir.)

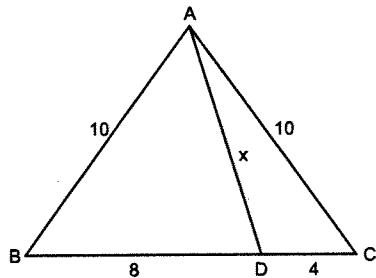
Aşağıdaki şekiller yukarıdaki şekele dönüştürülür.



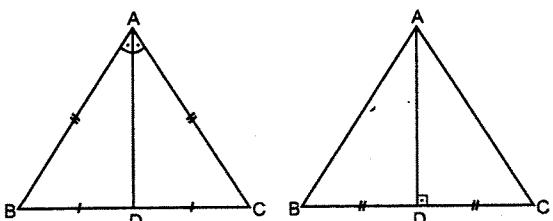
(A ile C birleştirilir.)

- \*
- Kenarları verilen tüm ikizkenar üçgenler için tepe- den tabana dik indirin ve yukarıdaki şekele dönüş- türün.

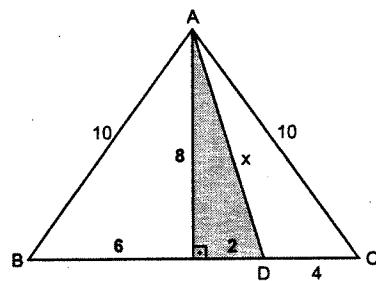
Örnek:



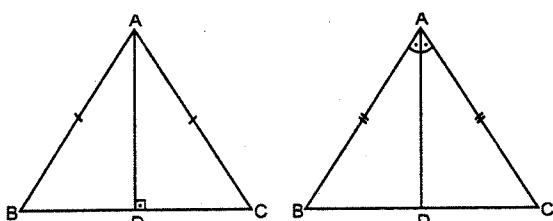
(gibi)

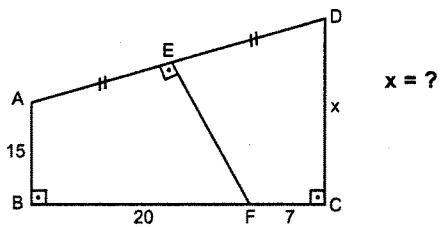


Çözüm:



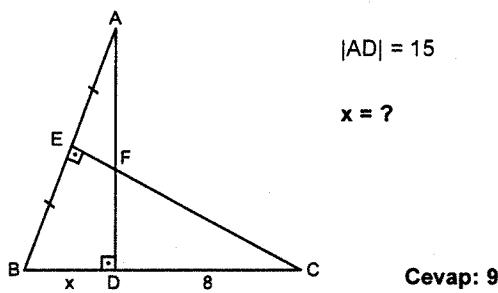
6-8-10 (Pisagor)



**109.**

$x = ?$

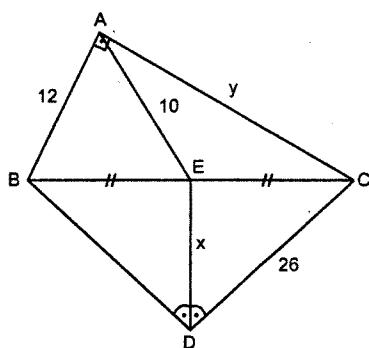
Cevap: 24

**110.**

$|AD| = 15$

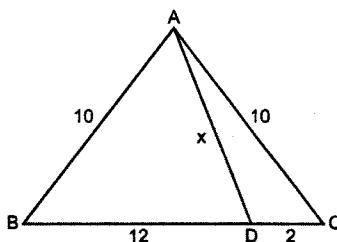
$x = ?$

Cevap: 9

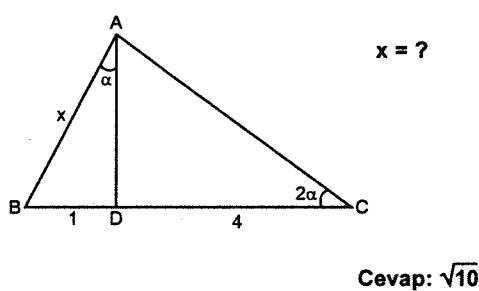
**113.**

$x - y = ?$

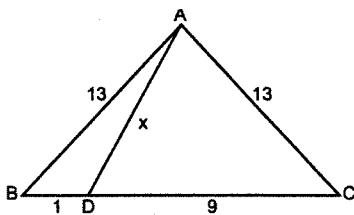
Cevap: 8

**114.**

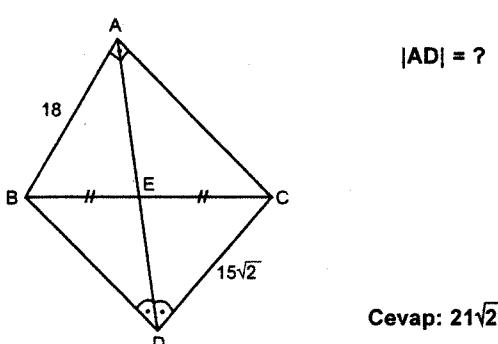
$x = ?$

Cevap:  $2\sqrt{19}$ **111.**

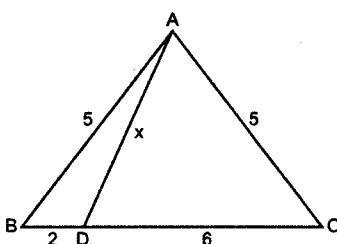
$x = ?$

Cevap:  $\sqrt{10}$ **115.**

$x = ?$

Cevap:  $4\sqrt{10}$ **112.**

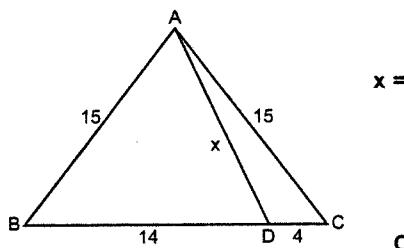
$|AD| = ?$

Cevap:  $21\sqrt{2}$ **116.**

$x = ?$

Cevap:  $\sqrt{13}$

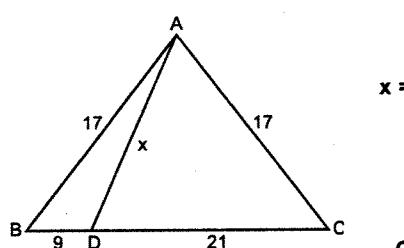
117.



$x = ?$

Cevap: 13

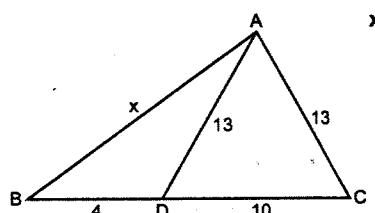
118.



$x = ?$

Cevap: 10

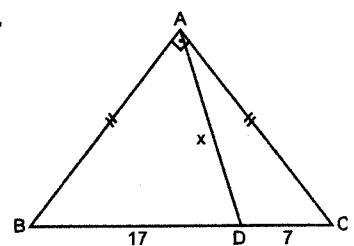
119.



$x = ?$

Cevap: 15

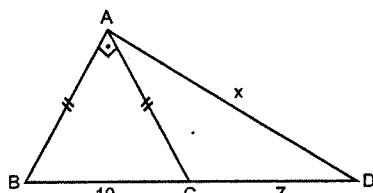
120.



$x = ?$

Cevap: 13

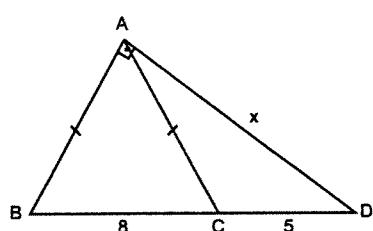
121.



$x = ?$

Cevap: 13

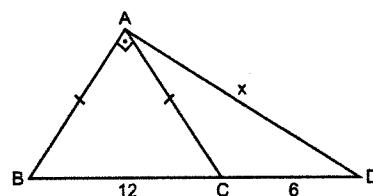
122.



$x = ?$

Cevap:  $3\sqrt{13}$ 

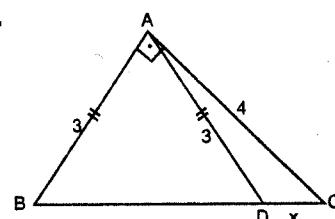
123.



$x = ?$

Cevap:  $6\sqrt{5}$ 

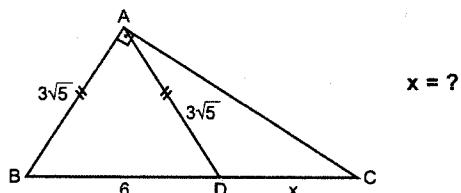
124.



$x = ?$

Cevap: 1,4

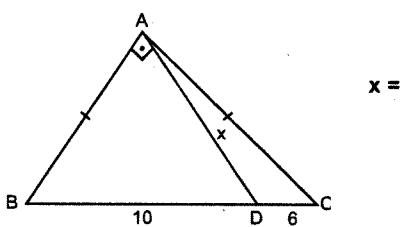
125.



$x = ?$

Cevap: 9

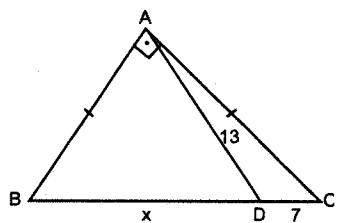
126.



$x = ?$

Cevap:  $2\sqrt{5}$ 

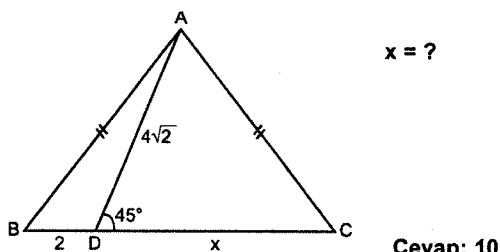
127.



$x = ?$

Cevap: 17

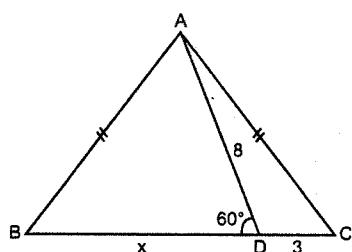
128.



$x = ?$

Cevap: 10

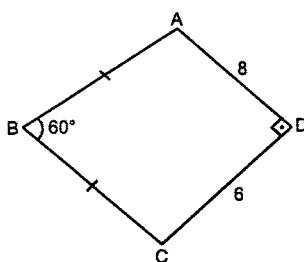
129.



$x = ?$

Cevap: 11

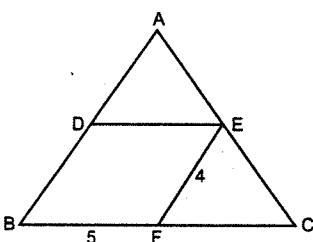
130.



Çevre(ABCD)

Cevap: 34

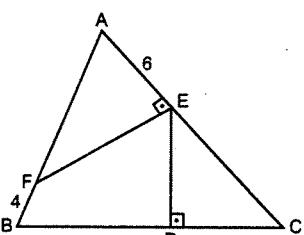
131.

ADE ve FEC  
eşkenar üçgen

$\hat{C}(ABC) = ?$

Cevap: 27

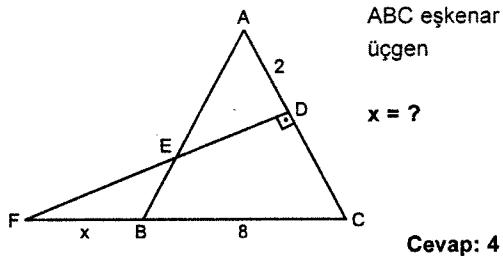
132.

ABC eşkenar  
Üçgen

$x = ?$

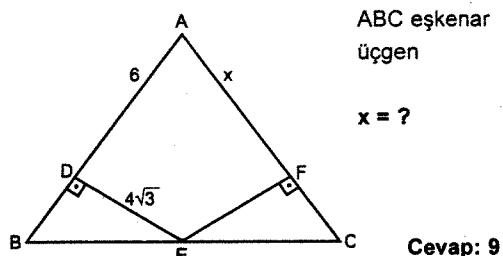
Cevap: 11

133.



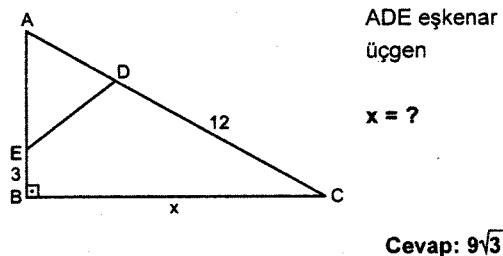
Cevap: 4

134.

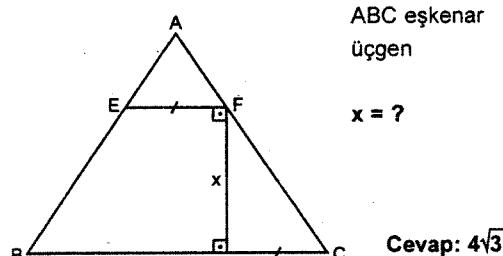


Cevap: 9

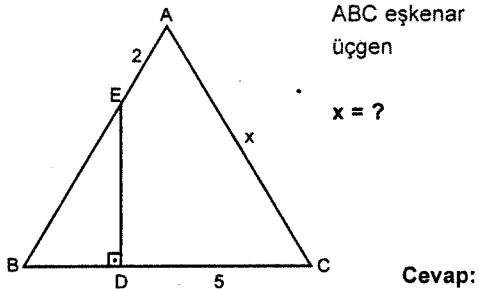
135.

Cevap:  $9\sqrt{3}$ 

136.

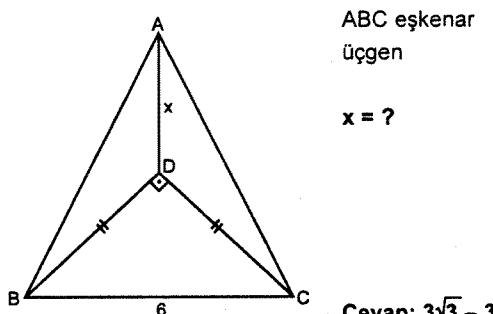
Cevap:  $4\sqrt{3}$ 

137.

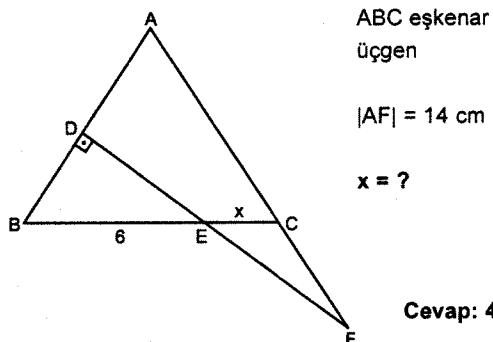


Cevap: 8

138.

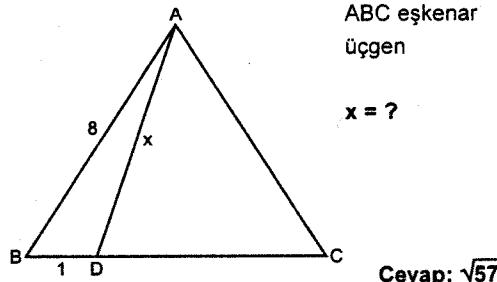
Cevap:  $3\sqrt{3} - 3$ 

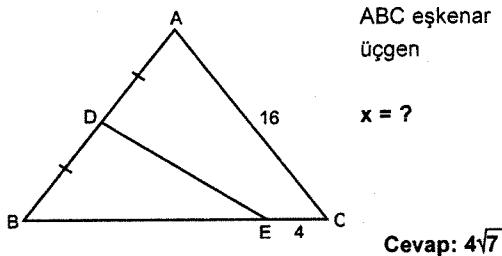
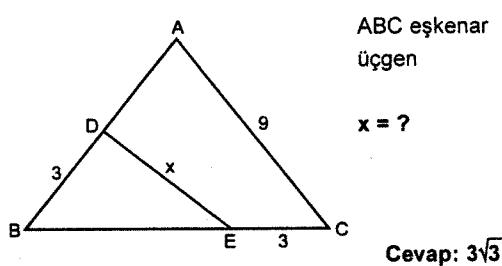
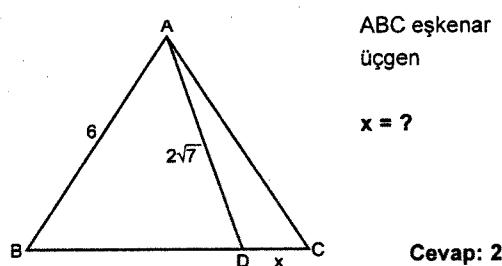
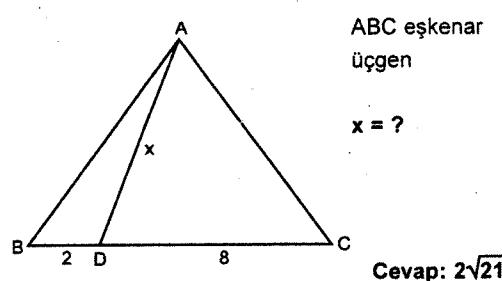
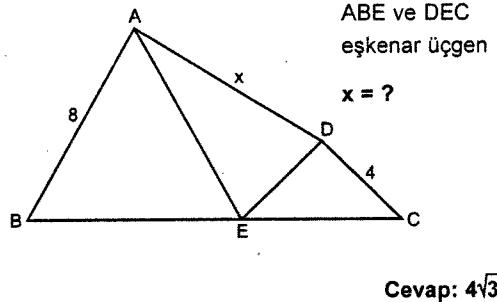
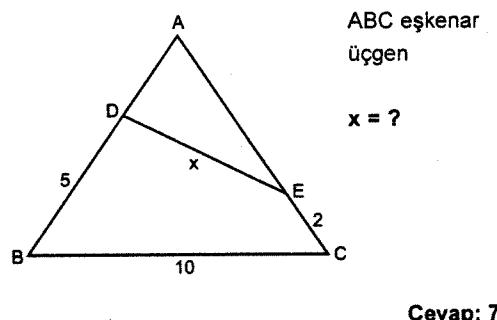
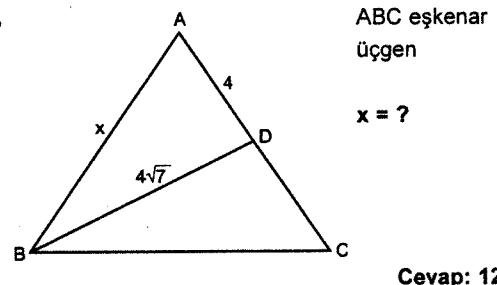
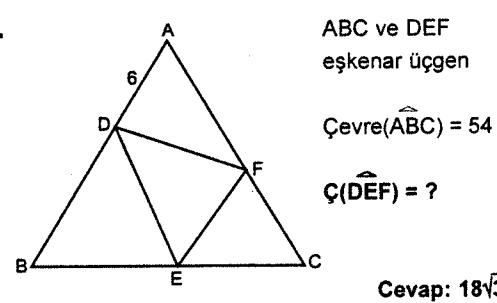
139.



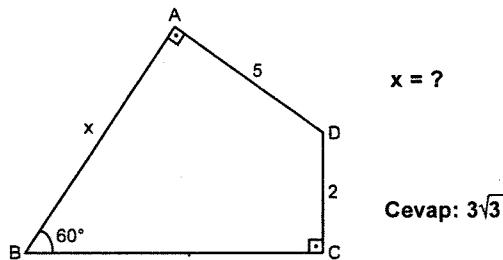
Cevap: 4

140.

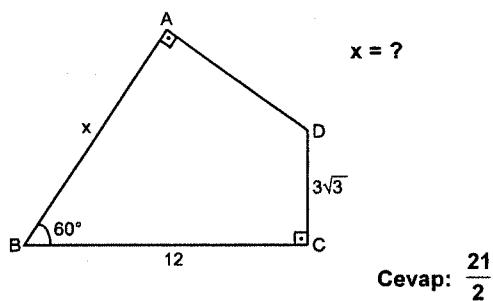
Cevap:  $\sqrt{57}$

**141.****142.****143.****144.****145.****146.****147.****148.**

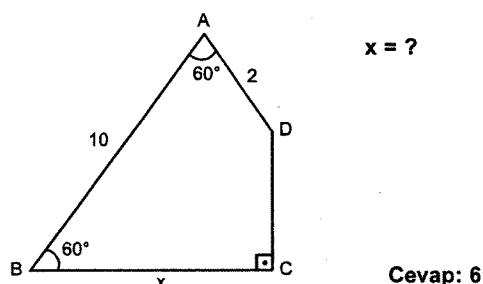
149.



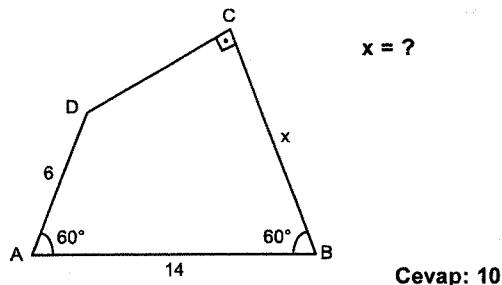
150.



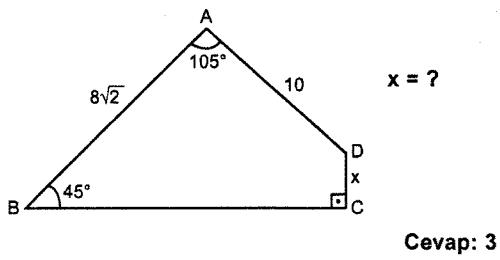
151.



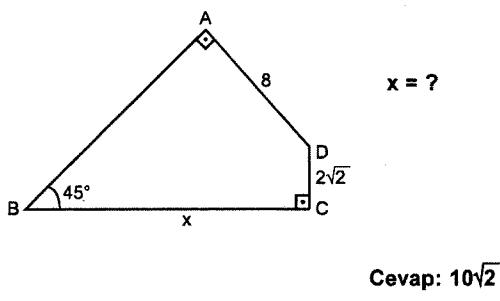
152.



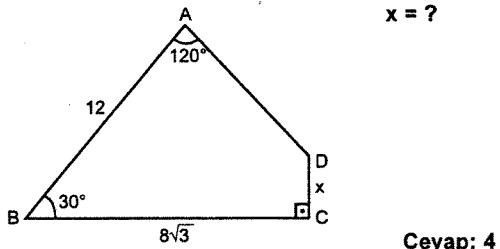
153.



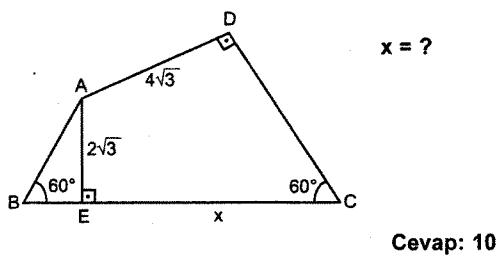
154.



155.

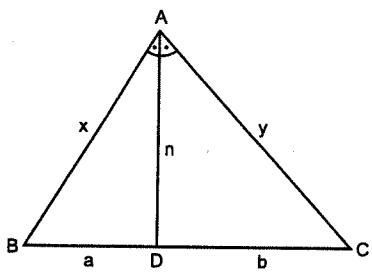


156.



## ÜÇGENDE AÇIORTAY ÖZELLİKLERİ

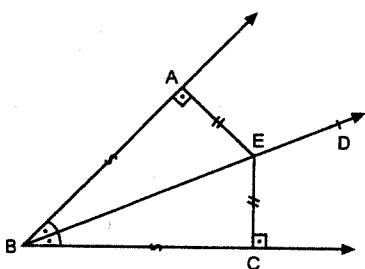
**İç Açıortay Özelliği:**



$$\frac{x}{y} = \frac{a}{b} \quad \text{veya} \quad \frac{x}{a} = \frac{y}{b}$$

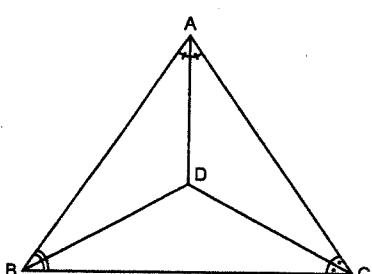
$$n^2 = x \cdot y - a \cdot b$$

- \* Açıortayın kollarına indirilen dikmeler birbirine eşittir.

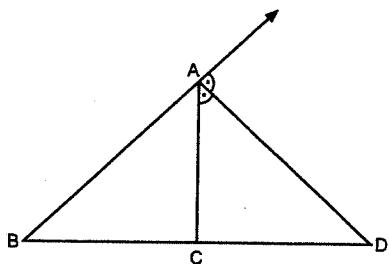


$$|AE| = |EC| \quad \text{ve} \quad |AB| = |BC|$$

- \* Açıortaylar bir noktada kesişir. Bu noktaya bu üçgenin iç teğet çemberinin merkezi denir. Bu üç iç açıortaydan herhangi ikisi var ise üçüncü açıortay da bu noktadan geçmek zorundadır.



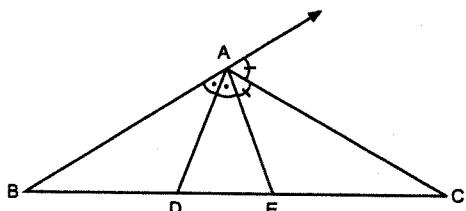
**\* Dış Açıortay Özelliği:**



[AD] : Dış açıortay

$$\frac{|AB|}{|BD|} = \frac{|AC|}{|CD|}$$

\*



Yukarıdaki şekil için:

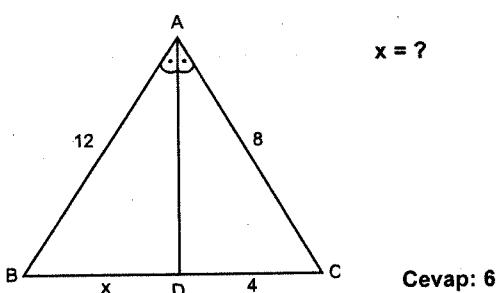
a)  $m(\widehat{DAC}) = 90^\circ$

b)  $\frac{|AB|}{|AE|} = \frac{|BD|}{|DE|}$  (İç açıortay özelliği)

c)  $\frac{|AB|}{|BC|} = \frac{|AE|}{|EC|}$  (Dış açıortay özelliği)

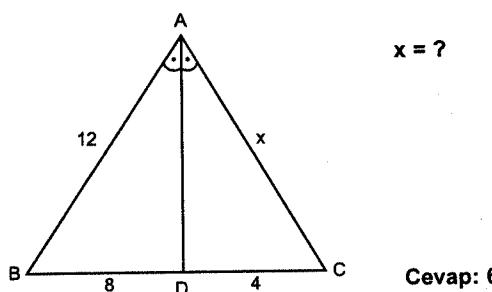
uygulanır.

1.



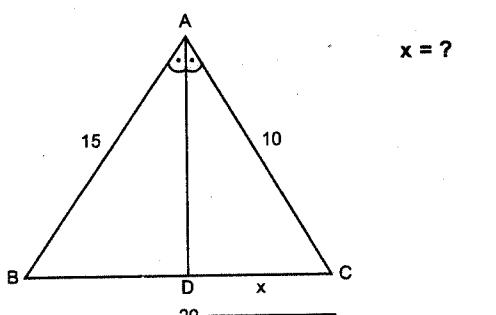
Cevap: 6

2.



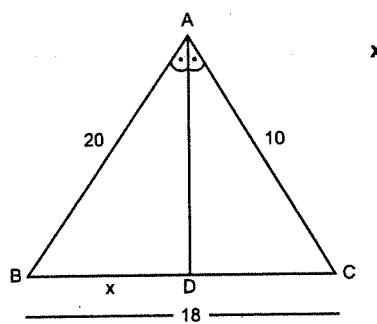
Cevap: 6

3.



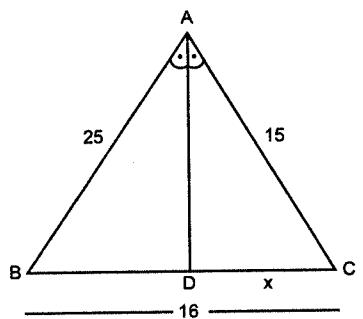
Cevap: 8

4.



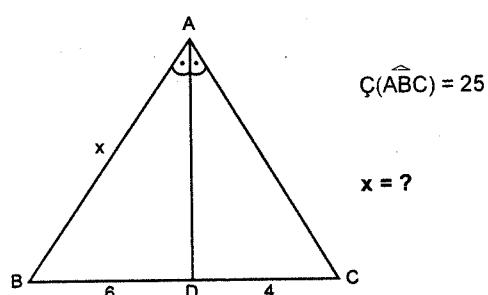
Cevap: 12

5.



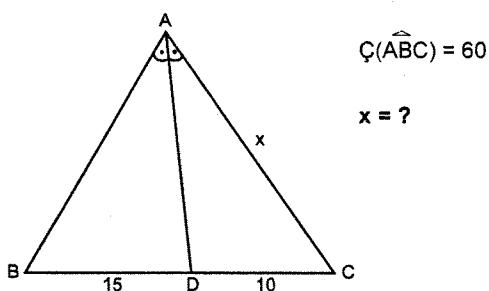
Cevap: 6

6.



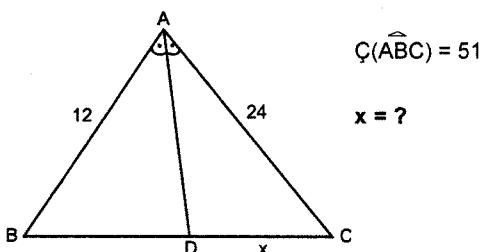
Cevap: 9

7.



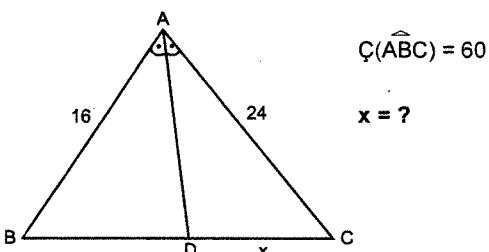
Cevap: 14

8.



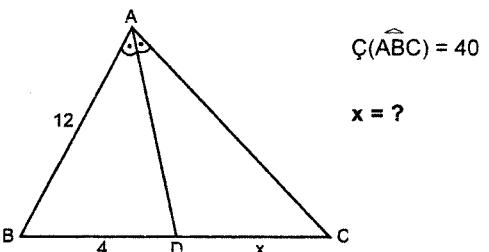
Cevap: 10

9.



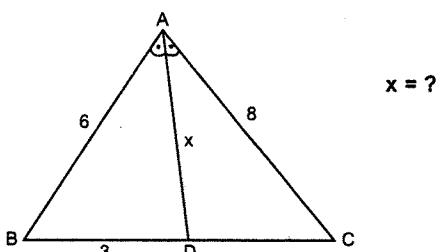
Cevap: 12

10.



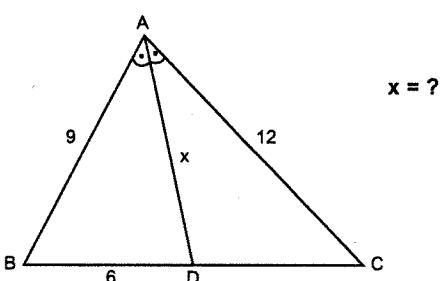
Cevap: 6

11.

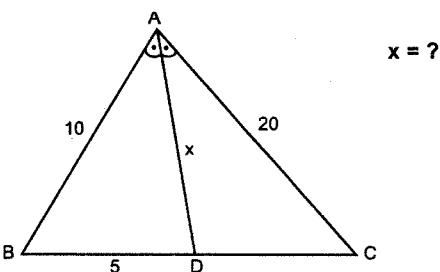


Cevap: 6

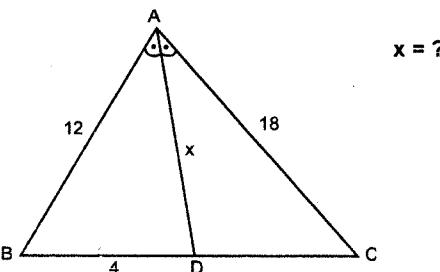
12.

Cevap:  $2\sqrt{15}$ 

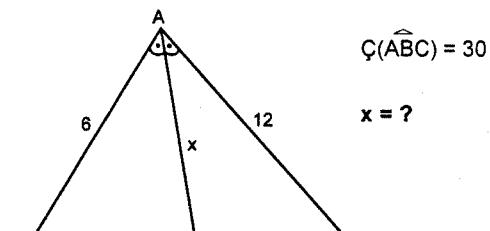
13.

Cevap:  $5\sqrt{6}$ 

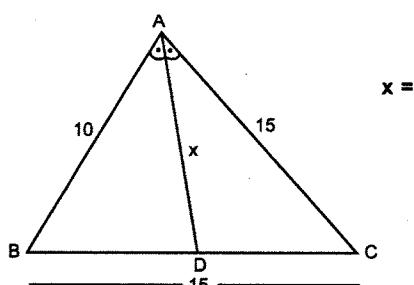
14.

Cevap:  $8\sqrt{3}$

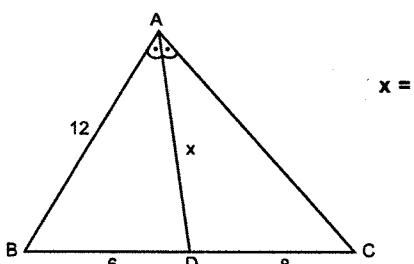
15.

Cevap:  $2\sqrt{10}$ 

16.

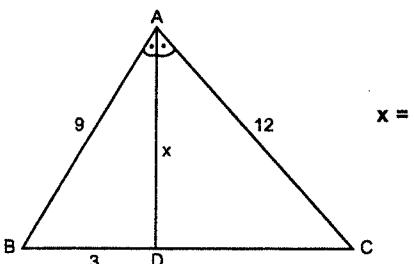
Cevap:  $4\sqrt{10}$ 

17.

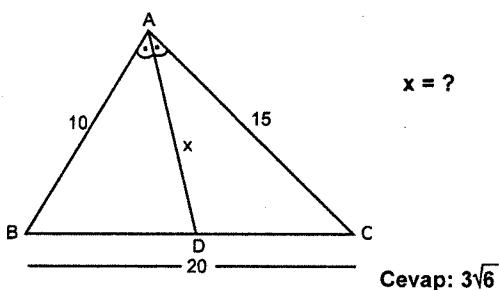


Cevap: 12

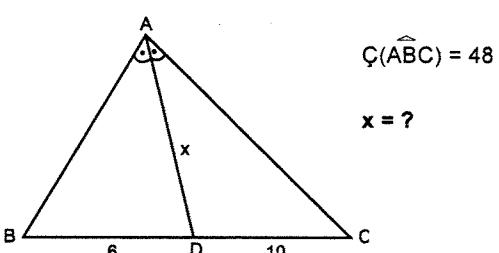
18.

Cevap:  $4\sqrt{6}$ 

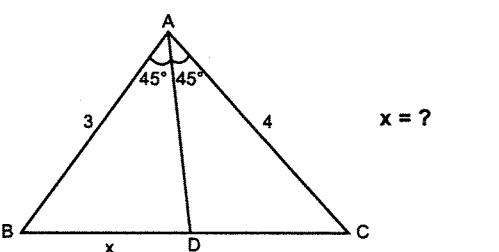
19.

Cevap:  $3\sqrt{6}$ 

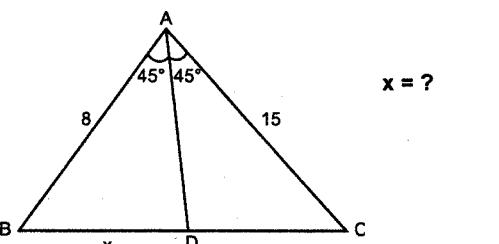
20.

Cevap:  $6\sqrt{5}$ 

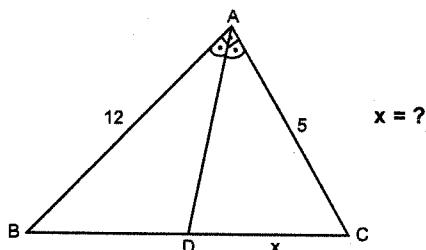
21.

Cevap:  $\frac{15}{7}$ 

22.

Cevap:  $\frac{136}{23}$

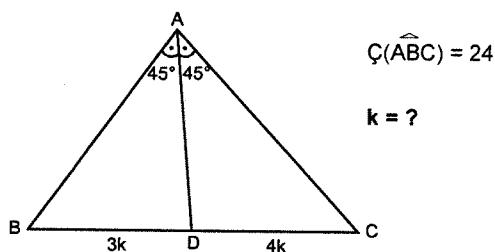
23.



$x = ?$

$\text{Cevap: } \frac{65}{17}$

24.

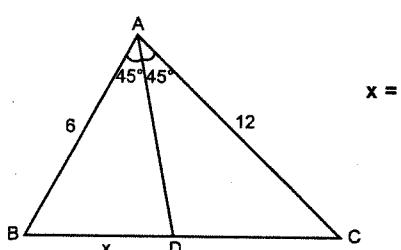


$\hat{C}(ABC) = 24$

$k = ?$

$\text{Cevap: } \frac{10}{7}$

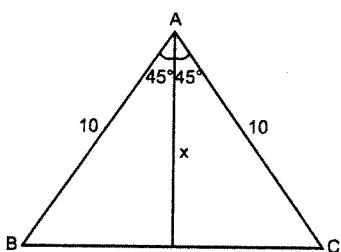
25.



$x = ?$

$\text{Cevap: } 2\sqrt{5}$

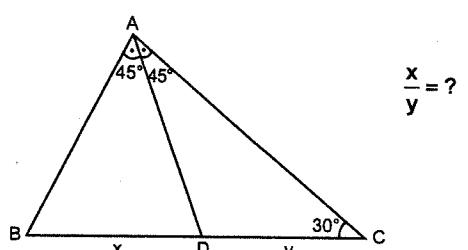
26.



$x = ?$

$\text{Cevap: } 5\sqrt{2}$

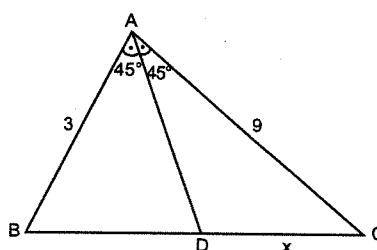
27.



$\frac{x}{y} = ?$

$\text{Cevap: } \frac{1}{\sqrt{3}}$

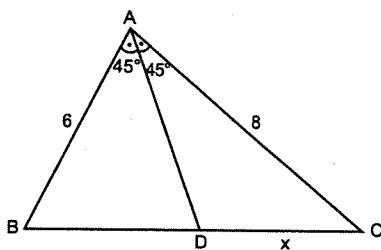
28.



$x = ?$

$\text{Cevap: } \frac{9\sqrt{10}}{4}$

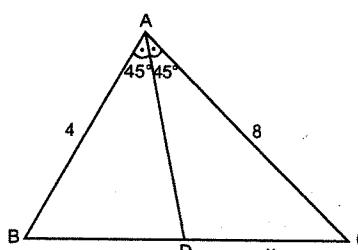
29.



$x = ?$

$\text{Cevap: } \frac{40}{7}$

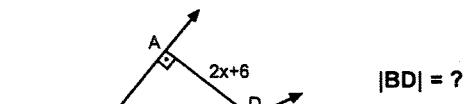
30.



$x = ?$

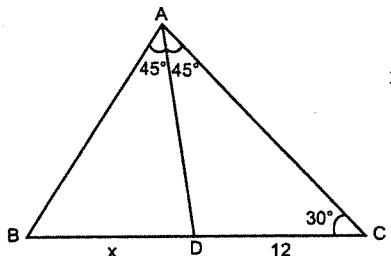
$\text{Cevap: } \frac{8\sqrt{5}}{3}$

31.



$|BD| = ?$

35.

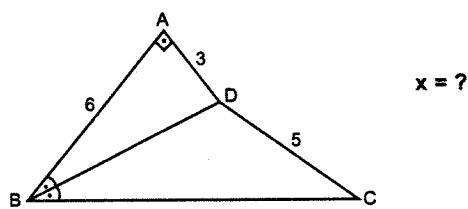


$x = ?$

Cevap: 25

Cevap:  $4\sqrt{3}$ 

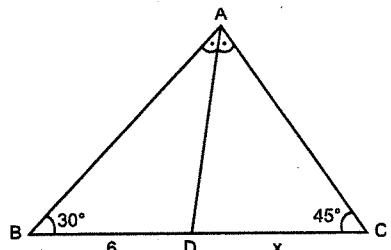
32.



$x = ?$

Cevap: 10

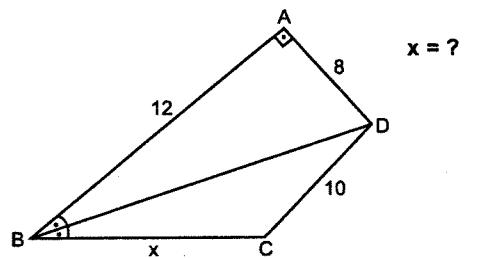
36.



$x = ?$

Cevap:  $3\sqrt{2}$ 

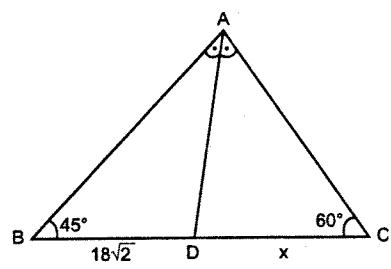
33.



$x = ?$

Cevap: 6

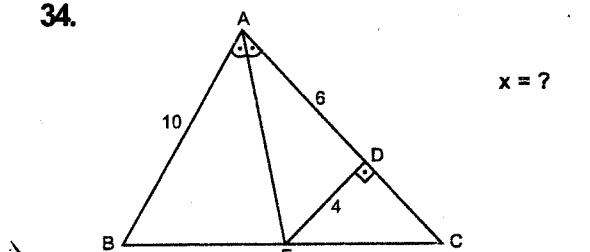
37.



$x = ?$

Cevap:  $12\sqrt{3}$ 

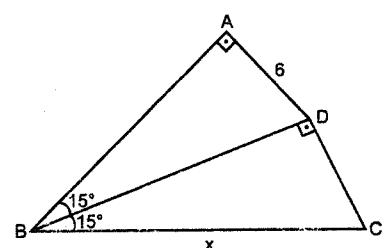
34.



$x = ?$

Cevap:  $4\sqrt{2}$ 

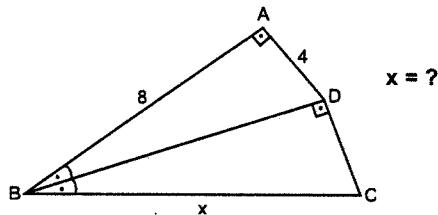
38.



$x = ?$

Cevap: 24

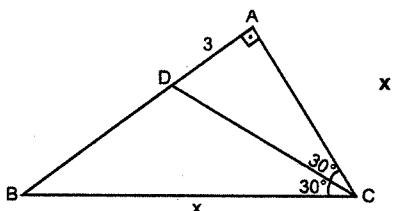
39.



$x = ?$

Cevap: 10

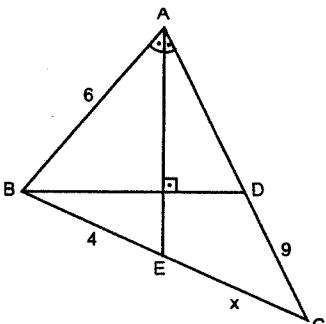
40.



$x = ?$

Cevap:  $6\sqrt{3}$ 

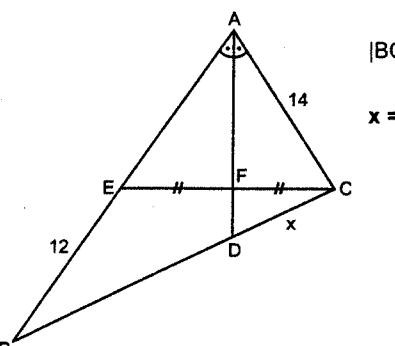
41.



$x = ?$

Cevap: 10

42.

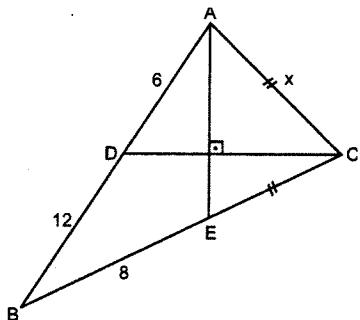


$|BC| = 20$

$x = ?$

Cevap: 7

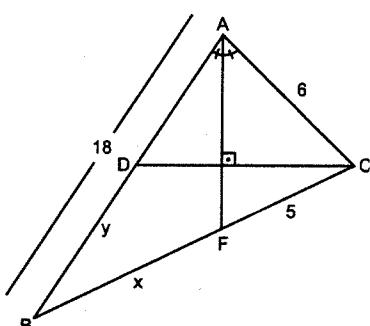
43.



$x = ?$

Cevap: 8

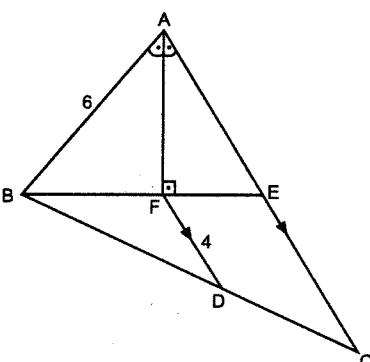
44.



$x - y = ?$

Cevap: 3

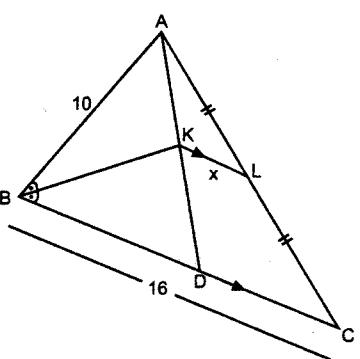
45.



$|AC| = ?$

Cevap: 14

46.



$x = ?$

Cevap: 3

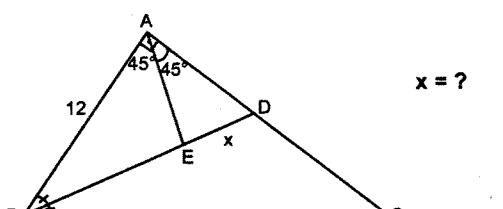
47.



$$|EK| = ?$$

Cevap: 7

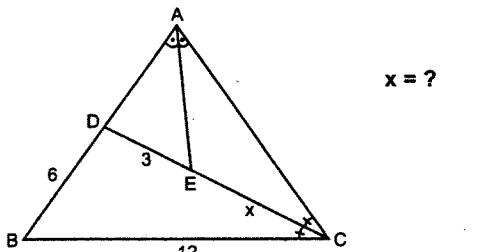
48.



$$x = ?$$

Cevap:  $2\sqrt{5}$ 

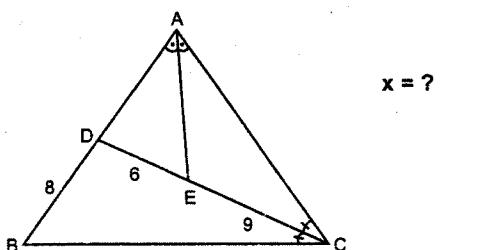
49.



$$x = ?$$

Cevap: 6

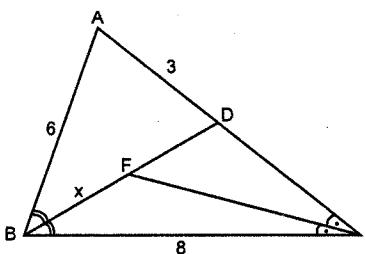
50.



$$x = ?$$

Cevap: 12

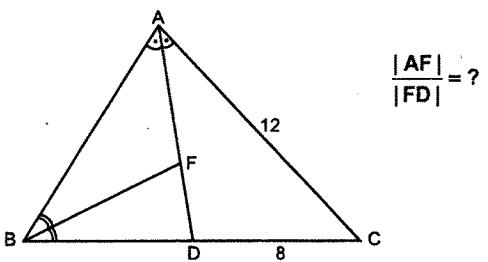
51.



$$x = ?$$

Cevap: 4

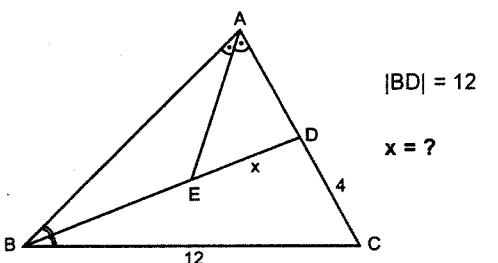
52.



$$\frac{|AF|}{|FD|} = ?$$

Cevap:  $\frac{3}{2}$ 

53.

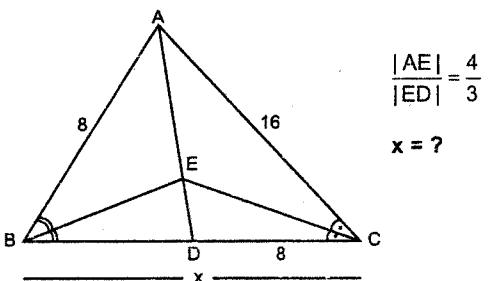


$$|BD| = 12$$

$$x = ?$$

Cevap: 3

54.

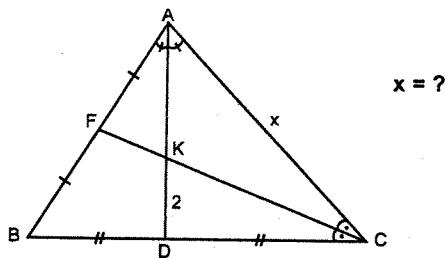


$$\frac{|AE|}{|ED|} = \frac{4}{3}$$

$$x = ?$$

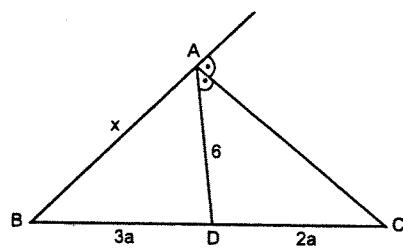
Cevap: 18

55.



$x = ?$

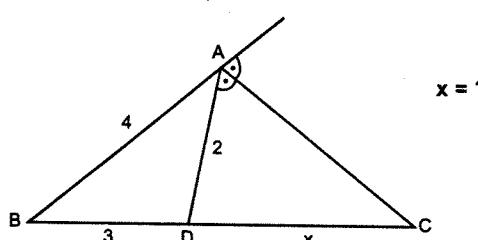
59.



$x = ?$

Cevap: 15

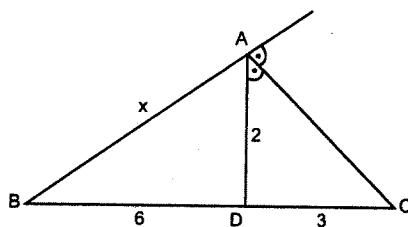
56.



$x = ?$

Cevap: 3

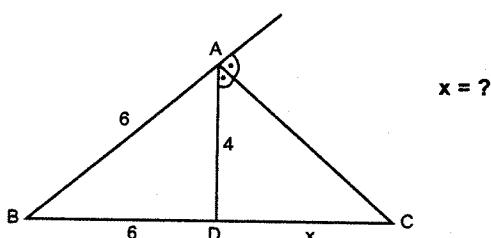
60.



$x = ?$

Cevap: 6

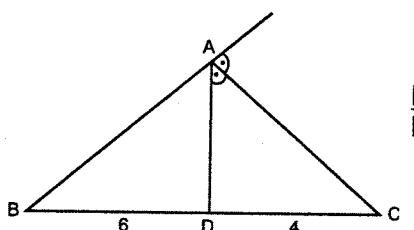
57.



$x = ?$

Cevap: 12

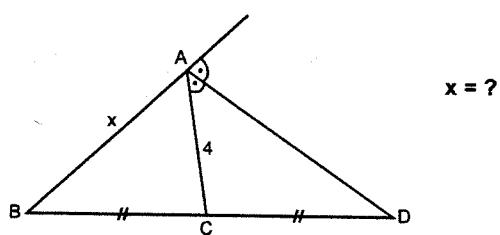
61.



$\frac{|AB|}{|AD|} = ?$

Cevap:  $\frac{5}{2}$ 

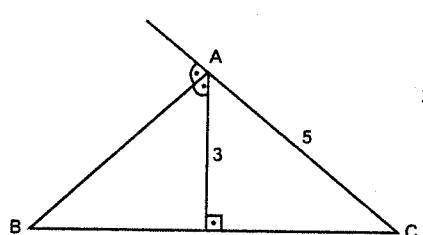
58.



$x = ?$

Cevap: 8

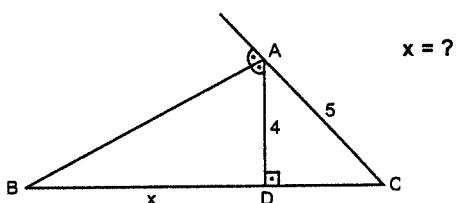
62.



$x = ?$

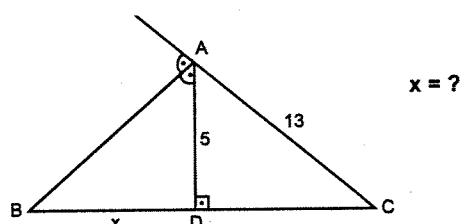
Cevap: 6

63.

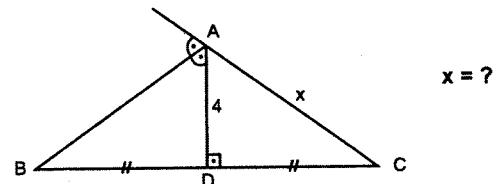


Cevap: 12

64.

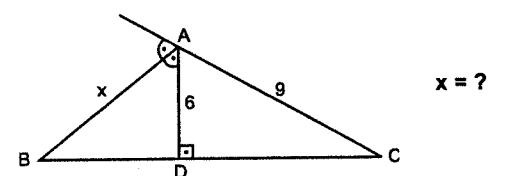
Cevap:  $\frac{15}{2}$ 

65.

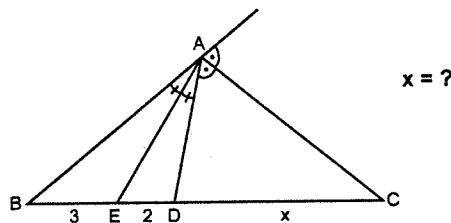


Cevap: 8

66.

Cevap:  $6\sqrt{6}$ 

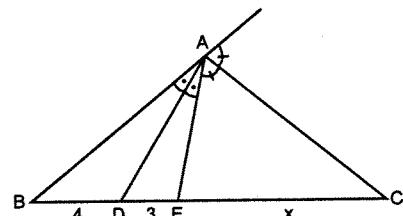
67.



x = ?

Cevap: 10

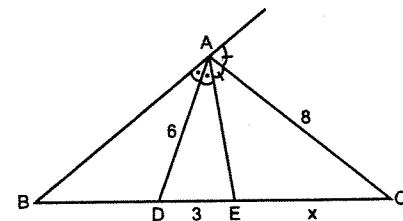
68.



x = ?

Cevap: 21

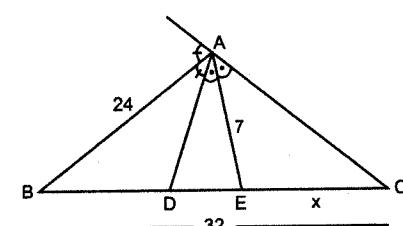
69.



x = ?

Cevap: 7

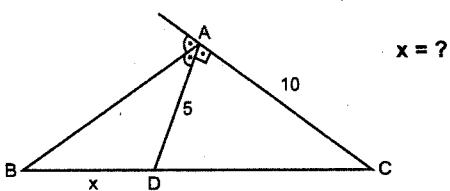
70.



x = ?

Cevap: 7

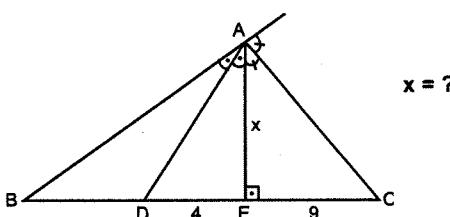
71.



$x = ?$

Cevap:  $5\sqrt{5}$ 

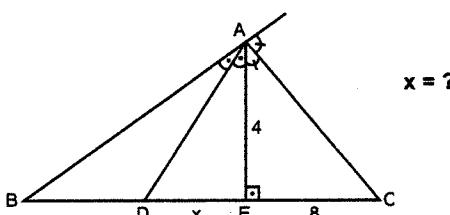
72.



$x = ?$

Cevap: 6

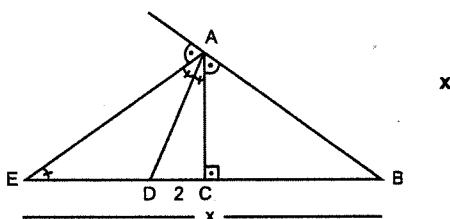
73.



$x = ?$

Cevap: 2

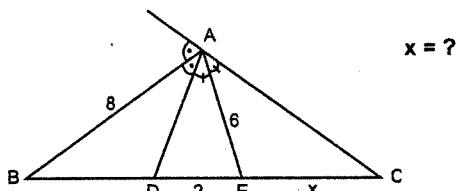
74.



$x = ?$

Cevap: 12

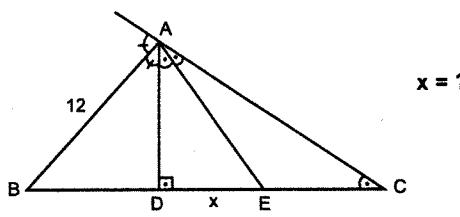
75.



$x = ?$

Cevap:  $\frac{10}{3}$ 

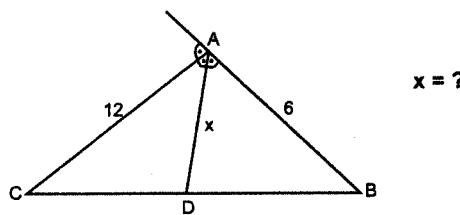
76.



$x = ?$

Cevap:  $2\sqrt{3}$ 

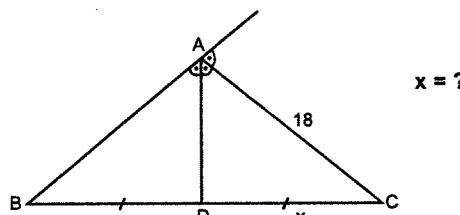
77.



$x = ?$

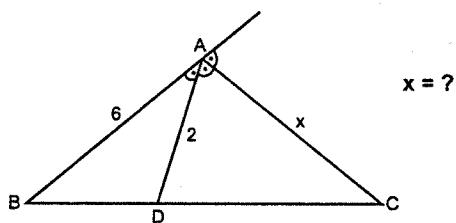
Cevap: 4

78.

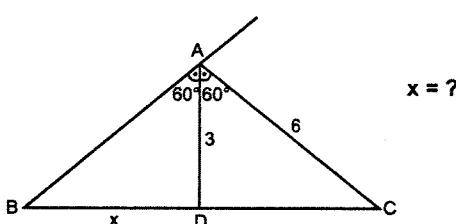
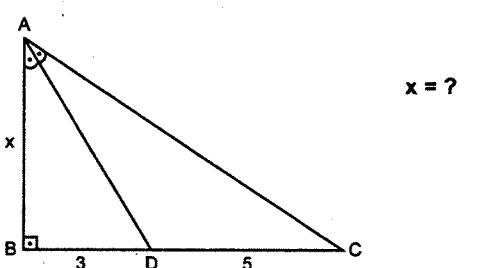


$x = ?$

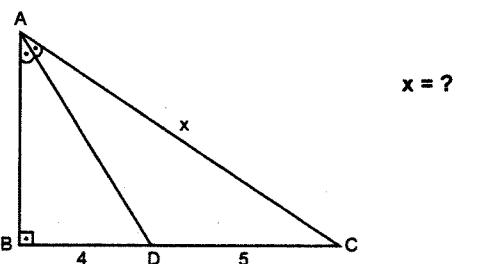
Cevap:  $9\sqrt{3}$

**79.**

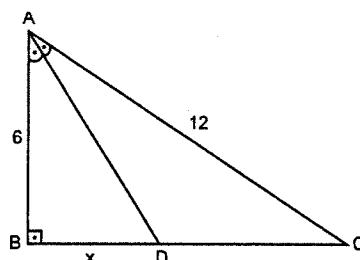
Cevap: 3

**80.**Cevap:  $3\sqrt{3}$ **81.**

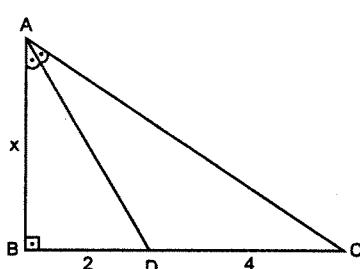
Cevap: 6

**82.**

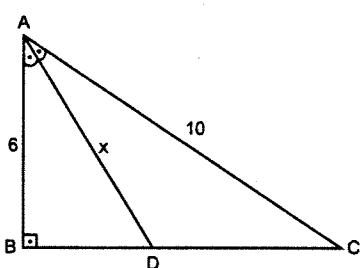
Cevap: 15

**83.**

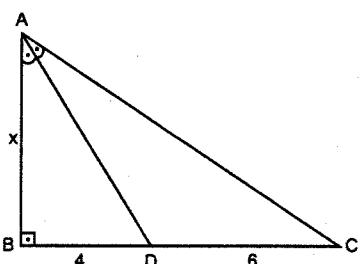
x = ?

Cevap:  $2\sqrt{3}$ **84.**

x = ?

Cevap:  $2\sqrt{3}$ **85.**

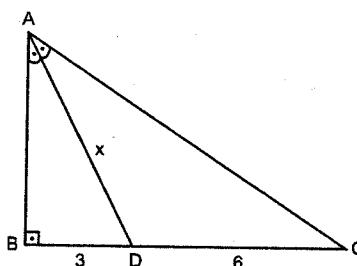
x = ?

Cevap:  $3\sqrt{5}$ **86.**

x = ?

Cevap:  $4\sqrt{5}$

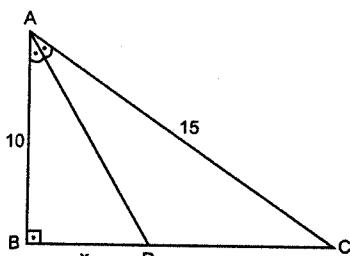
87.



$x = ?$

Cevap: 6

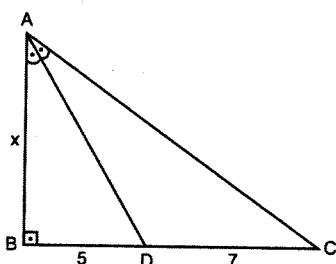
88.



$x = ?$

Cevap:  $2\sqrt{5}$ 

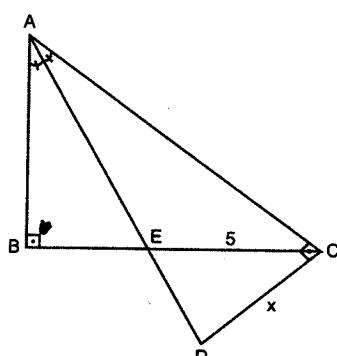
89.



$x = ?$

Cevap:  $5\sqrt{6}$ 

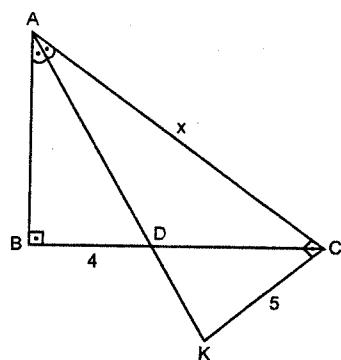
90.



$x = ?$

Cevap: 5

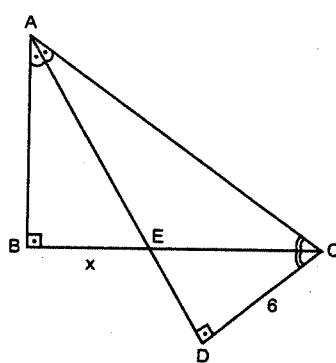
91.



$x = ?$

Cevap: 15

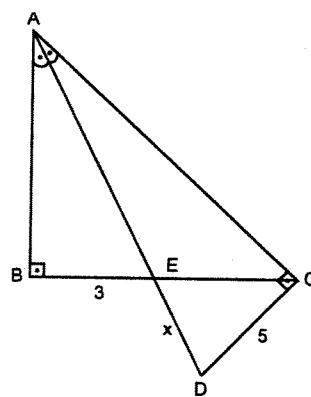
92.



$x = ?$

Cevap:  $2\sqrt{3}$ 

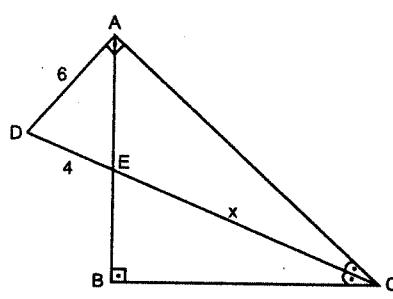
93.



$x = ?$

Cevap:  $2\sqrt{5}$ 

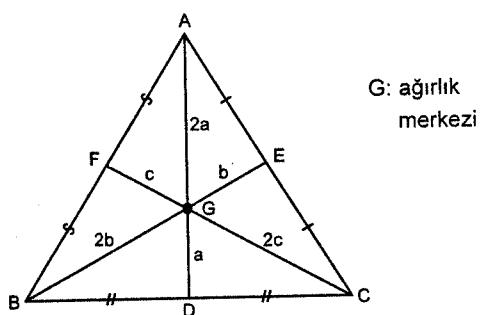
94.



$x = ?$

Cevap: 14

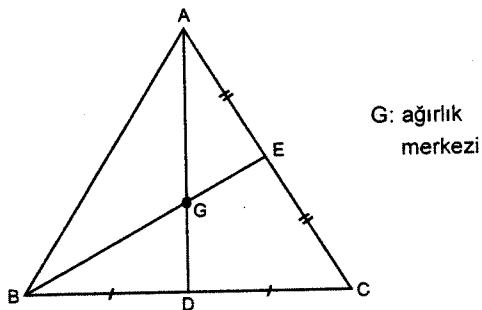
## ÜÇGENDE KENARORTAY ÖZELLİKLERİ



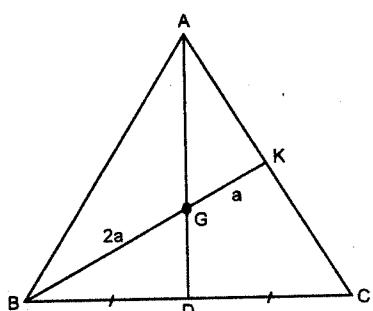
Üçgende kenarortaylar bir noktada kesişir. Bu noktaya bu üçgenin ağırlık merkezi denir. Ağırlık merkezi tabana 1 br, köşeye 2 br uzaklıktadır.

**Ne zaman ağırlık merkezi olduğu anlaşılır?**

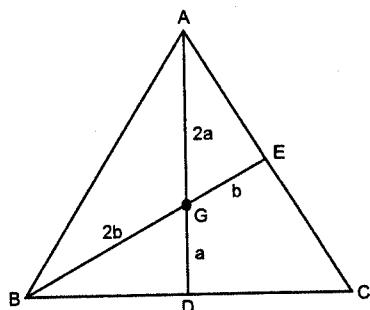
İki kenarortay verildiği zaman



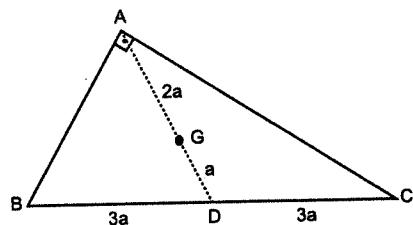
Bir kenarortay ve bir de bir'e iki oranı verilirse G ağırlık merkezi olduğu anlaşılır.



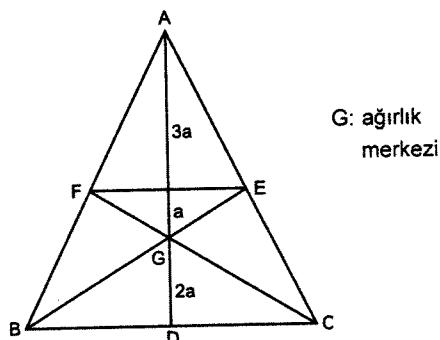
2 tane bir'e iki oranı verilirse G ağırlık merkezi olduğu anlaşılır.



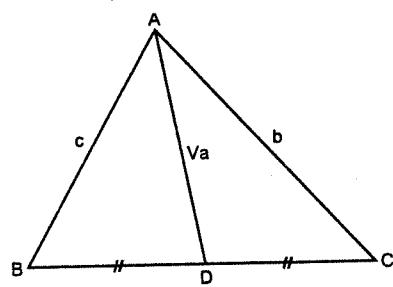
- \* Dik üçgende ağırlık merkezi verilmişse mutlaka muhteşem üçlü oluşturur.



- \* Ankara'nın telefon kodu (312) kuralı

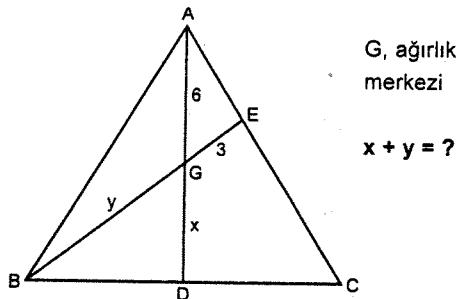


**Kenarortay Teoremi**



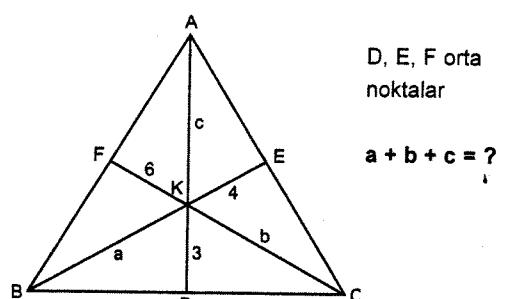
$$2.Va^2 = b^2 + c^2 - \frac{a^2}{2}$$

1.



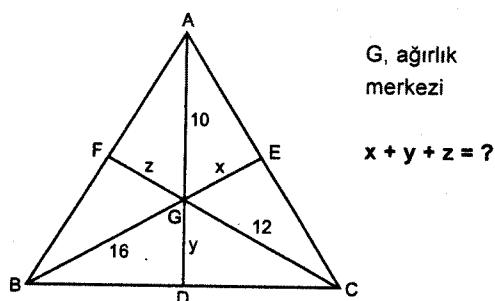
Cevap: 9

4.



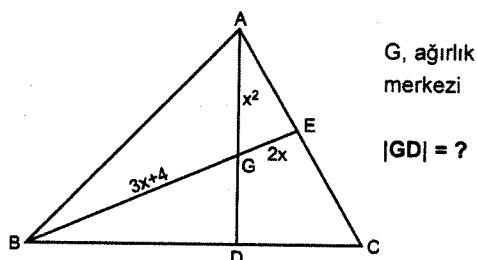
Cevap: 26

2.



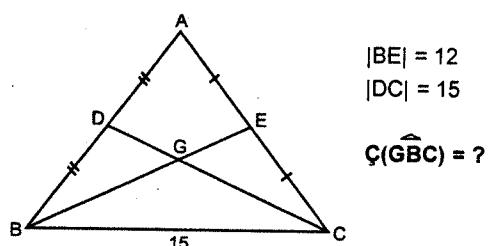
Cevap: 19

5.



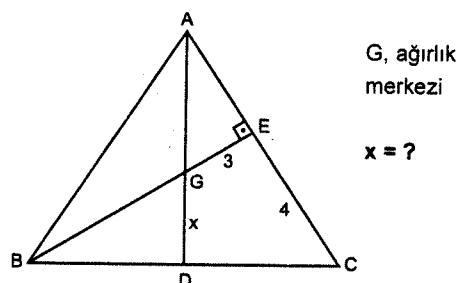
Cevap: 8

3.

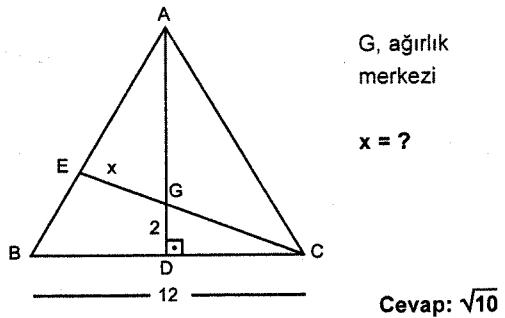


Cevap: 33

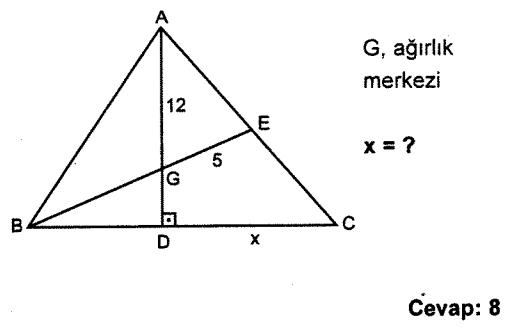
6.

Cevap:  $\frac{5}{2}$

7.

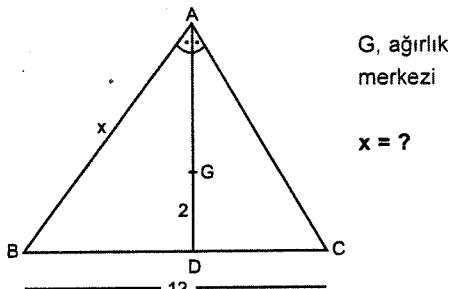
Cevap:  $\sqrt{10}$ 

8.

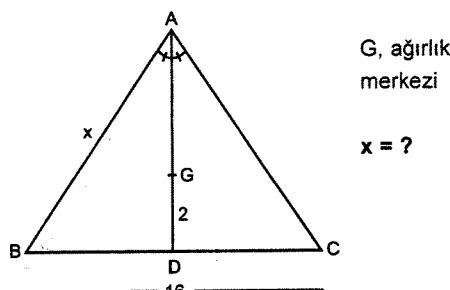


Cevap: 8

11.

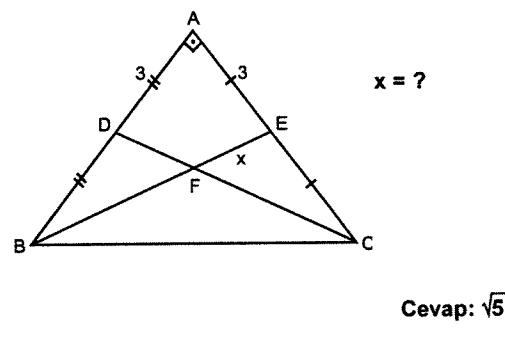
Cevap:  $6\sqrt{2}$ 

12.

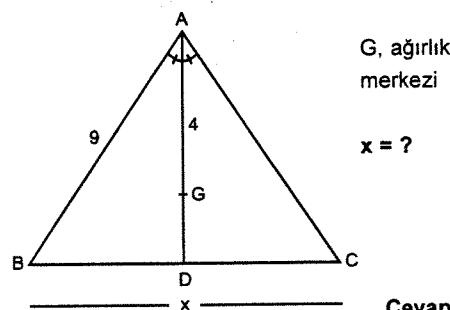


Cevap: 10

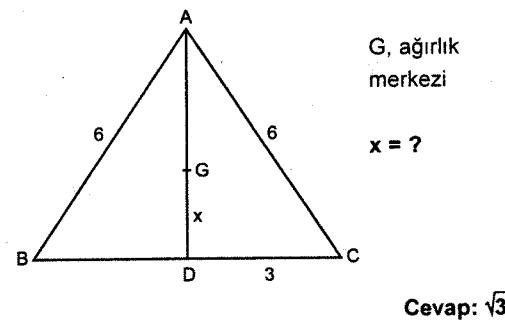
9.

Cevap:  $\sqrt{15}$ 

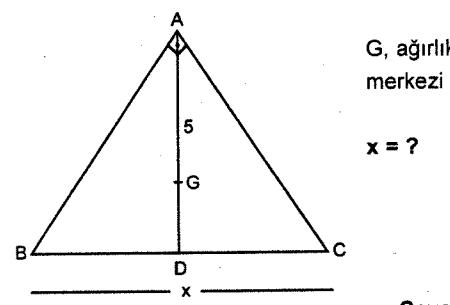
13.

Cevap:  $6\sqrt{5}$ 

10.

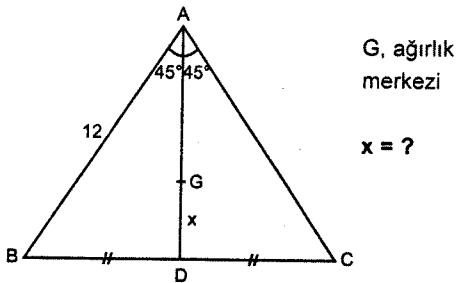
Cevap:  $\sqrt{3}$ 

14.

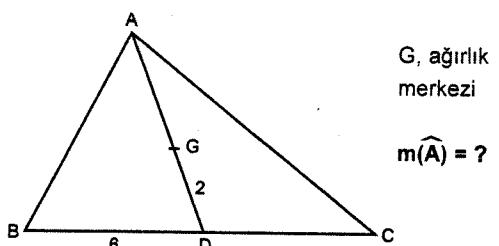


Cevap: 15

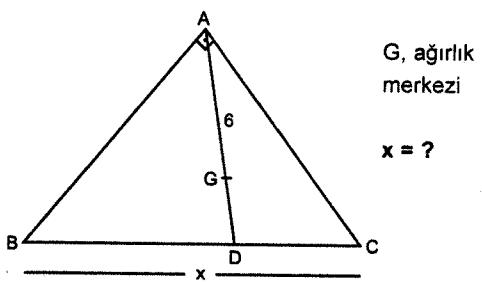
15.

Cevap:  $2\sqrt{2}$ 

19.

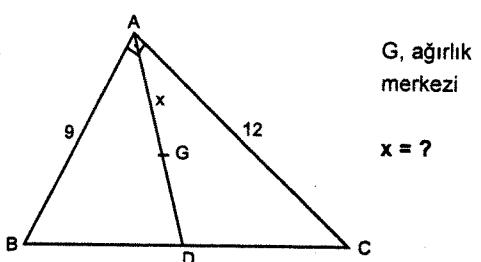
Cevap:  $90^\circ$ 

16.



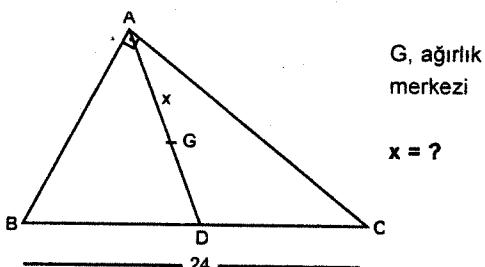
Cevap: 18

20.



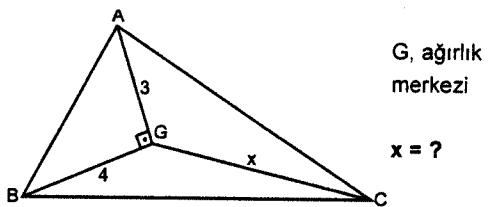
Cevap: 5

17.



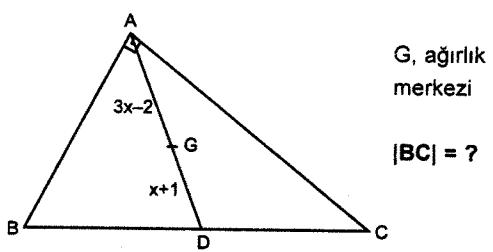
Cevap: 8

21.



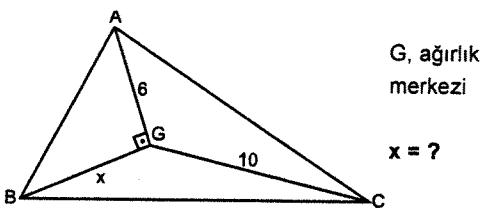
Cevap: 5

18.



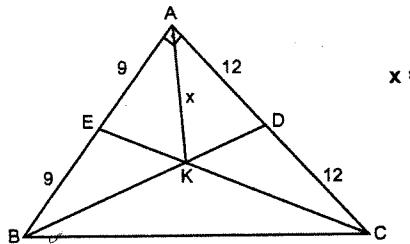
Cevap: 30

22.



Cevap: 8

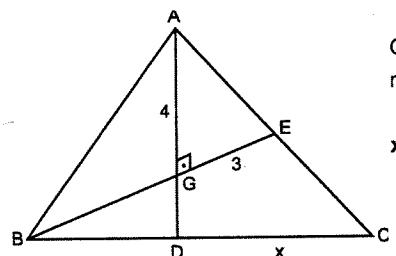
23.



$x = ?$

Cevap: 10

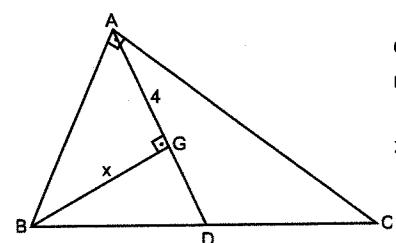
24.

G, ağırlık  
merkezi

$x = ?$

Cevap:  $2\sqrt{10}$ 

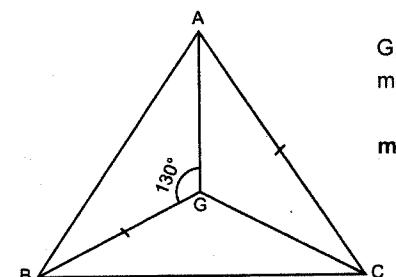
25.

G, ağırlık  
merkezi

$x = ?$

Cevap:  $4\sqrt{2}$ 

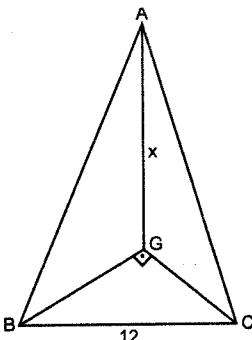
26.

G, ağırlık  
merkezi

$m(\widehat{BGC}) = ?$

Cevap:  $140^\circ$ 

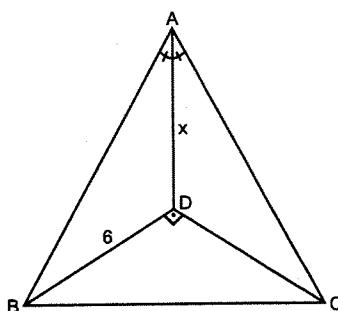
27.

G, ağırlık  
merkezi

$x = ?$

Cevap: 12

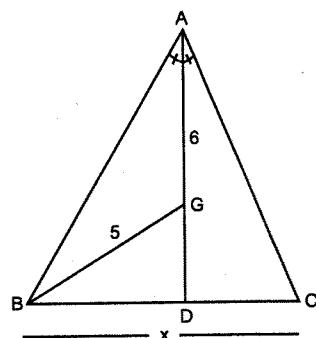
28.

D, ağırlık  
merkezi

$x = ?$

Cevap:  $6\sqrt{2}$ 

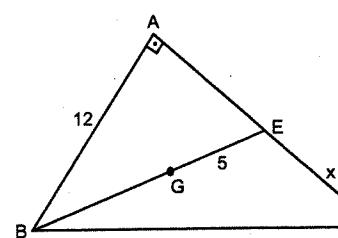
29.

G, ağırlık  
merkezi

$x = ?$

Cevap: 8

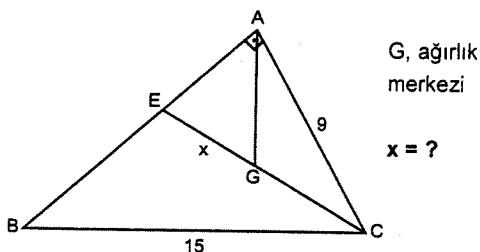
30.

G, ağırlık  
merkezi

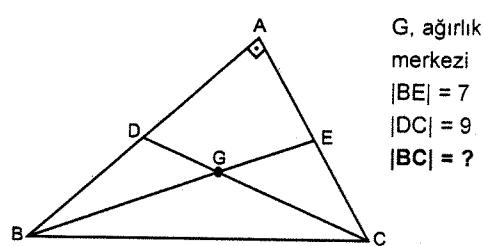
$x = ?$

Cevap: 9

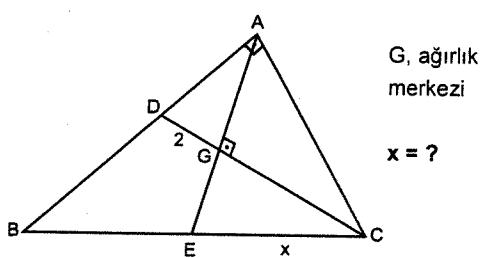
31.



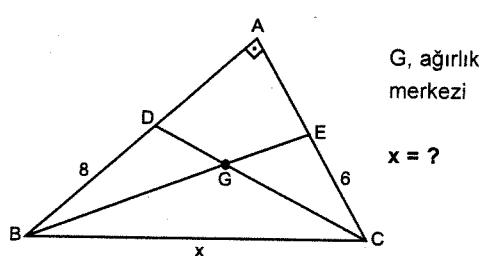
35.

Cevap:  $\sqrt{13}$ Cevap:  $2\sqrt{26}$ 

32.

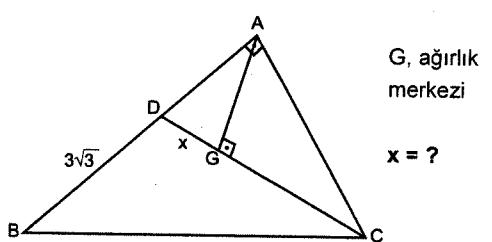
Cevap:  $3\sqrt{2}$ 

36.



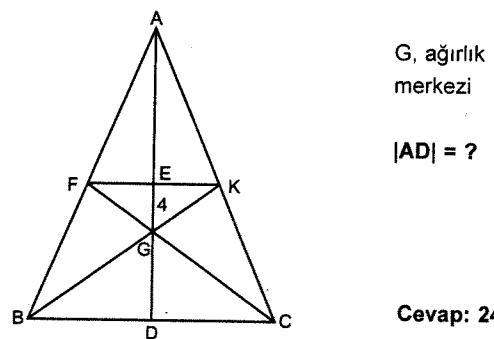
Cevap: 20

33.



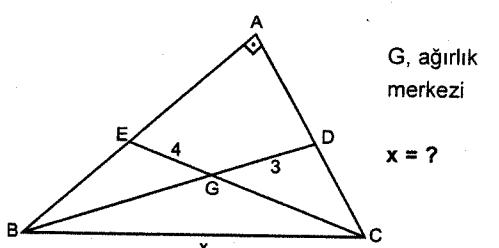
Cevap: 3

37.

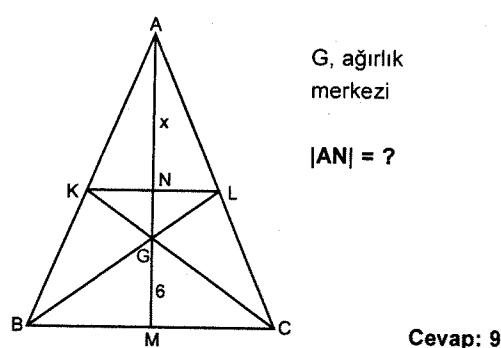


Cevap: 24

34.

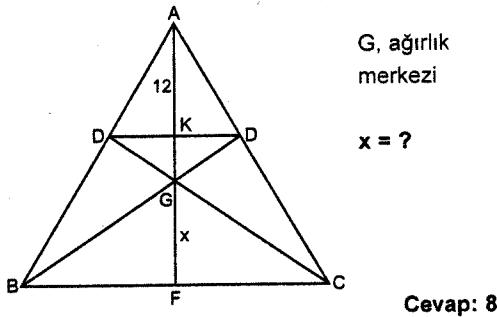
Cevap:  $6\sqrt{5}$ 

38.



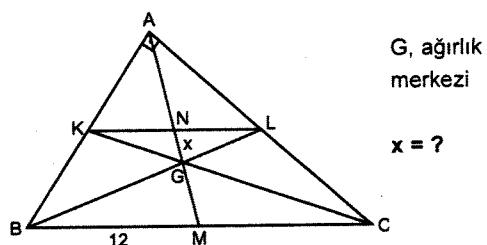
Cevap: 9

49.



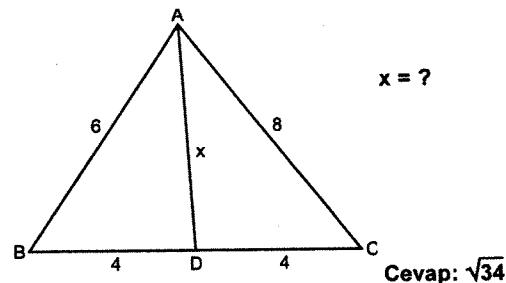
Cevap: 8

40.

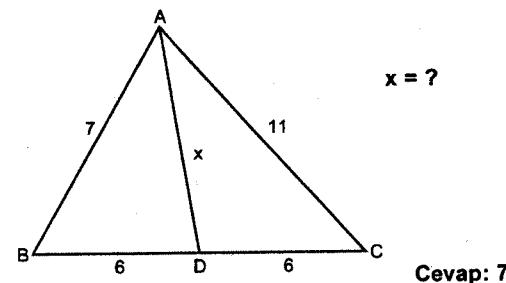


Cevap: 2

41.

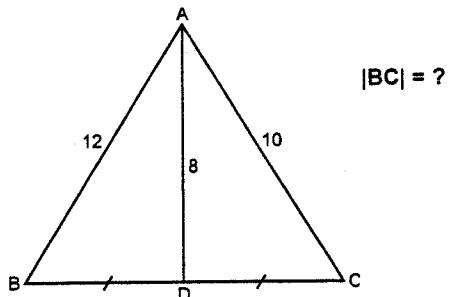
Cevap:  $\sqrt{34}$ 

42.

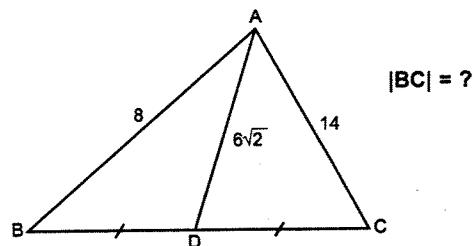


Cevap: 7

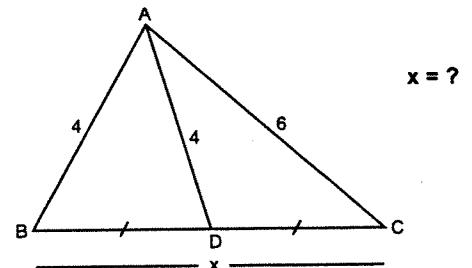
43.

Cevap:  $2\sqrt{58}$ 

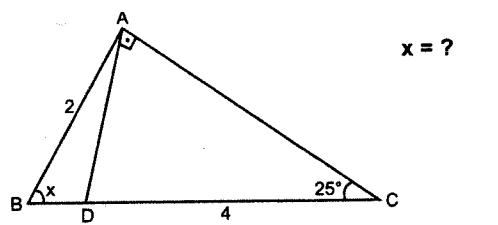
44.

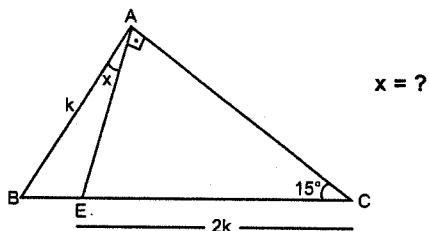
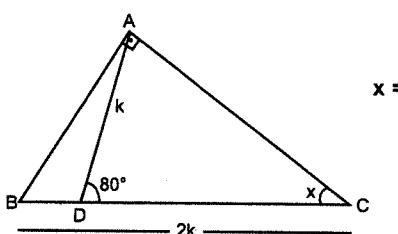
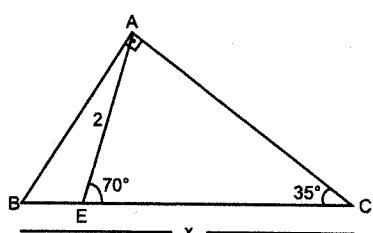
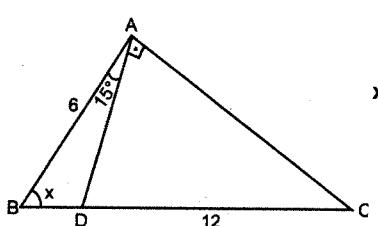
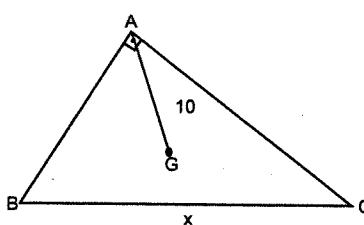
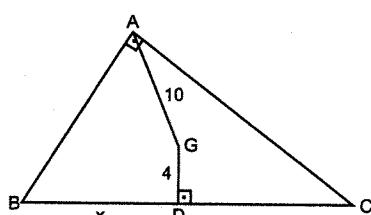
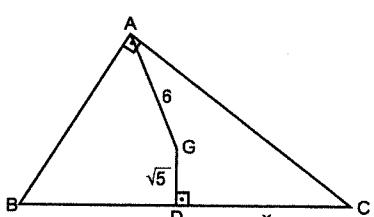
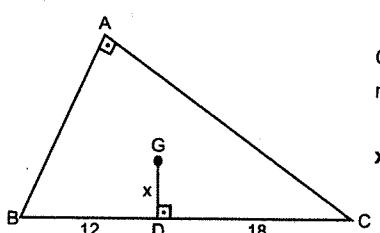
Cevap:  $2\sqrt{58}$ 

45.

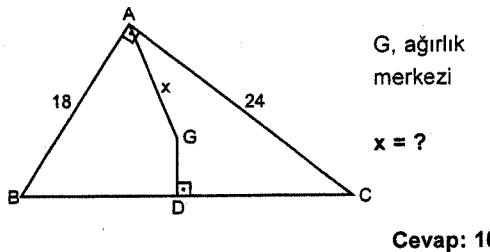
Cevap:  $2\sqrt{10}$ 

46.

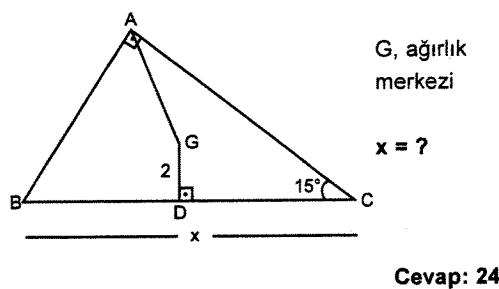
Cevap:  $50^\circ$

**47.** $x = ?$ **Cevap: 45****48.** $x = ?$ **Cevap: 40****49.** $x = ?$ **Cevap: 4****50.** $x = ?$ **Cevap: 50°****51.** $G, \text{ağırlık merkezi}$  $x = ?$ **Cevap: 30****52.** $G, \text{ağırlık merkezi}$  $x = ?$ **Cevap: 12****53.** $G, \text{ağırlık merkezi}$  $x = ?$ **Cevap: 11****54.** $G, \text{ağırlık merkezi}$  $x = ?$ **Cevap: 4**

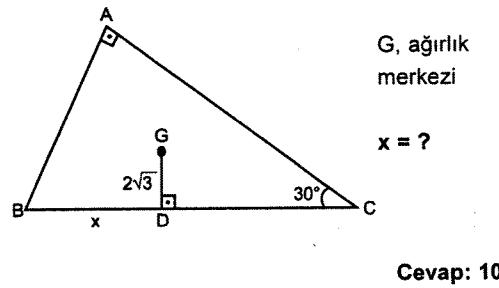
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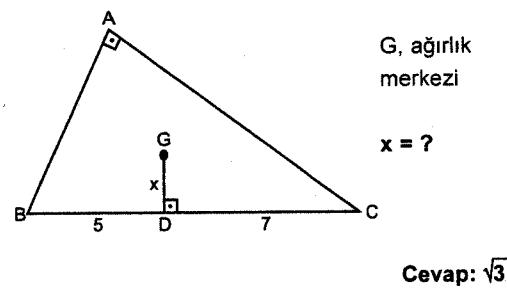
56.



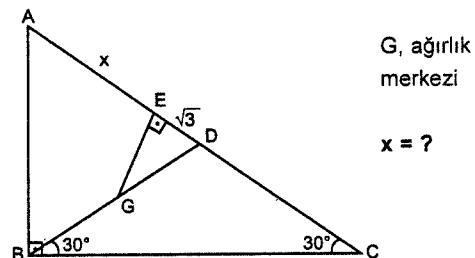
57.



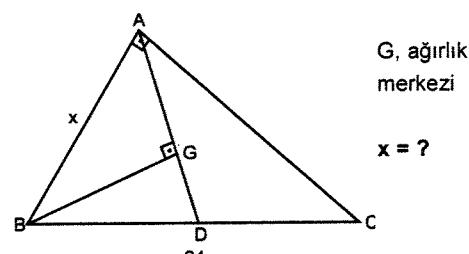
58.



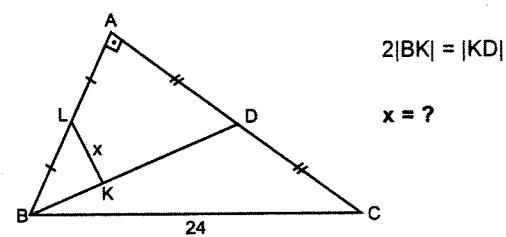
59.



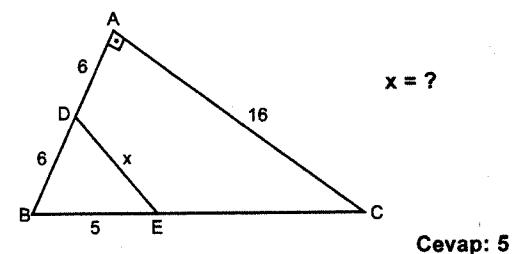
60.



61.



62.



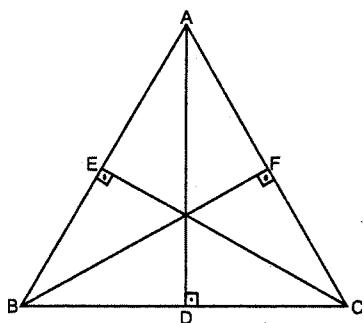
## ÜÇGENDE ALAN

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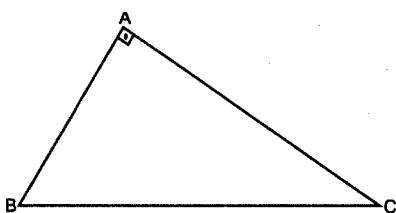
1.



$$\text{Alan}(\triangle ABC) = \frac{\text{Taban} \times \text{Yükseklik}}{2}$$

$$\text{Alan}(\triangle ABC) = \frac{|BC| \cdot |AD|}{2} = \frac{|AB| \cdot |EC|}{2} = \frac{|AC| \cdot |BF|}{2}$$

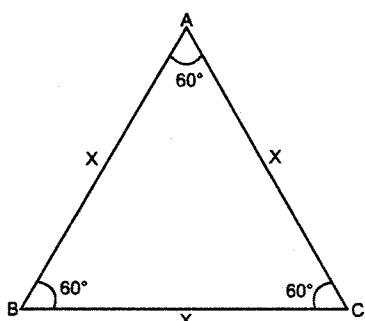
2.



$\text{Alan}(\triangle ABC) = \text{Dik kenarların çarpımının yarısıdır.}$

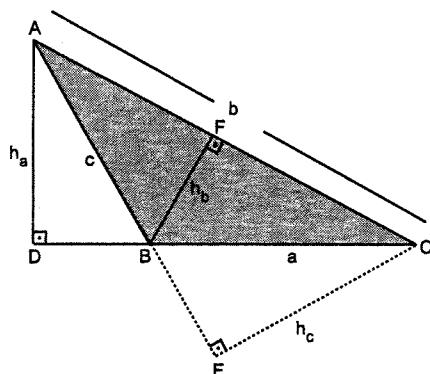
$$\text{Alan}(\triangle ABC) = \frac{|AB| \cdot |AC|}{2}$$

3.



$$\text{Eşkenar üçgenin alanı} = \frac{x^2\sqrt{3}}{4}$$

4.

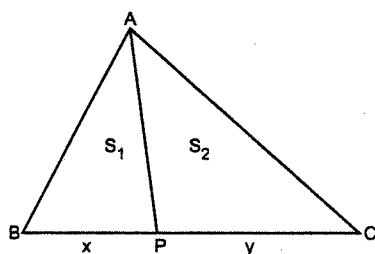


$$\text{Alan}(\triangle ABC) = T.A = \frac{a \cdot h_a}{2} = \frac{b \cdot h_b}{2} = \frac{c \cdot h_c}{2}$$

5.

İkizkenar üçgenin alanı sorulduğu zaman, tepeinden tabana dik indirin ve gerekli işlemler yapıldıktan sonra taban ve bu tabana ait yükseklik çarpımının yarısı kuralı ile alanı bulun.

6.

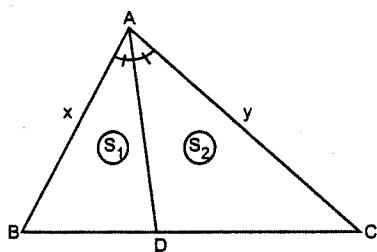


Yükseklikleri aynı olan iki üçgenin alanları oranı tabanları oranına eşittir.

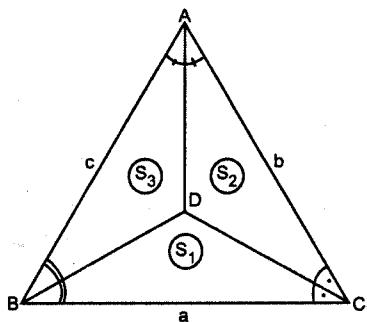
$$\frac{x}{y} = \frac{S_1}{S_2}$$

## AÇIORTAYDA ALAN

7.

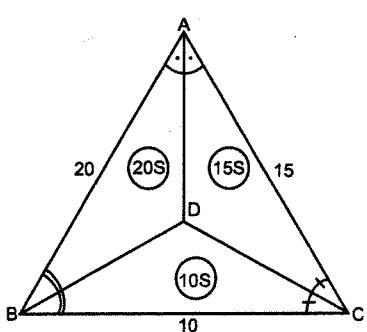


$$\frac{S_1}{S_2} = \frac{x}{y}$$



$$\frac{S_1}{a} = \frac{S_2}{b} = \frac{S_3}{c}$$

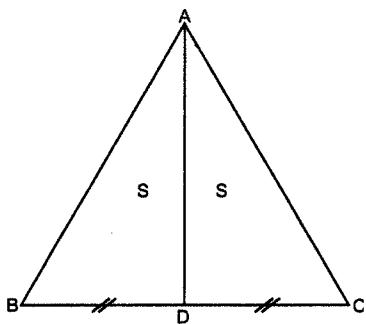
## Örnek



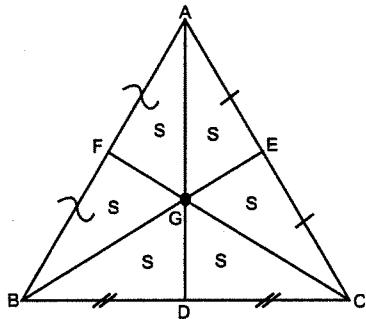
gibi.

## KENARORTAYDA ALAN

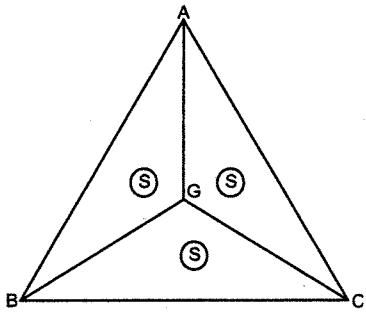
8. a)



b)

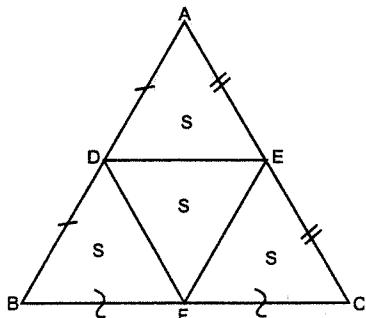


c)



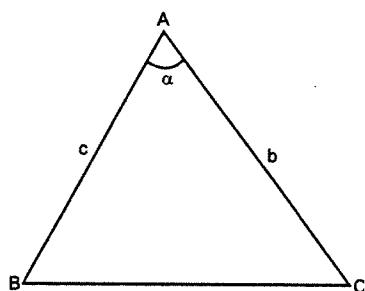
G: ağırlık merkezi

d)



## Sinüs'lü Alan Formülü

9.



$$\text{Alan}(\triangle ABC) = \frac{b.c}{2} \sin\alpha$$

$$\sin 30 = \frac{1}{2} = \sin 150$$

$$\sin 60 = \frac{\sqrt{3}}{2} = \sin 120$$

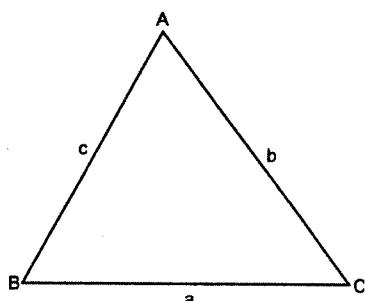
$$\sin 45 = \frac{\sqrt{2}}{2} = \sin 135$$

$$\sin 90 = 1$$

$$\sin\alpha = \sin(180 - \alpha)$$

Alan sorularında iki kenar ve bu iki kenar arasındaki açının sinüs'ü belli ise mutlaka bu formülü uygulayın.

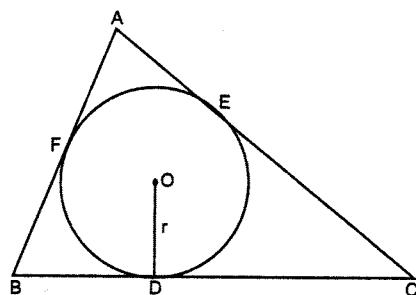
10.



$$\text{Ç}(\triangle ABC) = 2u = a + b + c$$

$$\text{Alan}(\triangle ABC) = \sqrt{u(u-a)(u-b)(u-c)}$$

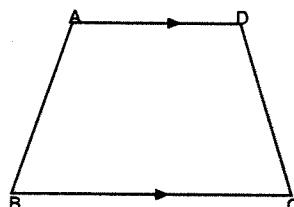
11.



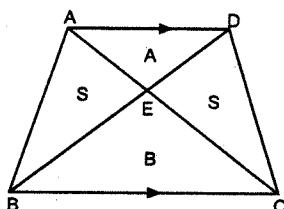
$$\text{Alan}(\triangle ABC) = u \cdot r$$

$$u = \frac{\text{Ç}(\triangle ABC)}{2}$$

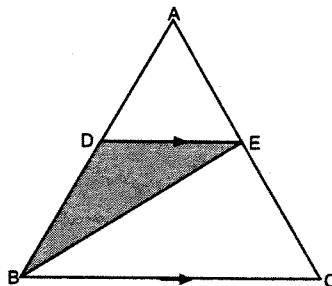
## 12. ALAN KAYDIRMA



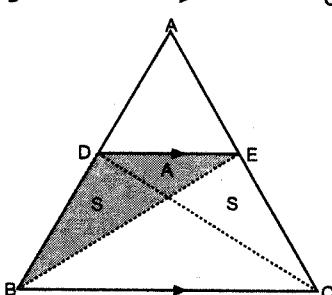
Yamuk



$$S^2 = A \cdot B$$



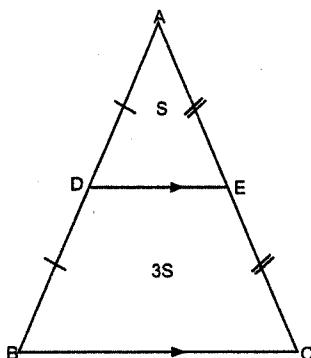
T.A sorulduğunda



$$\text{Alan}(\triangle BDE) = \text{Alan}(\triangle DEC)$$

Alanı kaydirmış olduk.

13. İki üçgen benzer ise benzerik oranını karesi Alanları oranına eşittir.

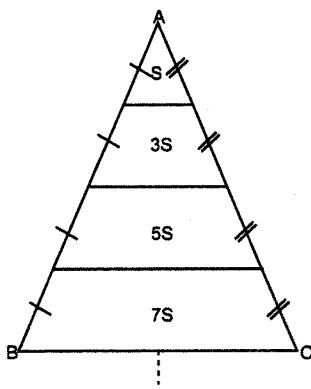


$$k: \text{benzerlik oranı} = \frac{1}{2}$$

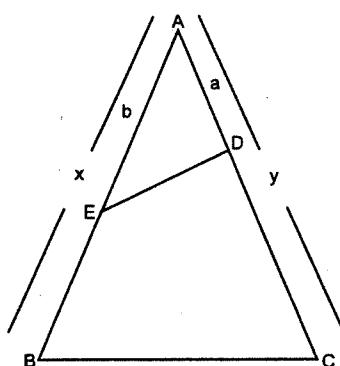
$$k^2 = \text{Alanları oranı} = \frac{1}{4}$$

$$A(\triangle ADE) = S$$

$$A(\triangle ABC) = 4S$$

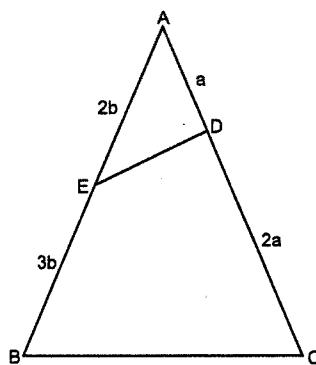


- 14.

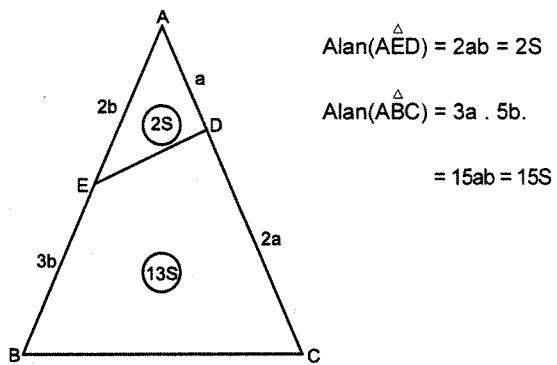


$$\frac{A(\triangle AED)}{A(\triangle ABC)} = \frac{a.b}{x.y}$$

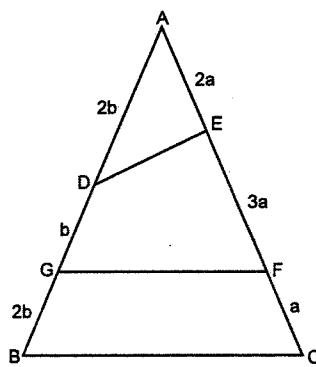
### Örnek



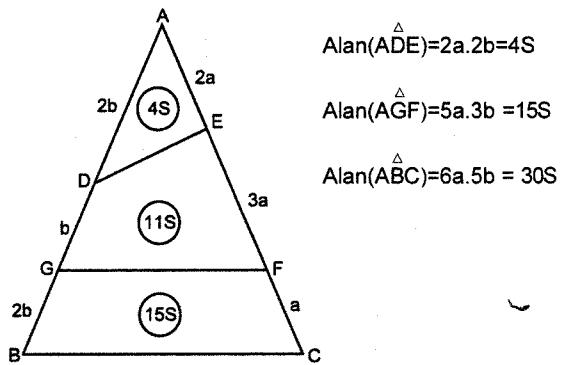
### Çözüm



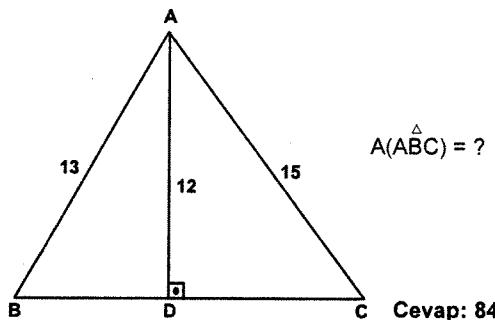
### Örnek



### Çözüm



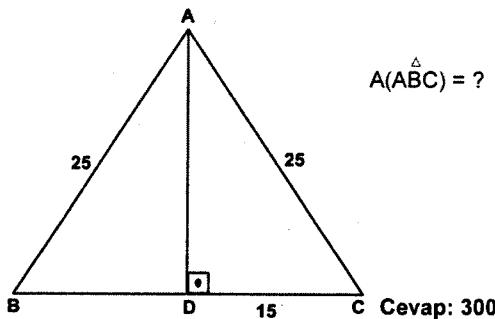
1.



$$A(\triangle ABC) = ?$$

Cevap: 84

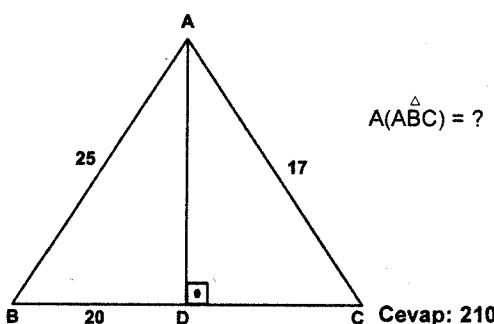
2.



$$A(\triangle ABC) = ?$$

Cevap: 300

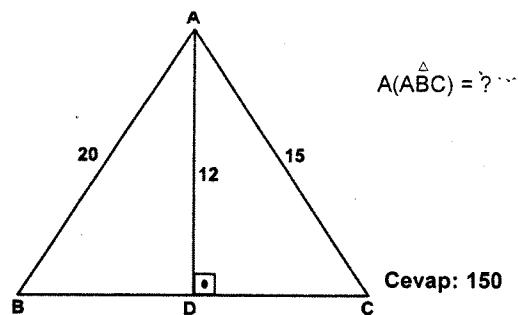
3.



$$A(\triangle ABC) = ?$$

Cevap: 210

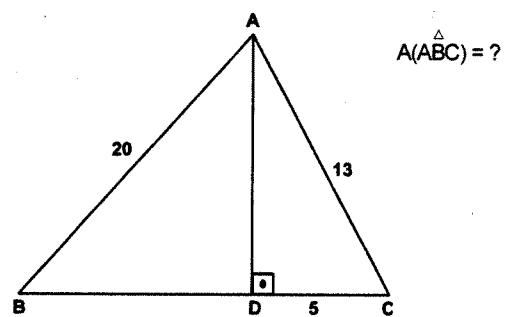
4.



$$A(\triangle ABC) = ?$$

Cevap: 150

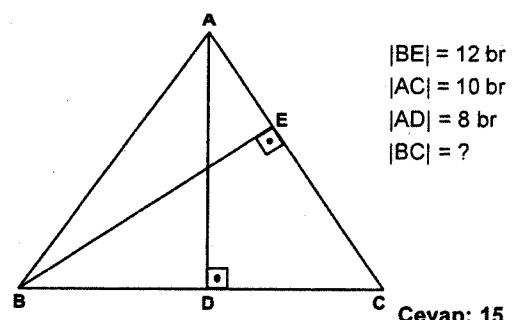
5.



$$A(\triangle ABC) = ?$$

Cevap: 126

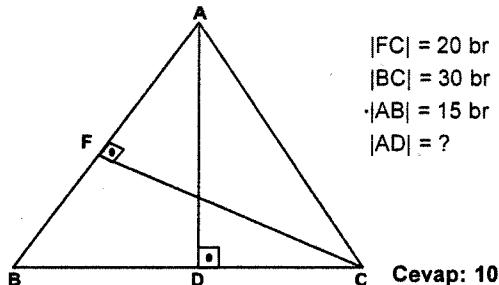
6.



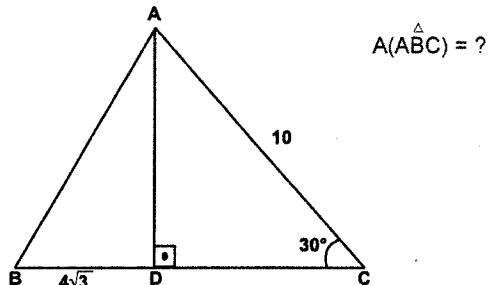
$$\begin{aligned} |BE| &= 12 \text{ br} \\ |AC| &= 10 \text{ br} \\ |AD| &= 8 \text{ br} \\ |BC| &=? \end{aligned}$$

Cevap: 15

7.

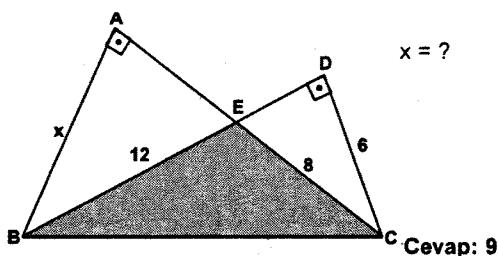


11.

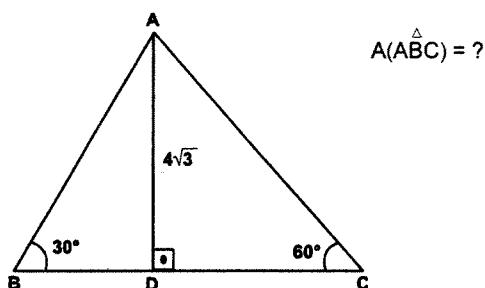


$$\text{Cevap: } \frac{45\sqrt{3}}{2}$$

8.

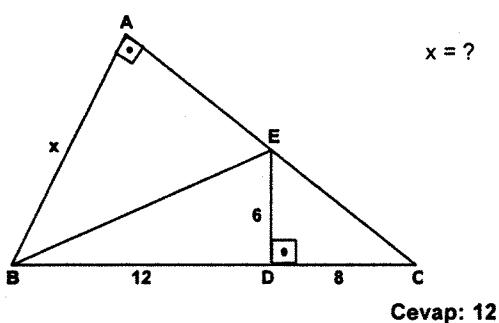


12.

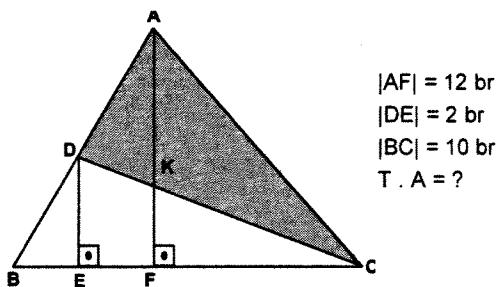


$$\text{Cevap: } 32\sqrt{3}$$

9.

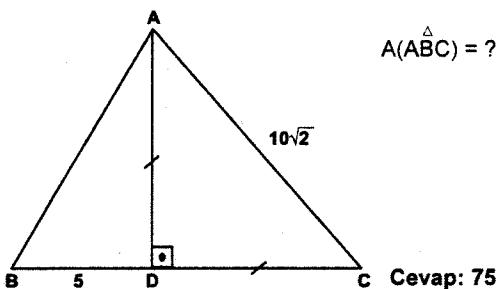


13.

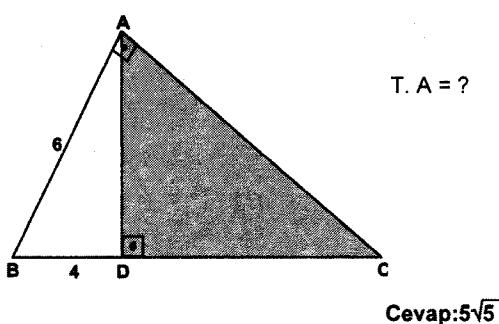


$$\text{Cevap: } 50$$

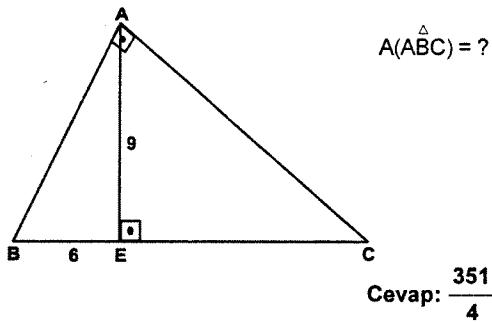
10.



14.



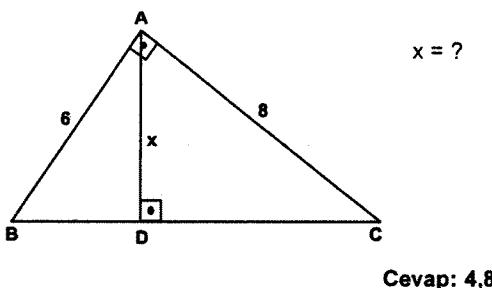
15.



$$A(\triangle ABC) = ?$$

$$\text{Cevap: } \frac{351}{4}$$

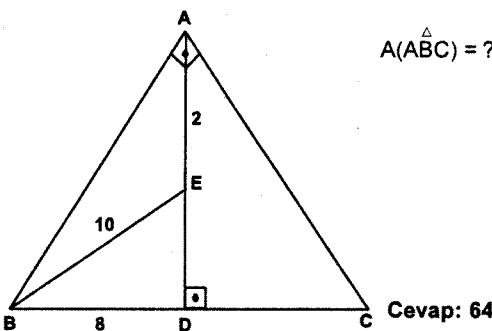
16.



$$x = ?$$

$$\text{Cevap: } 4,8$$

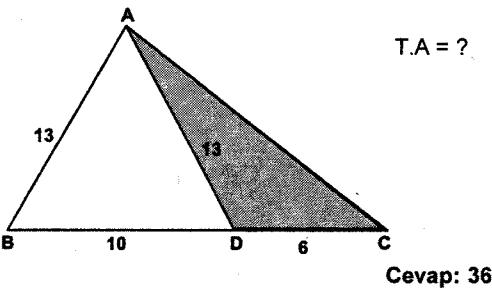
17.



$$A(\triangle ABC) = ?$$

$$\text{Cevap: } 64$$

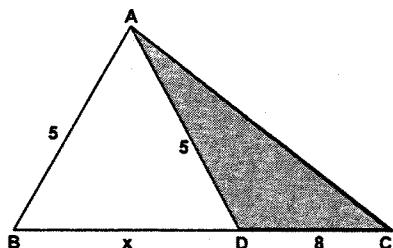
18.



$$T.A = ?$$

$$\text{Cevap: } 36$$

19.

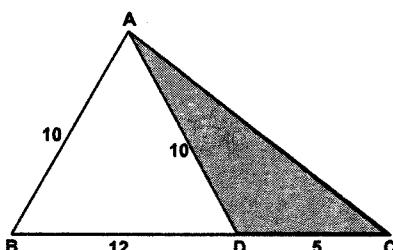


$$T : A = 12$$

$$x = ?$$

$$\text{Cevap: } 8$$

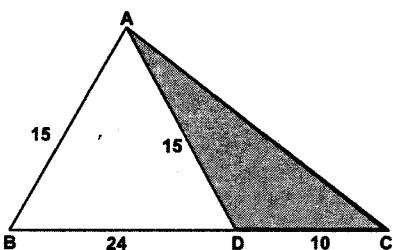
20.



$$T : A = ?$$

$$\text{Cevap: } 20$$

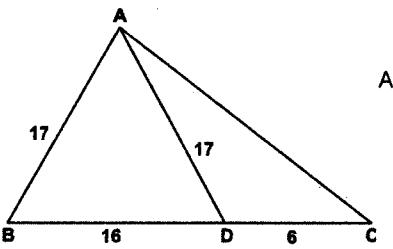
21.



$$T : A = ?$$

$$\text{Cevap: } 45$$

22.



$$A(\triangle ABC) = ?$$

$$\text{Cevap: } 165$$

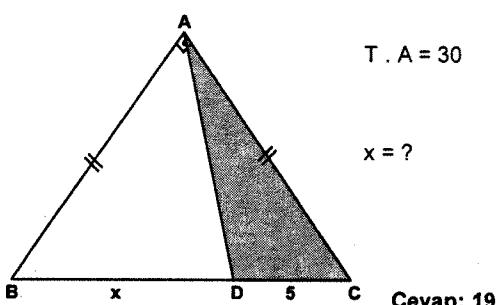
23.



$T.A = ?$

$Cevap: \sqrt{5}$

24.

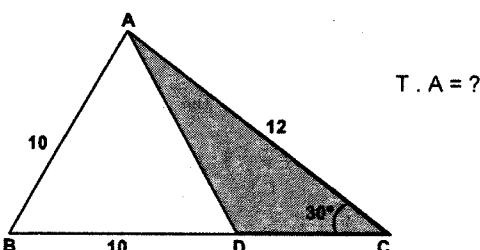


$T.A = 30$

$x = ?$

$Cevap: 19$

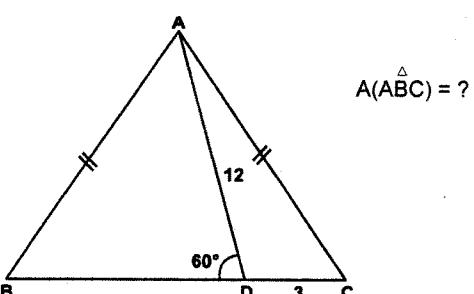
25.



$T.A = ?$

$Cevap: 18\sqrt{3} - 6$

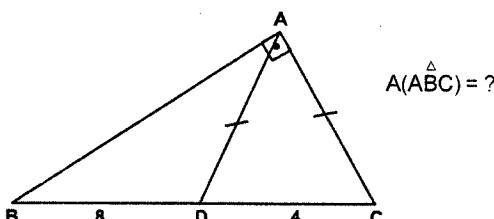
26.



$A(\triangle ABC) = ?$

$Cevap: 54\sqrt{3}$

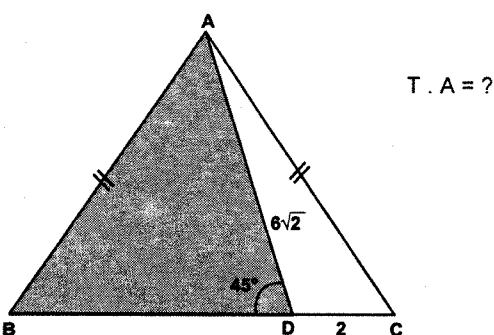
27.



$A(\triangle ABC) = ?$

$Cevap: 12\sqrt{5}$

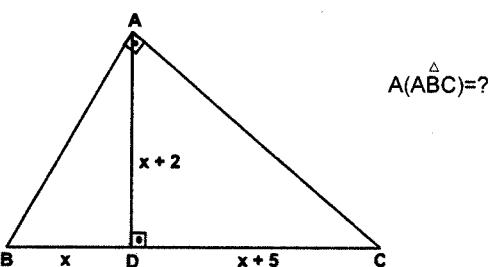
28.



$T.A = ?$

$Cevap: 42$

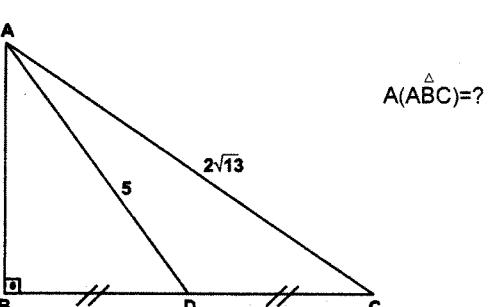
29.



$A(\triangle ABC) = ?$

$Cevap: 39$

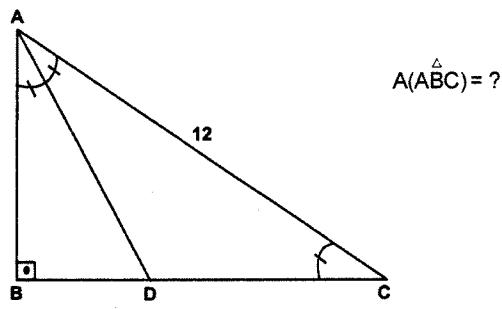
30.



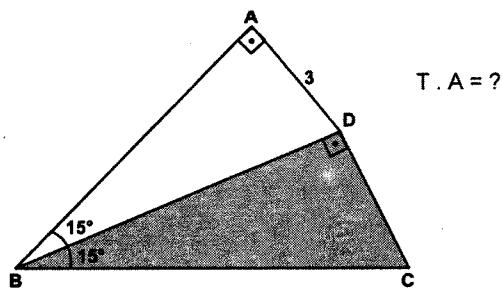
$A(\triangle ABC) = ?$

$Cevap: 12$

31.

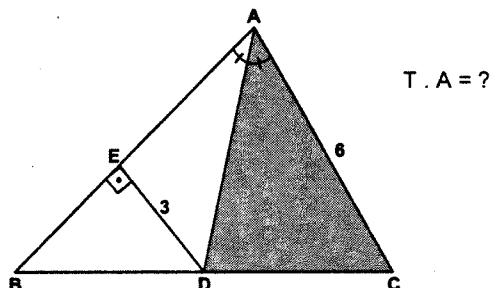
Cevap:  $18\sqrt{3}$ 

32.



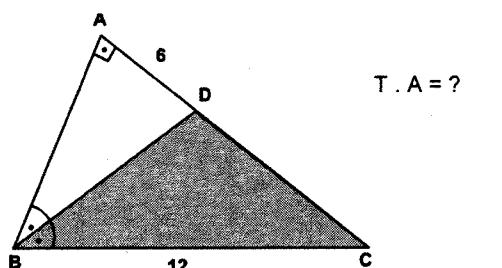
Cevap: 18

33.



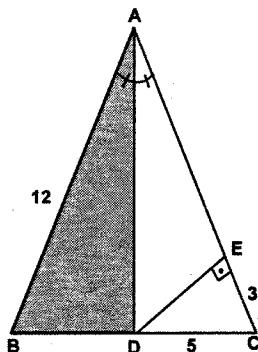
Cevap: 9

34.



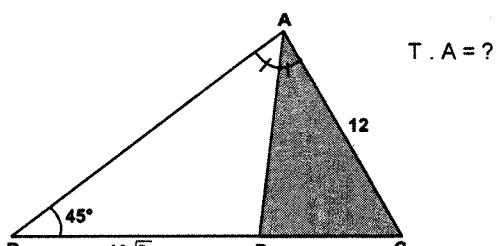
Cevap: 36

35.



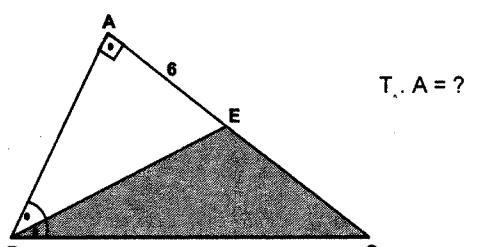
Cevap: 24

36.



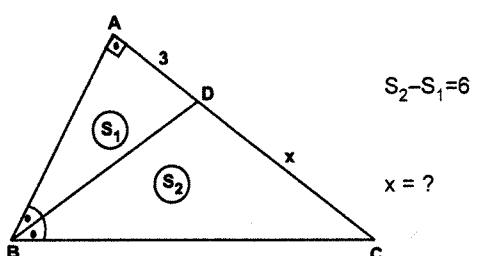
Cevap: 60

37.



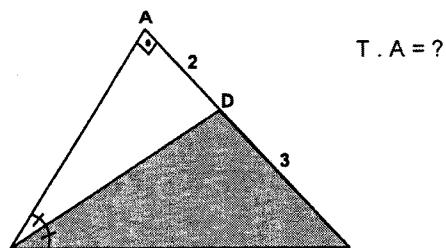
Cevap: 60

38.



Cevap: 5

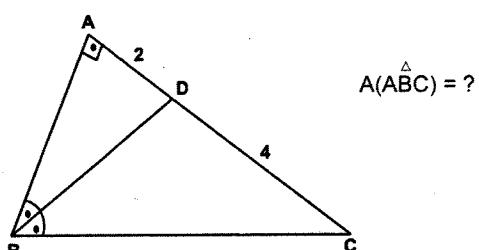
39.



$$T \cdot A = ?$$

Cevap:  $3\sqrt{5}$ 

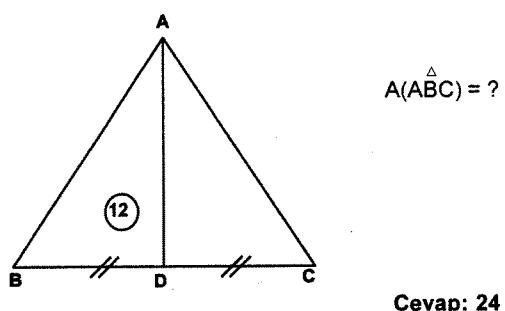
40.



$$A(\triangle ABC) = ?$$

Cevap:  $6\sqrt{3}$ 

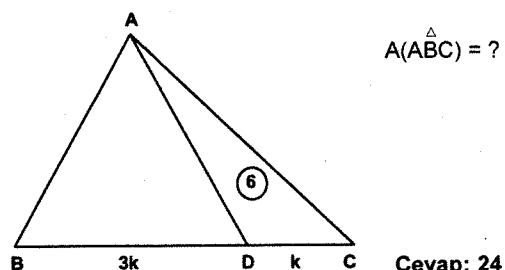
41.



$$A(\triangle ABC) = ?$$

Cevap: 24

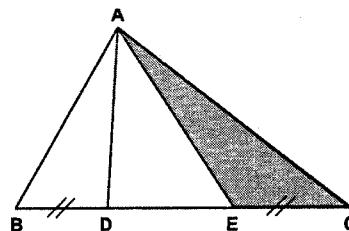
42.



$$A(\triangle ABC) = ?$$

Cevap: 24

43.



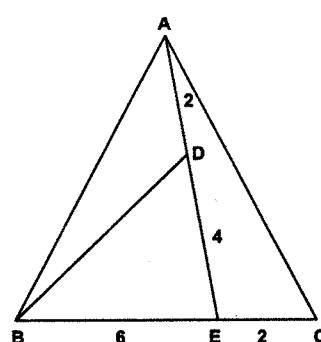
$$2|DE| = |BC|$$

$$A(\triangle ABC) = 32$$

$$T \cdot A = ?$$

Cevap: 8

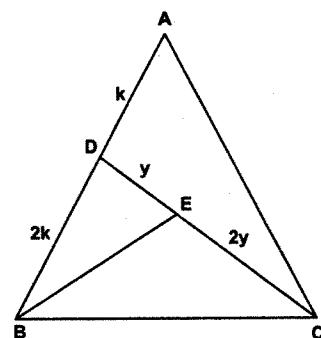
44.



$$\frac{A(\triangle ABD)}{A(\triangle ABC)} = ?$$

Cevap:  $\frac{1}{4}$ 

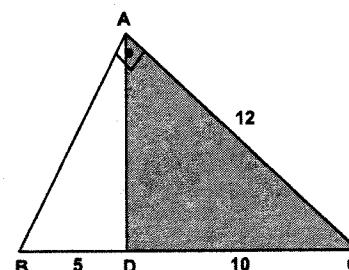
45.



$$\frac{A(\triangle BEC)}{A(\triangle ABC)} = ?$$

Cevap:  $\frac{4}{9}$ 

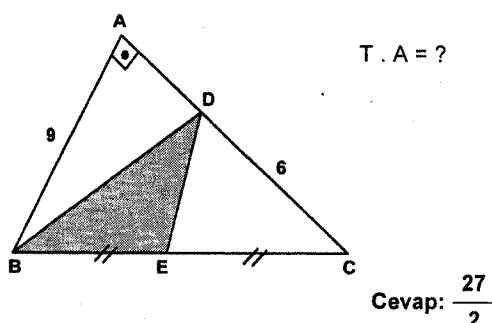
46.



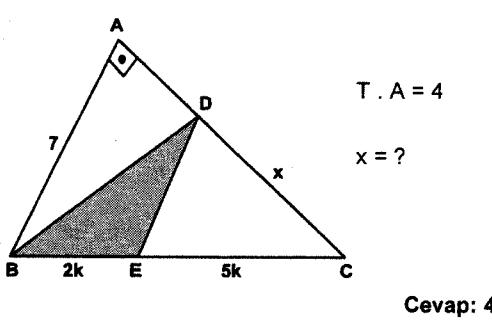
$$T \cdot A = ?$$

Cevap: 36

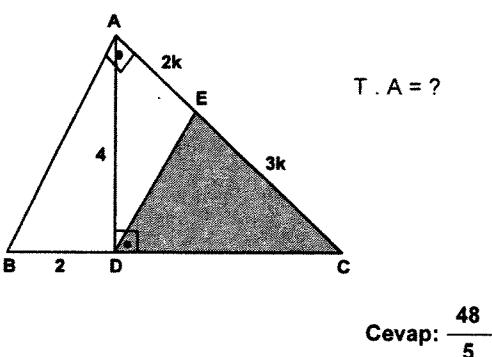
47.



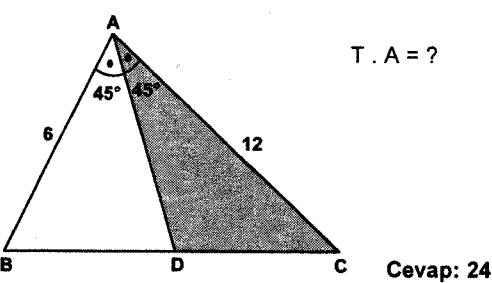
48.



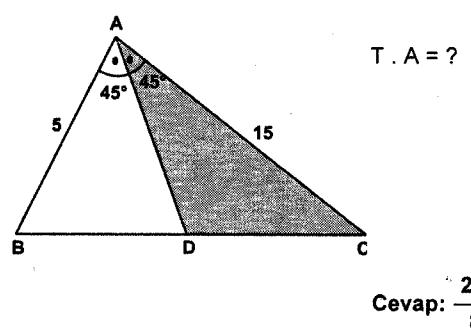
49.



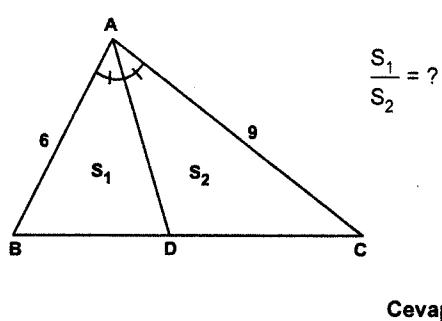
50.



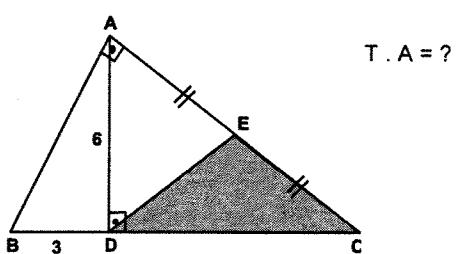
51.



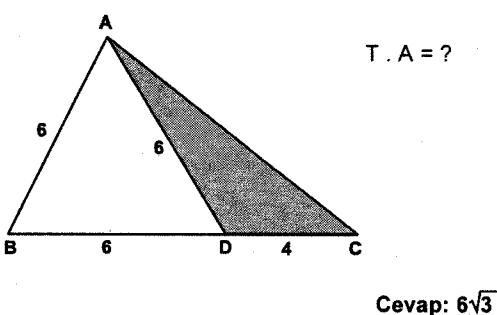
52.



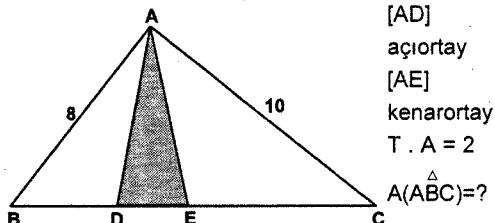
53.



54.

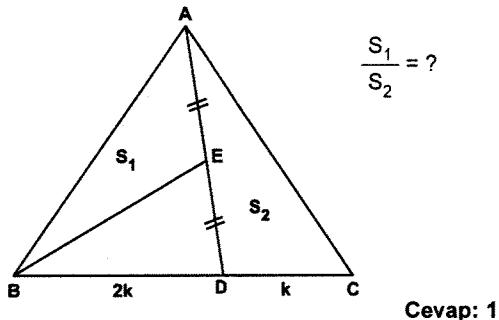


55.



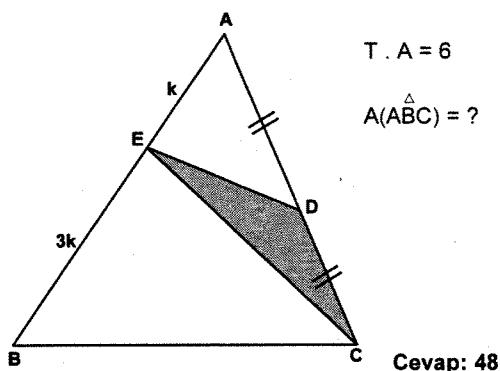
Cevap: 36

56.



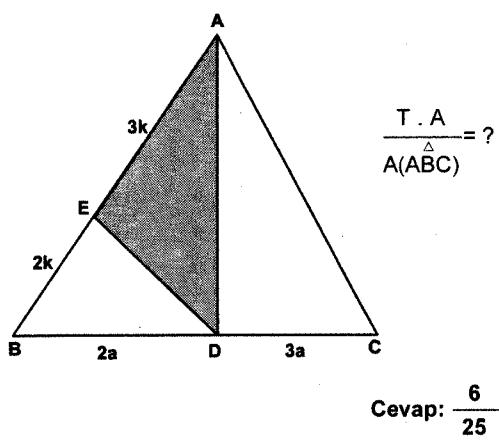
Cevap: 1

57.

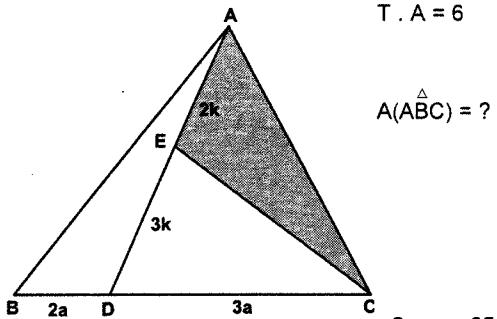


Cevap: 48

58.

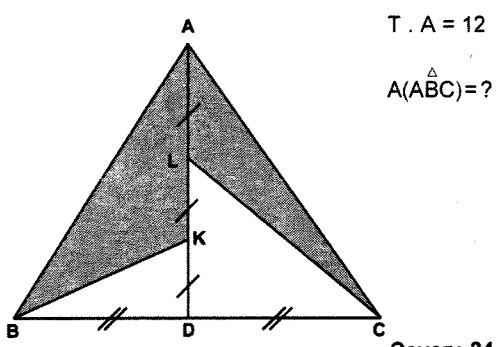
Cevap:  $\frac{6}{25}$ 

59.



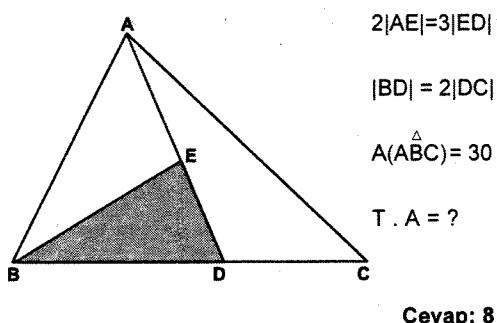
Cevap: 25

60.



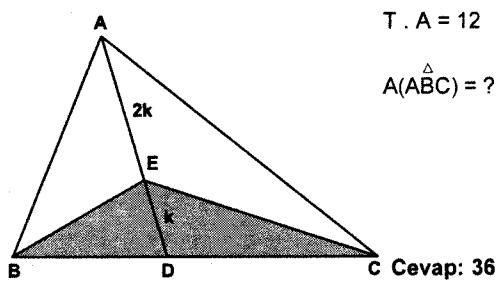
Cevap: 24

61.



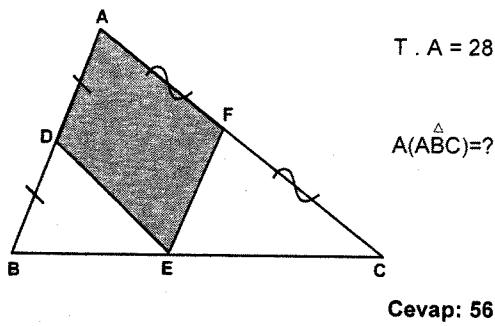
Cevap: 8

62.

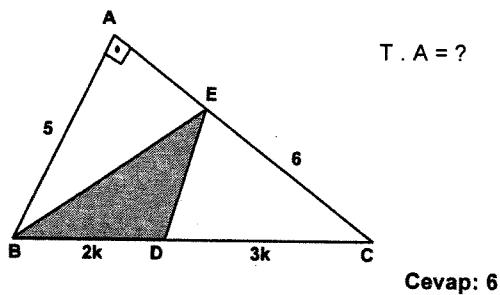


Cevap: 36

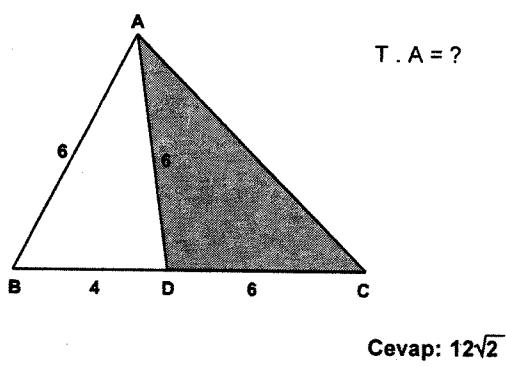
63.



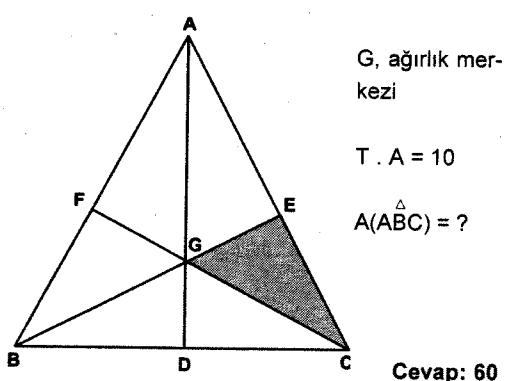
64.



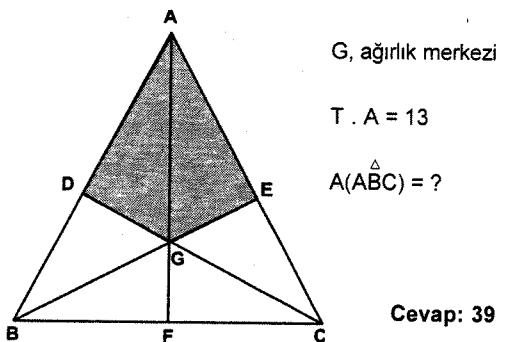
65.



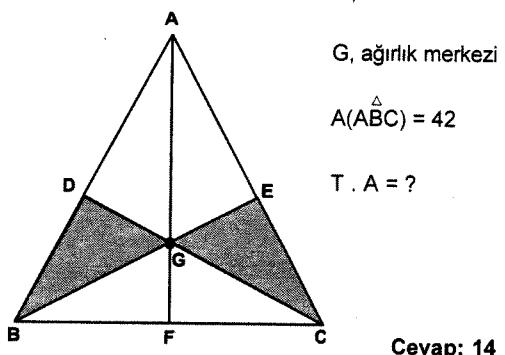
66.



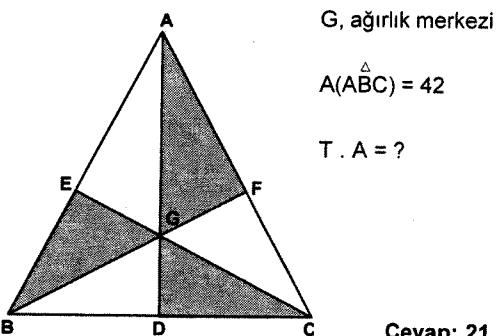
67.



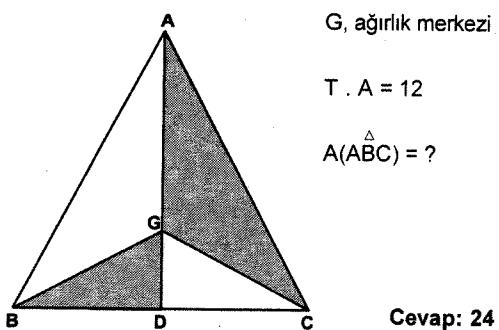
68.



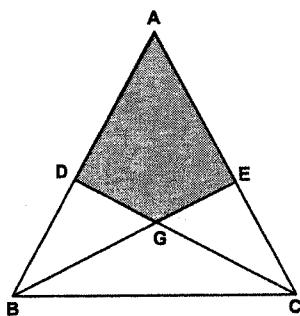
69.



70.



71.

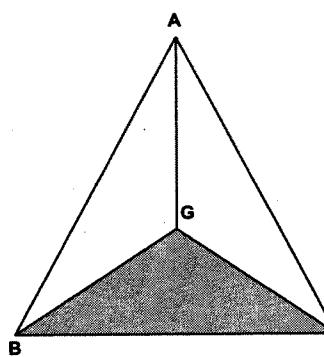
G, ağırlık  
merkezi

$$A(\triangle BGC) = 20$$

$$T \cdot A = ?$$

Cevap: 20

72.

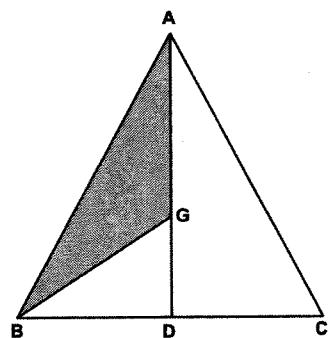
G, ağırlık  
merkezi

$$T \cdot A = 18$$

$$A(\triangle ABC) = ?$$

Cevap: 54

73.

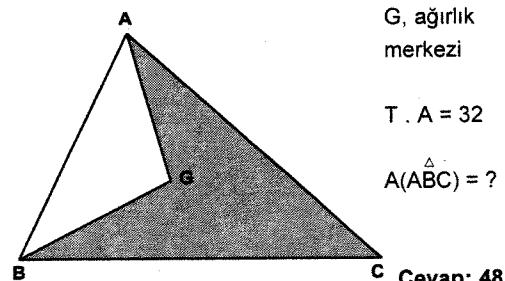
G, ağırlık  
merkezi

$$A(\triangle ADC) = 12$$

$$T \cdot A = ?$$

Cevap: 8

74.

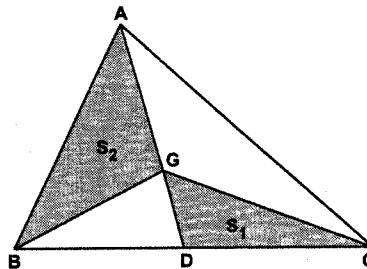
G, ağırlık  
merkezi

$$T \cdot A = 32$$

$$A(\triangle ABC) = ?$$

Cevap: 48

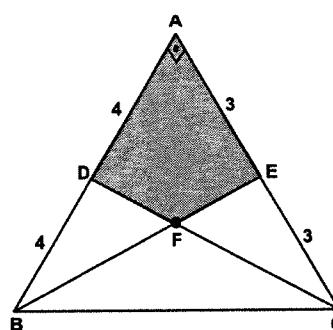
75.

G, ağırlık  
merkezi

$$\frac{S_1}{S_2} = ?$$

Cevap:  $\frac{1}{2}$ 

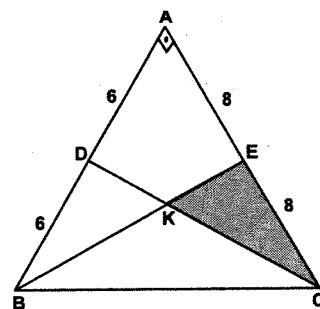
76.



$$T \cdot A = ?$$

Cevap: 8

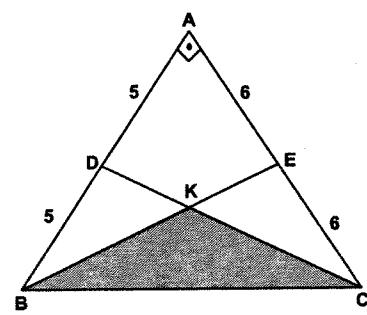
77.



$$T \cdot A = ?$$

Cevap: 16

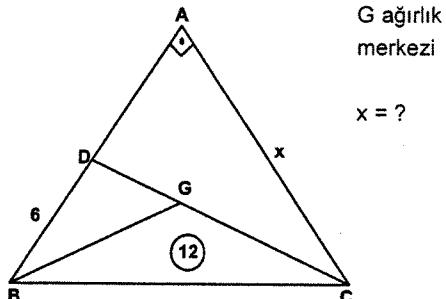
78.



$$T \cdot A = ?$$

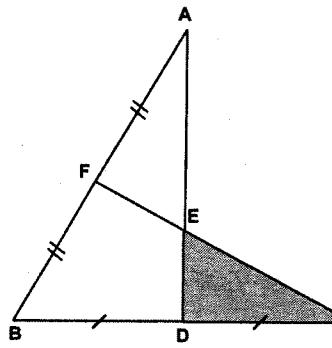
Cevap: 20

79.



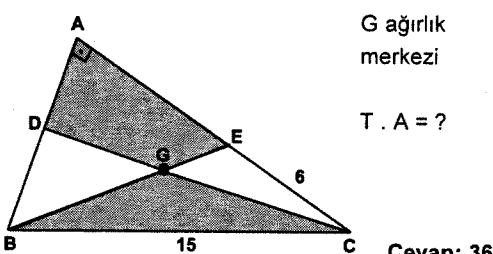
Cevap: 6

83.



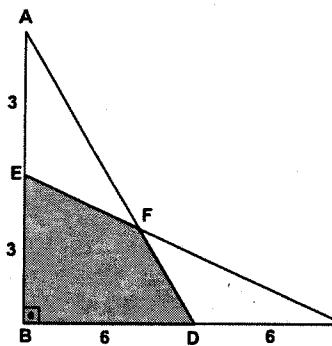
Cevap: 15

80.



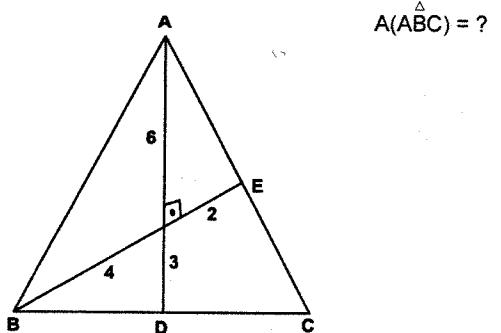
Cevap: 36

84.



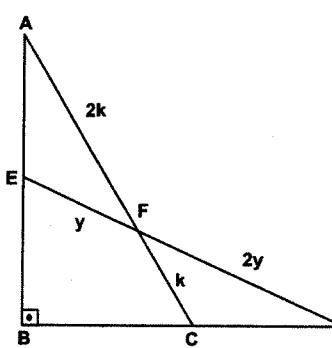
Cevap: 12

81.



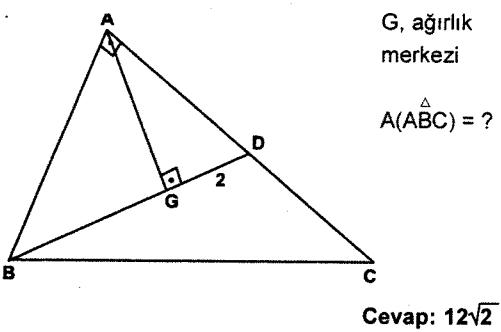
Cevap: 36

85.

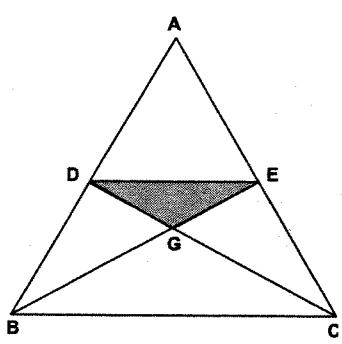


Cevap: 32

82.

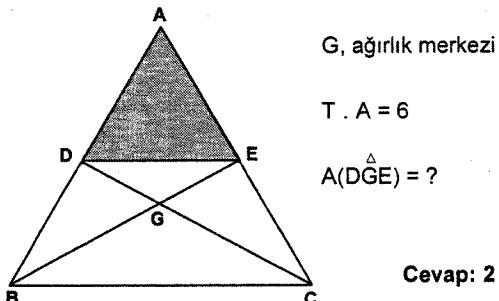
Cevap:  $12\sqrt{2}$ 

86.



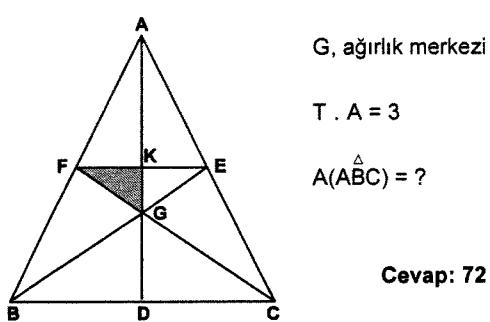
Cevap: 72

87.



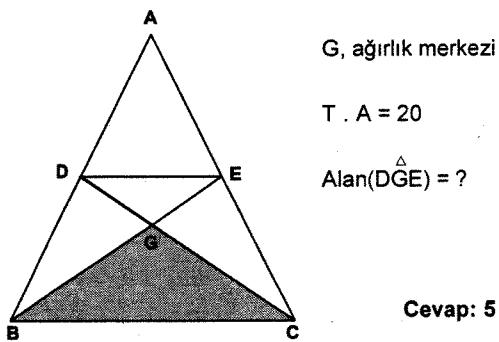
Cevap: 2

88.



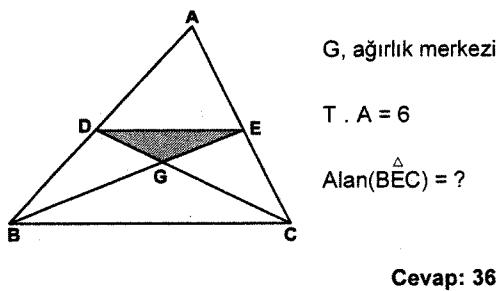
Cevap: 72

89.



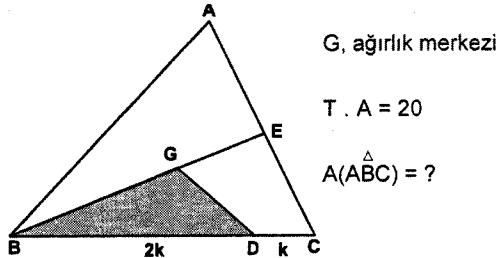
Cevap: 5

90.



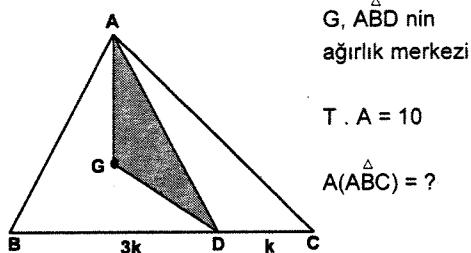
Cevap: 36

91.



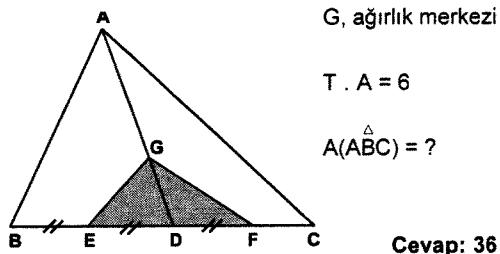
Cevap: 90

92.



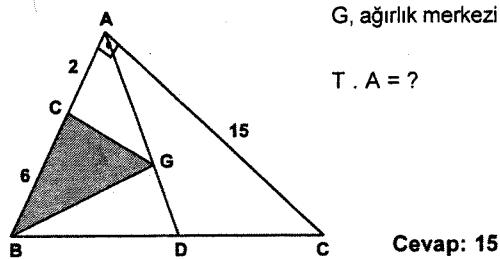
Cevap: 40

93.



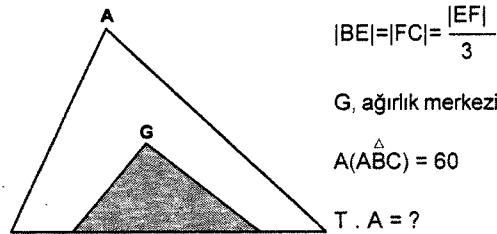
Cevap: 36

94.



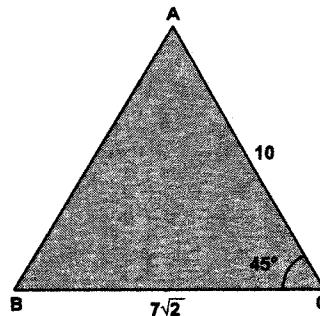
Cevap: 15

95.



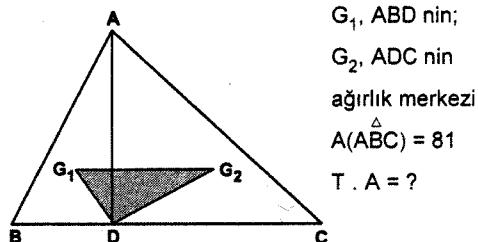
Cevap: 12

99.



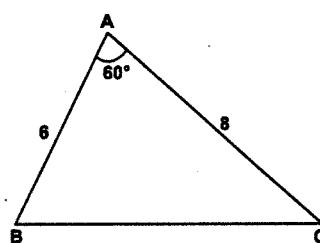
Cevap: 35

96.

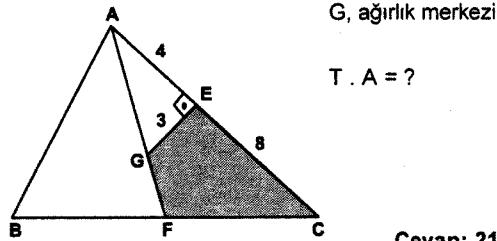


Cevap: 9

100.

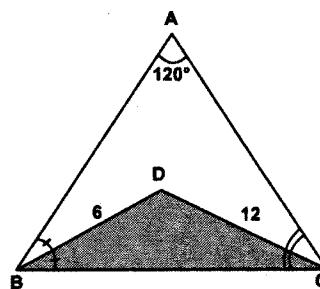
Cevap:  $12\sqrt{3}$ 

97.



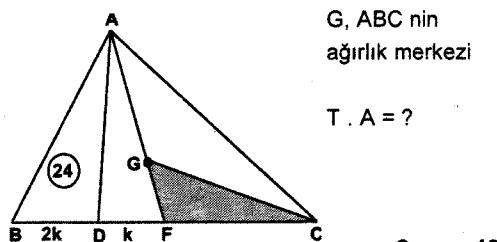
Cevap: 21

101.



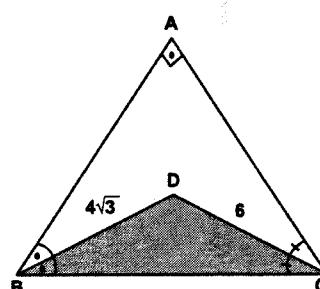
Cevap: 18

98.

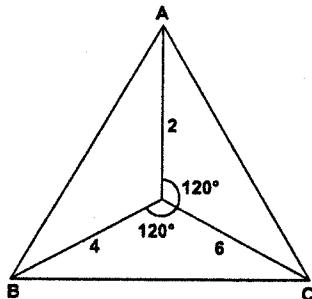


Cevap: 12

102.

Cevap:  $6\sqrt{6}$

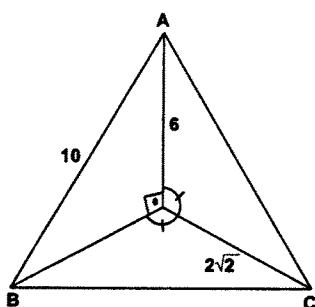
103.



$A(\triangle ABC) = ?$

Cevap:  $11\sqrt{3}$ 

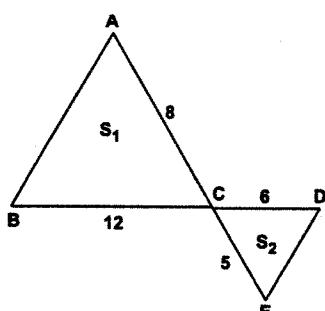
104.



$A(\triangle ABC) = ?$

Cevap: 38

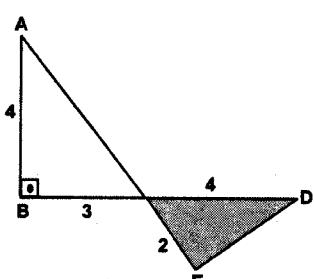
105.



$\frac{S_1}{S_2} = ?$

Cevap:  $\frac{16}{5}$ 

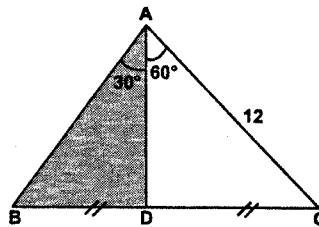
105.



$T.A = ?$

Cevap:  $\frac{16}{5}$ 

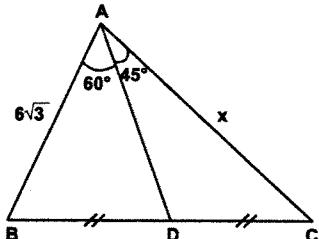
107.



$T.A = ?$

Cevap:  $36\sqrt{3}$ 

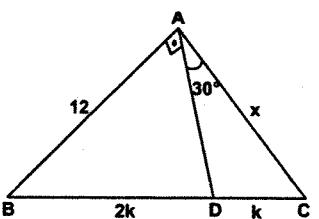
108.



$x = ?$

Cevap:  $9\sqrt{2}$ 

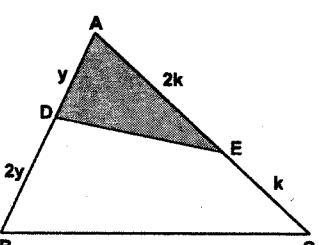
109.



$x = ?$

Cevap: 12

110.

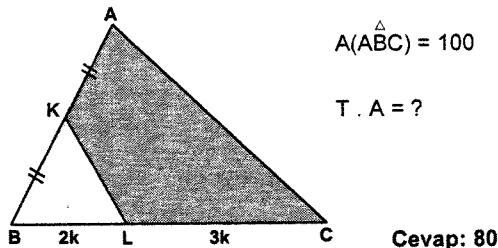


$A(\triangle ABC) = 36$

$T.A = ?$

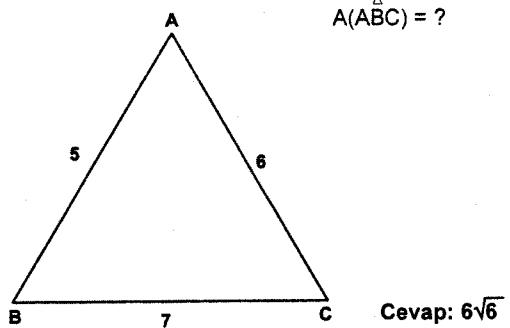
Cevap: 8

111.

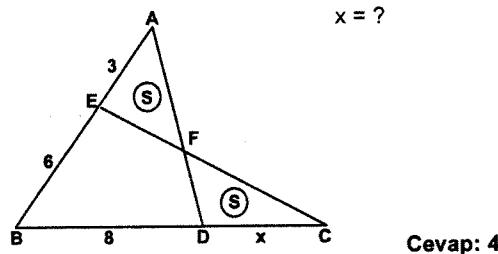


Cevap: 80

115.

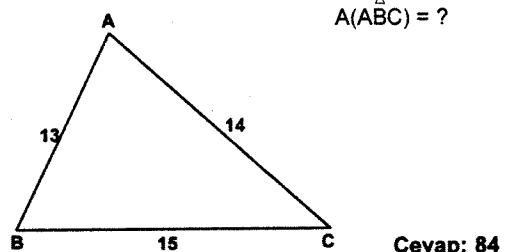
Cevap:  $6\sqrt{6}$ 

112.



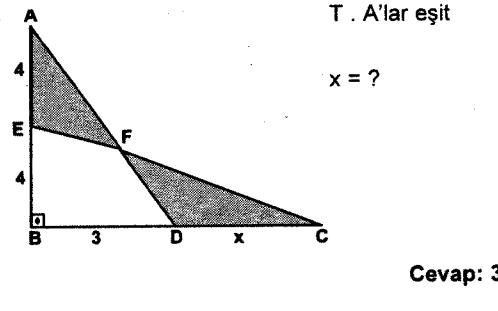
Cevap: 4

116.



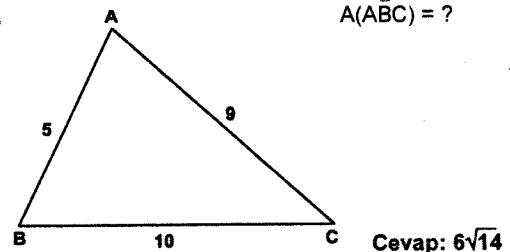
Cevap: 84

113.

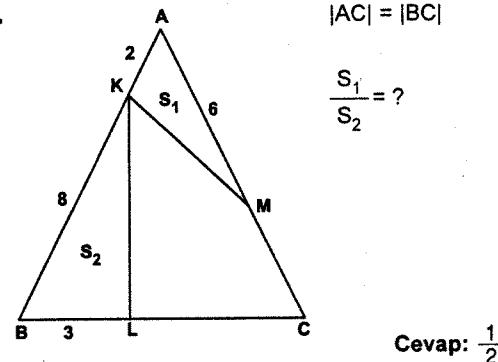


Cevap: 3

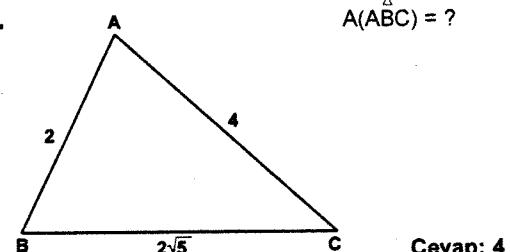
117.

Cevap:  $6\sqrt{14}$ 

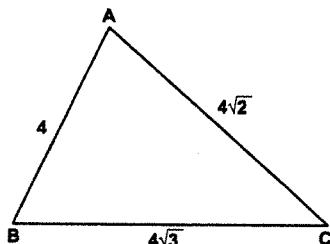
114.

Cevap:  $\frac{1}{2}$ 

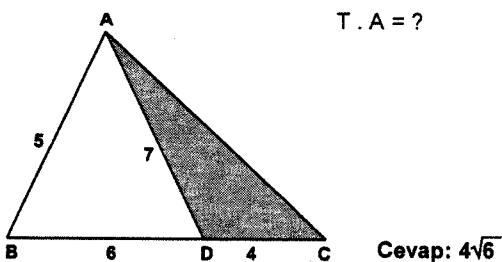
118.



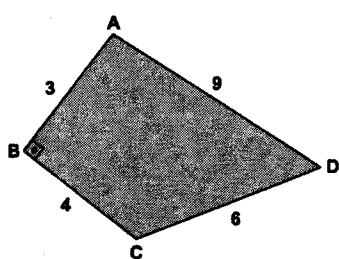
Cevap: 4

**119.**

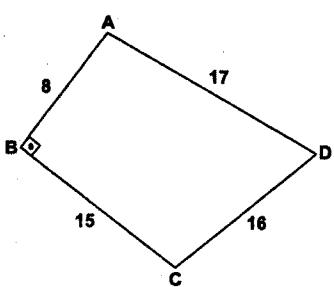
$$A(\triangle ABC) = ?$$

Cevap:  $8\sqrt{2}$ **120.**

$$T \cdot A = ?$$

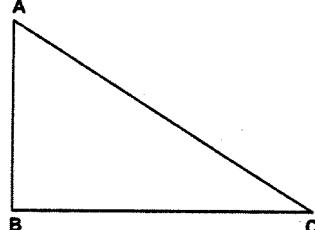
Cevap:  $4\sqrt{6}$ **121.**

$$T \cdot A = ?$$

Cevap:  $10\sqrt{2} + 6$ **122.**

$$A(\square ABCD) = ?$$

Cevap: 180

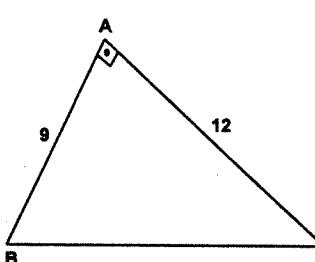
**123.**

İç teğet çemberinin yarıçapı 3 ve

$$\angle C(\triangle ABC) = 20^\circ$$

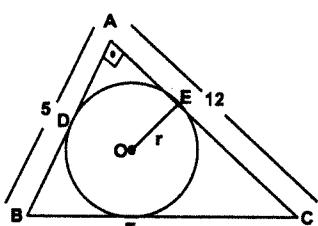
$$A(\triangle ABC) = ?$$

Cevap: 30

**124.**

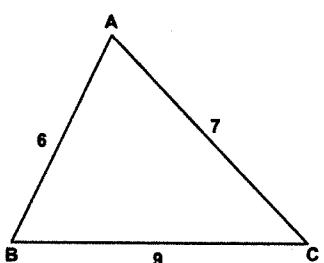
İç teğet çemberinin yarıçapı kaçtır?

Cevap: 3

**125.**

İç teğet çemberinin yarıçapı kaçtır?

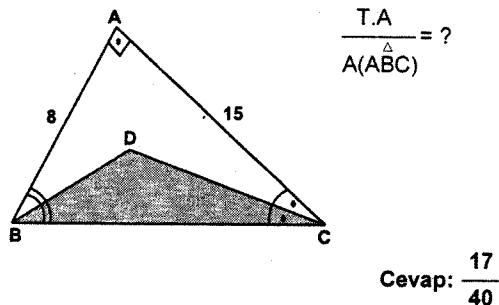
Cevap: 2

**126.**

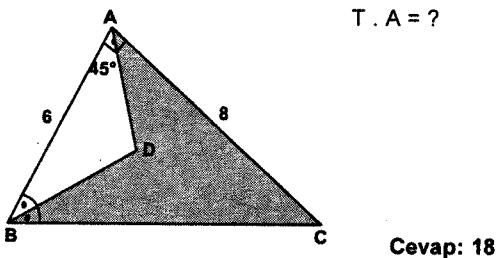
İç teğet çemberinin yarıçapı kaçtır?

Cevap:  $\frac{2\sqrt{110}}{11}$

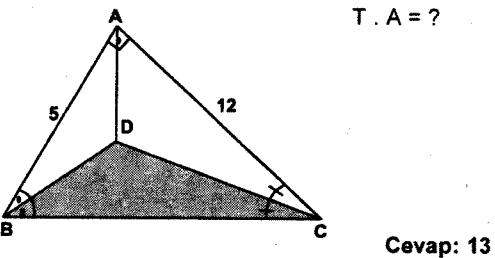
127.



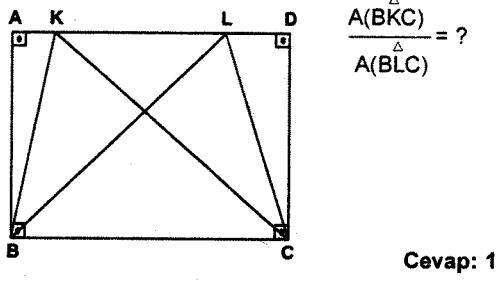
128.



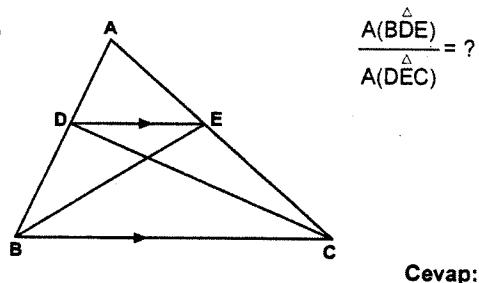
129.



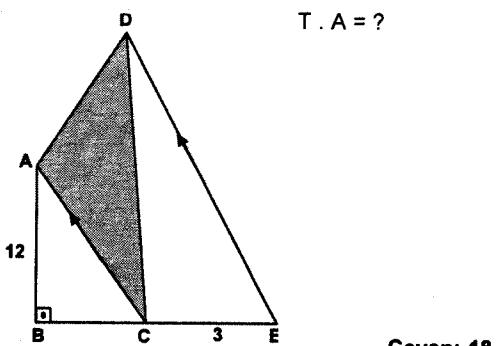
130.



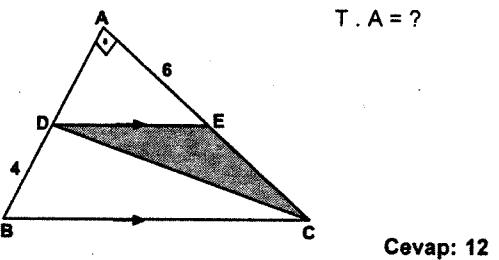
131.



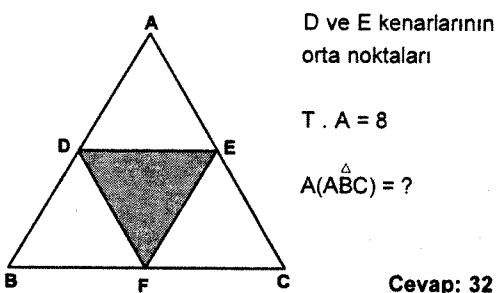
132.



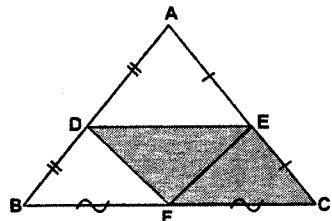
133.



134.



135.

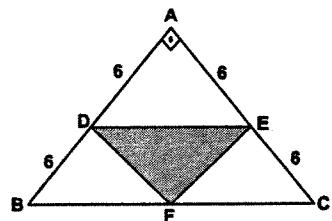


$$A(\triangle ABC) = 40$$

T . A = ?

Cevap: 20

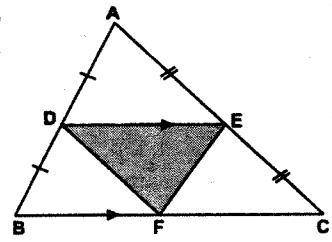
136.



T . A = ?

Cevap: 18

137.

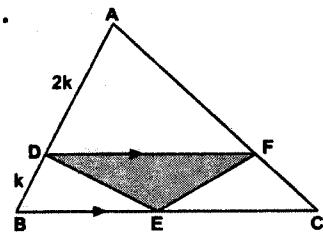


T . A = 10

$$A(\triangle ABC) = ?$$

Cevap: 40

138.

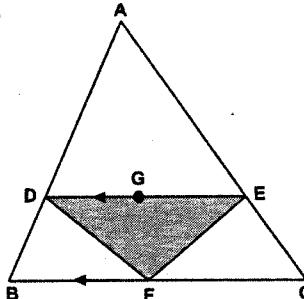


T . A = 20

$$A(\triangle ABC) = ?$$

Cevap: 90

139.



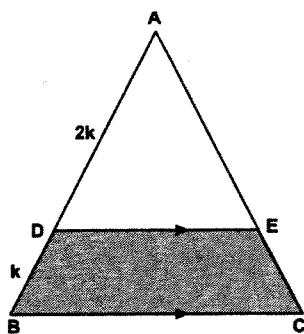
G, ağırlık merkezi

$$A(\triangle ABC) = 120$$

T . A = ?

Cevap:  $\frac{80}{3}$

140.

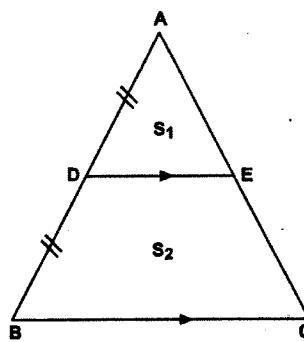


$$A(\triangle ABC) = 81$$

T . A = ?

Cevap: 45

141.

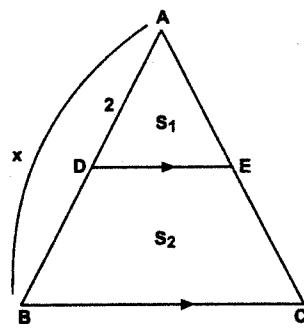


$$S_2 - S_1 = 16$$

$$A(\triangle ABC) = ?$$

Cevap: 32

142.



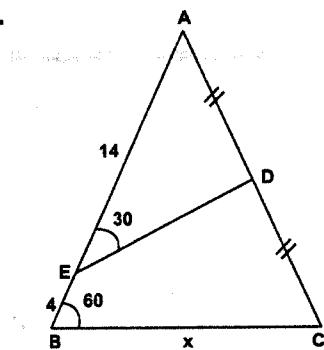
$$S_2 = S_1$$

$$x = ?$$

Cevap:  $2\sqrt{2}$



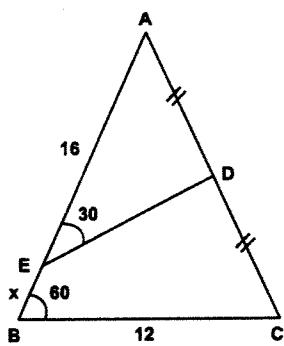
7.



$x = ?$

Cevap: 10

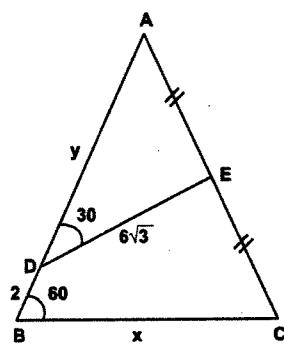
8.



$x = ?$

Cevap: 4

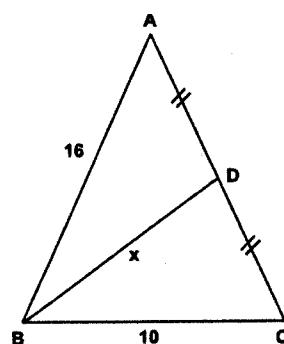
9.



$y + x = ?$

Cevap: 26

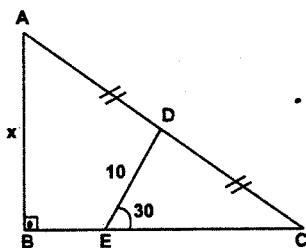
10.



x'in alabileceği kaç tam sayı değeri vardır?

Cevap: 9

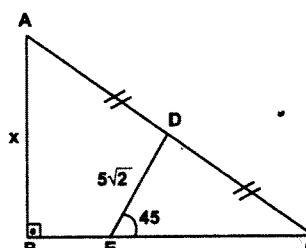
11.



$x = ?$

Cevap: 10

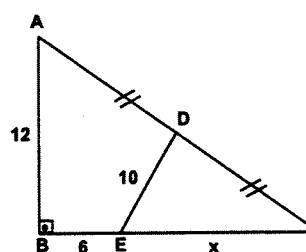
12.



$x = ?$

Cevap: 10

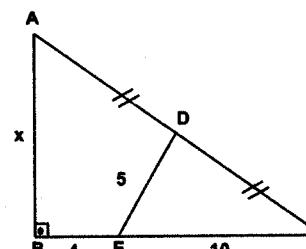
13.



$x = ?$

Cevap: 22

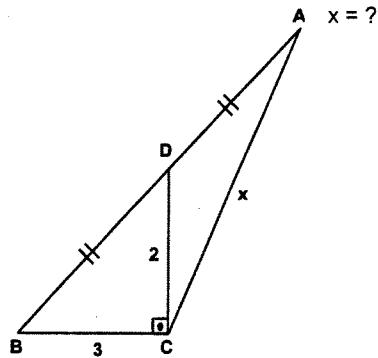
14.



$x = ?$

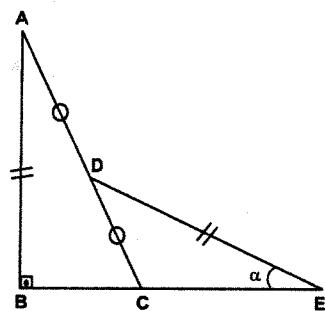
Cevap: 8

15.



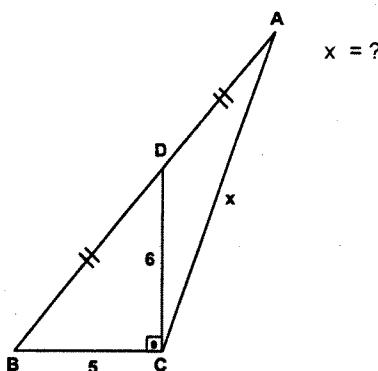
Cevap: 5

19.

 $\alpha = ?$ 

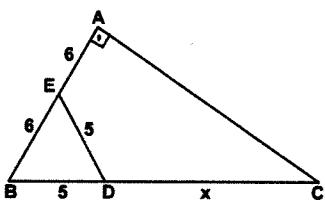
Cevap: 30

16.



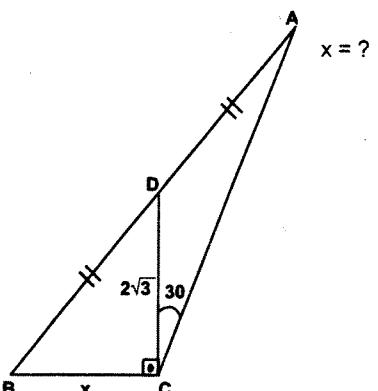
Cevap: 13

20.

 $x = ?$ 

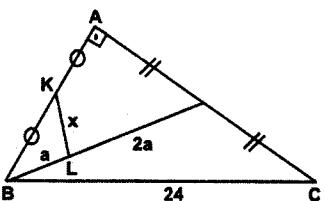
Cevap: 15

17



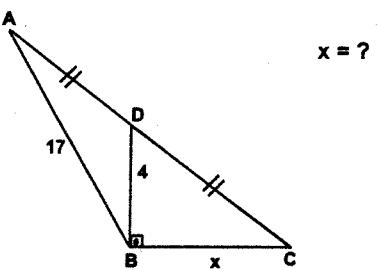
Cevap: 4

21.

 $x = ?$ 

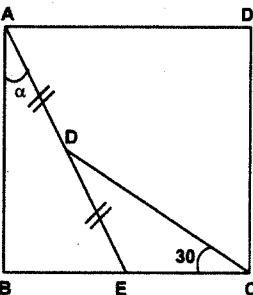
Cevap: 4

18.



Cevap: 15

22.

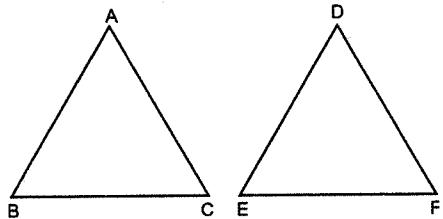


ABCD kare

 $x = ?$ 

Cevap: 15

# BENZERLİK



İki üçgen benzer ise kenarları orantılı, orantılı kenarların karşısındaki açılar ise eşittir.

“ $\sim$ ” Benzerlik simbolüdür.

$$\triangle ABC \sim \triangle DEF \Rightarrow m(\widehat{A}) = m(\widehat{D}) \\ m(\widehat{B}) = m(\widehat{E}) \\ m(\widehat{C}) = m(\widehat{F}) \text{ ve}$$

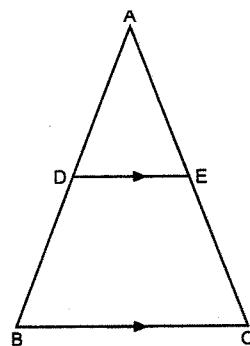
$$\frac{|AB|}{|DE|} = \frac{|BC|}{|EF|} = \frac{|AC|}{|DF|} = k$$

$k$ : benzerlik oranıdır.

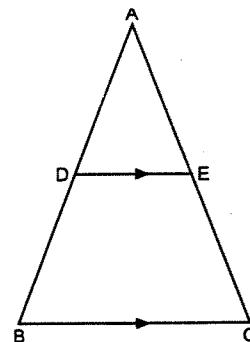
## \* İki üçgen benzer ise

- Kenarları oranı
- yükseklikleri oranı
- açıortayları oranı
- kenarortayları oranı
- çevreleri oranı benzerlik oranı ( $k$ )'ya eşittir.
- Alanları oranı ise benzerlik oranının karesine eşittir.

## Temel Benzerlik Şekli

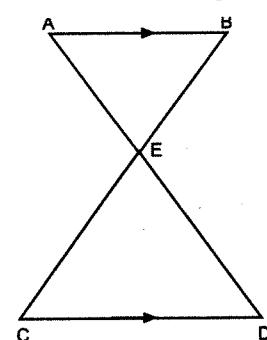


$$\triangle ADE \sim \triangle ABC \\ \frac{|AD|}{|AB|} = \frac{|DE|}{|BC|} = \frac{|AE|}{|AC|}$$



$$\frac{|AD|}{|DB|} = \frac{|AE|}{|EC|}$$

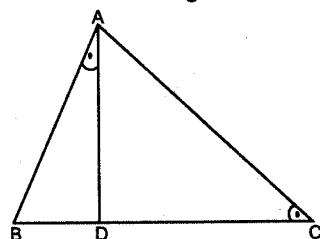
## \* Kelebek Benzerliği



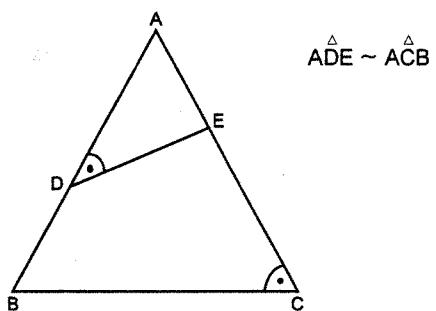
$$\triangle ABE \sim \triangle DCE$$

Bu benzerlik paralelkenar, kare, dikdörtgen ve yamukta çok sık kullanılır.

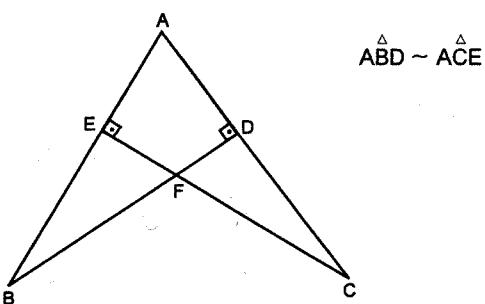
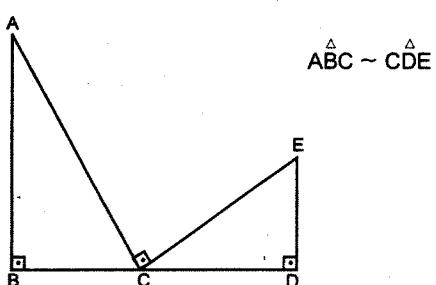
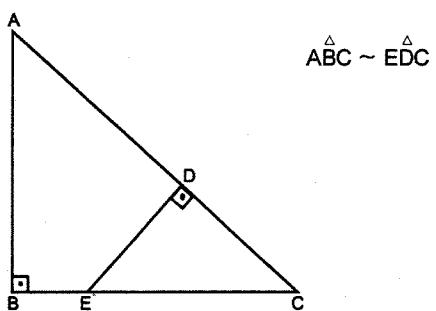
## \* Bir açısı ortak ve birer açısı aynı olan şeklärin benzerliği



$$\triangle ABC \sim \triangle DBA$$

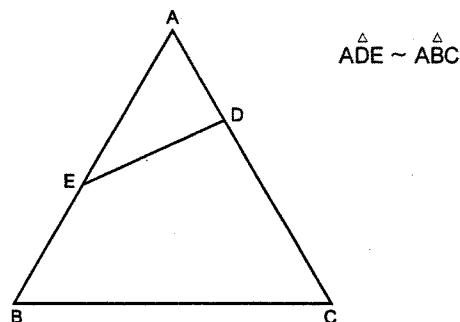


\* Şekiller içinde birden fazla doksan dereceler var ise,



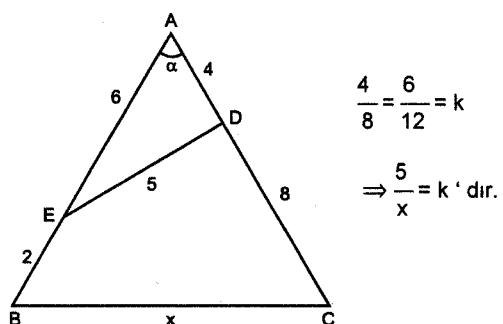
Kare, dikdörtgen gibi şekiller arasında bu benzerlik kullanılır.

#### \* Kenar - Açı - Kenar Benzerliği

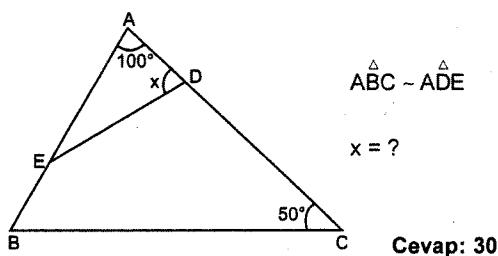


İki üçgen için ortak açının komşu kenarlarının oranına ise bu açının karşısındaki kenarların oranında aynıdır.

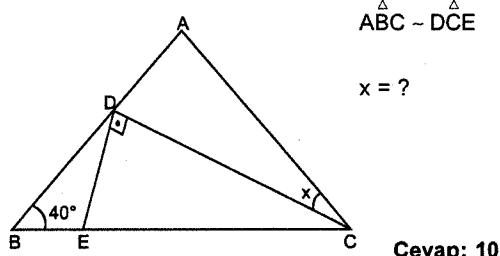
#### Örnek



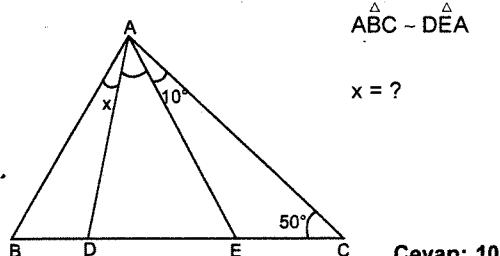
Yani iki üçgen için 4 ile çaprazındaki kenar 8, 6 ile çaprazındaki kenar 12 birbirine bölünür. Eğer eşit çıkarsa ortak açının karşısındaki kenarda bu oranın eşittir.

**1.**

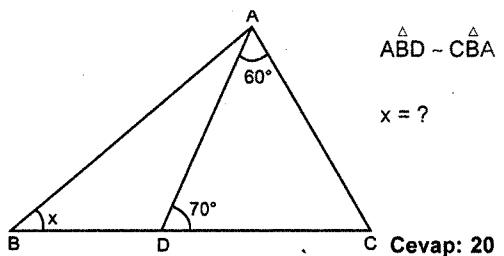
Cevap: 30

**2.**

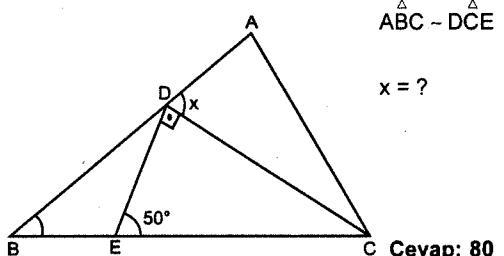
Cevap: 10

**3.**

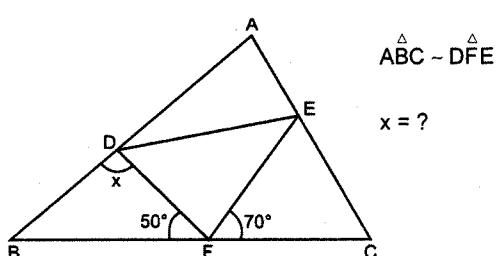
Cevap: 10

**4.**

Cevap: 20

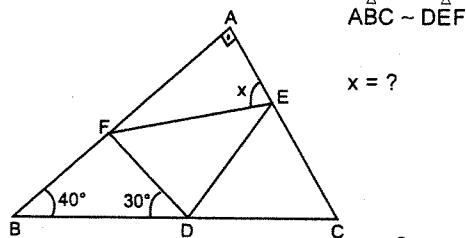
**5.**

Cevap: 80

**6.**

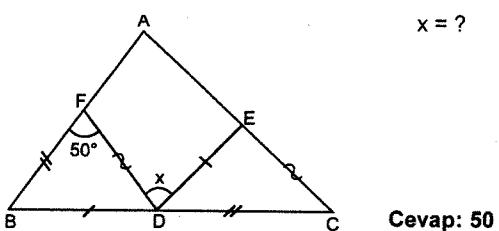
Cevap: 70

7.



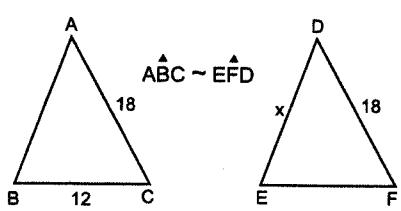
Cevap: 70

8.



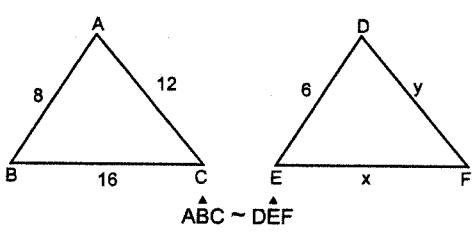
Cevap: 50

9.

 $x = ?$ 

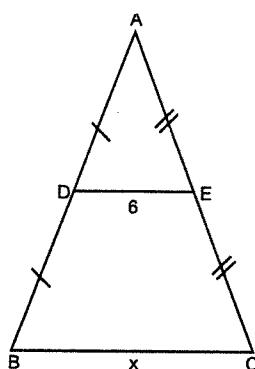
Cevap: 27

10.



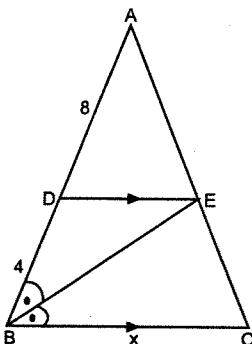
Cevap: 21

11.



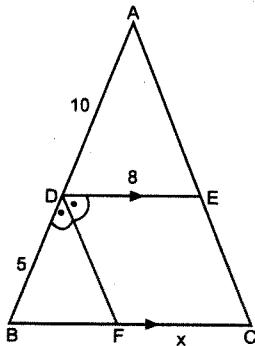
Cevap: 12

12.



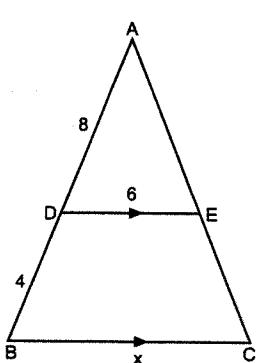
Cevap: 6

13.



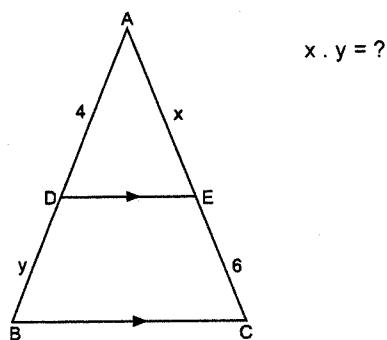
Cevap: 7

14.



Cevap: 9

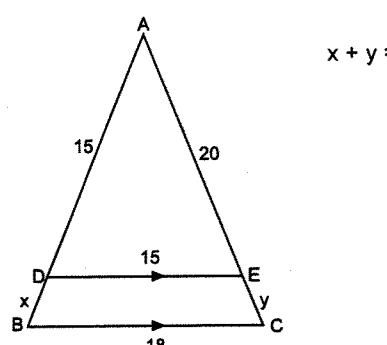
15.



$$x \cdot y = ?$$

Cevap: 24

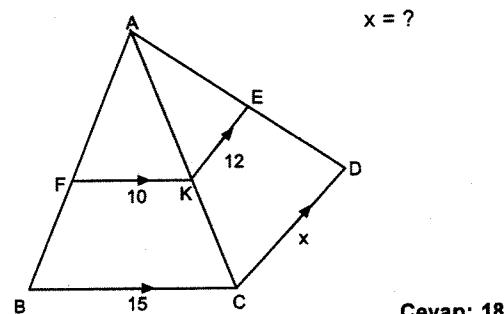
16.



$$x + y = ?$$

Cevap: 7

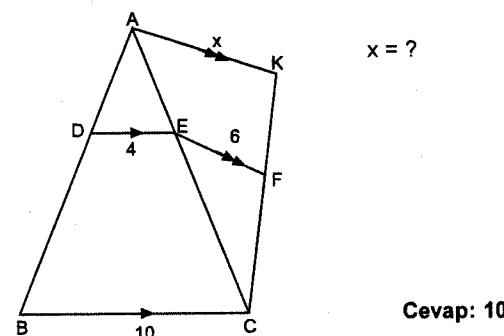
17.



$$x = ?$$

Cevap: 18

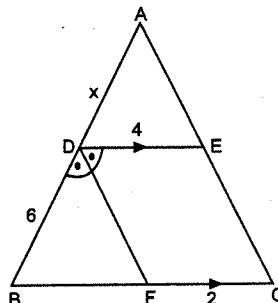
18.



$$x = ?$$

Cevap: 10

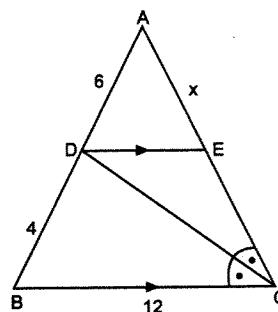
19.



$$x = ?$$

Cevap: 6

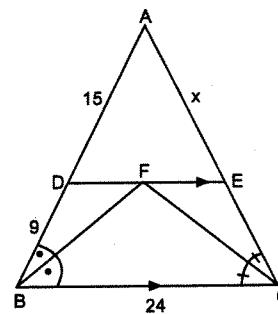
20.



$$x = ?$$

Cevap: 10,8

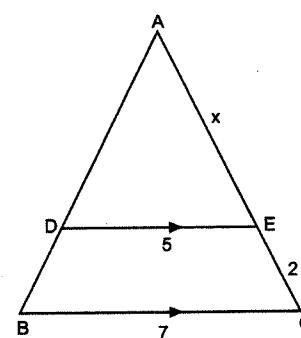
21.



$$x = ?$$

Cevap: 10

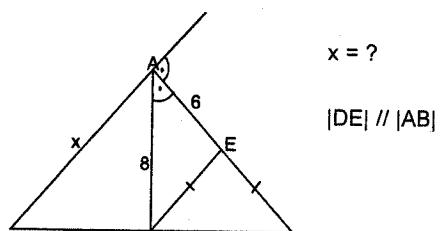
22.



$$x = ?$$

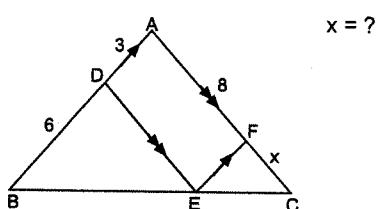
Cevap: 5

23.



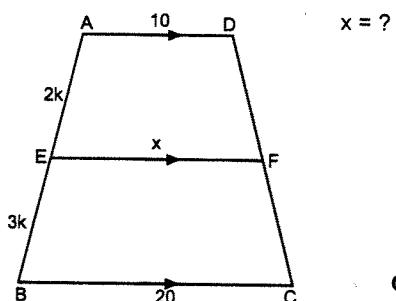
Cevap: 14

24.



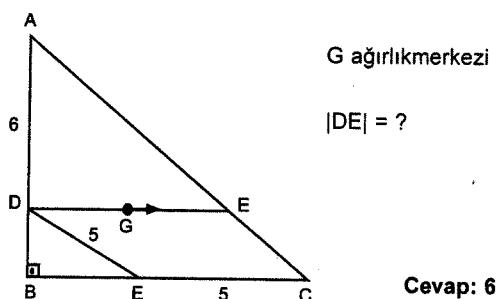
Cevap: 4

25.



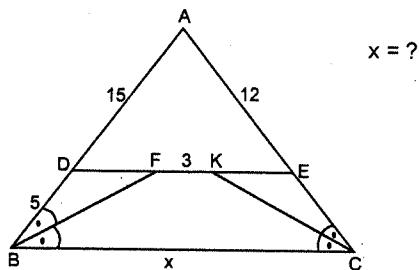
Cevap: 14

26.



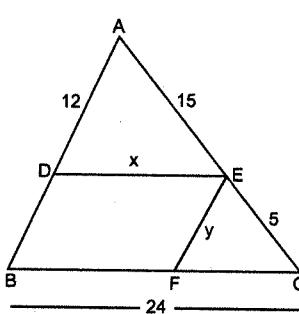
Cevap: 6

27.



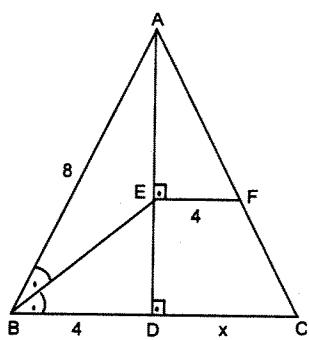
Cevap: 16

28.



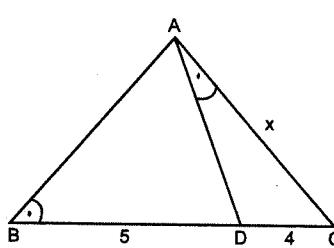
Cevap: 14

29.



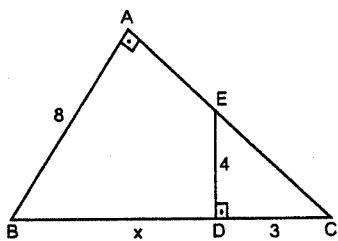
Cevap: 6

30.



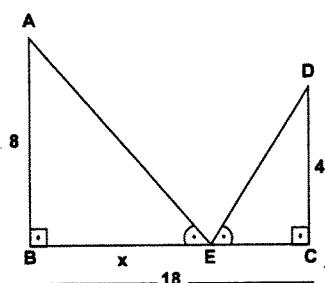
Cevap: 6

31.

 $x = ?$ 

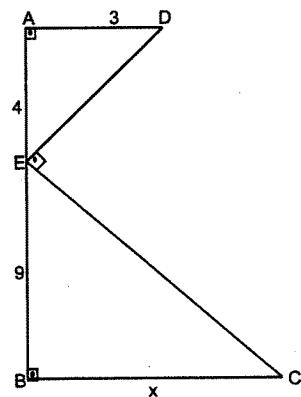
Cevap: 7

32.

 $x = ?$ 

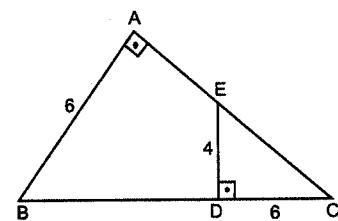
Cevap: 12

33.

 $x = ?$ 

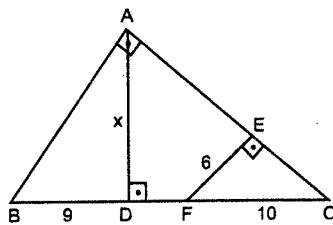
Cevap: 12

34.

 $|AC| = ?$ 

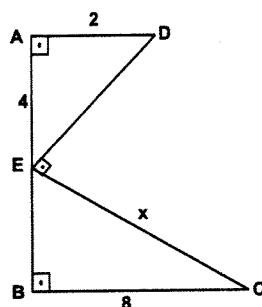
Cevap: 9

35.

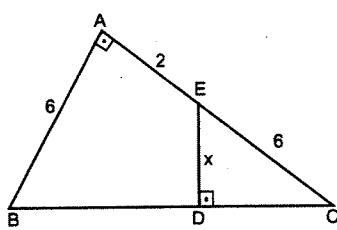
 $x = ?$ 

Cevap: 12

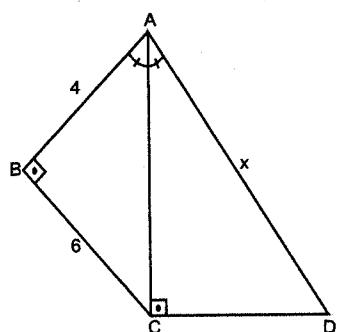
36.

 $x = ?$ Cevap:  $4\sqrt{5}$ 

37.

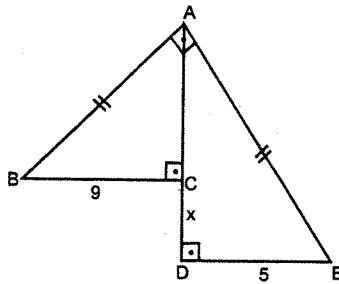
 $x = ?$ Cevap:  $\frac{18}{5}$ 

38.

 $x = ?$ 

Cevap: 13

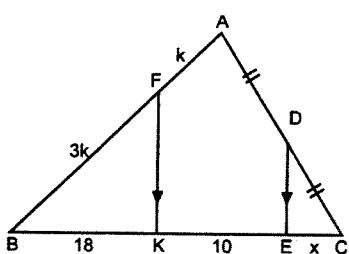
39.



$x = ?$

Cevap: 4

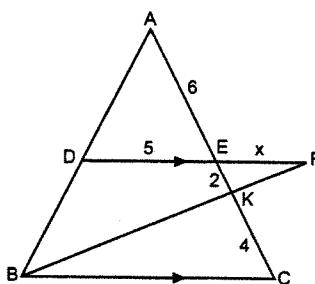
40.



$x = ?$

Cevap: 4

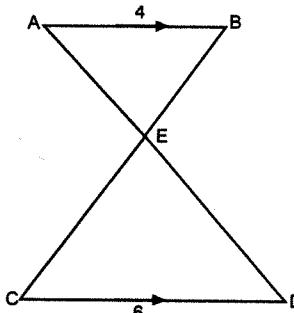
43.



$x = ?$

Cevap: 5

44.



$x = ?$

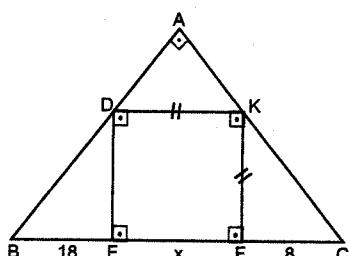
$|BC| = 10$

$|AD| = 15$

$\triangle CED \sim ?$

Cevap: 21

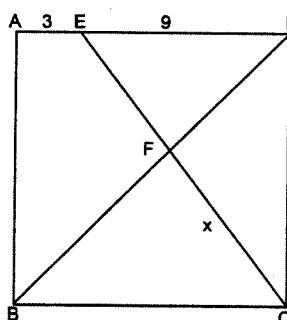
41.



$x = ?$

Cevap: 12

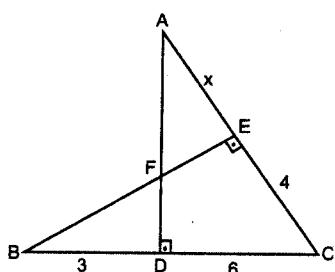
45.



ABCD kare

$\frac{60}{7}$

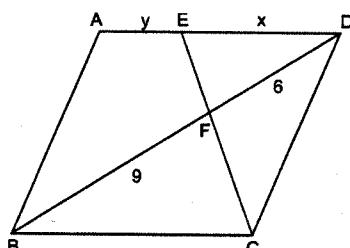
42.



$x = ?$

Cevap:  $\frac{19}{2}$ 

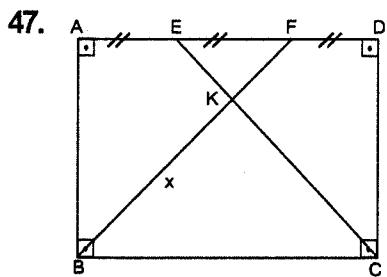
46.



Paralelkenar

$\frac{x}{y} = ?$

Cevap: 2

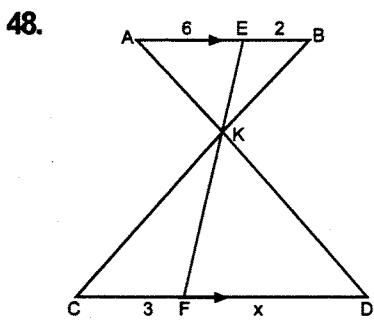


ABCD  
dikdörtgen

$$|BF| = 20$$

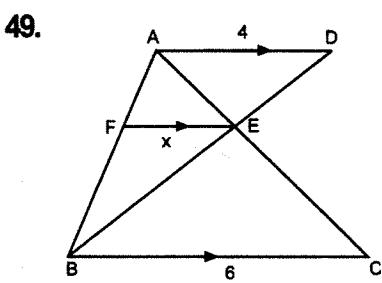
$$x = ?$$

Cevap: 15



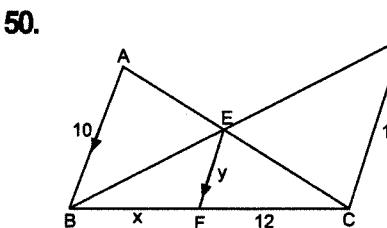
$$x = ?$$

Cevap: 9



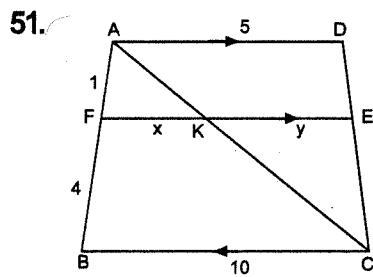
$$x = ?$$

Cevap:  $\frac{12}{5}$



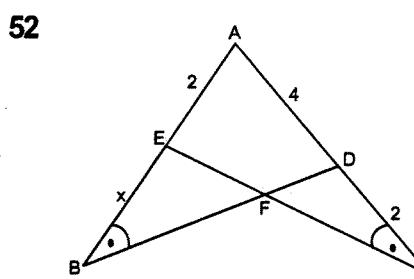
$$x + y = ?$$

Cevap: 14



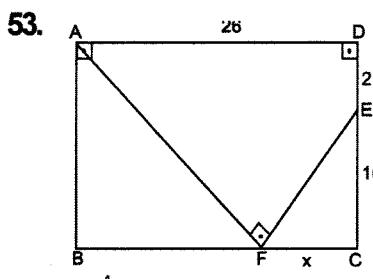
$$x \cdot y = ?$$

Cevap: 8



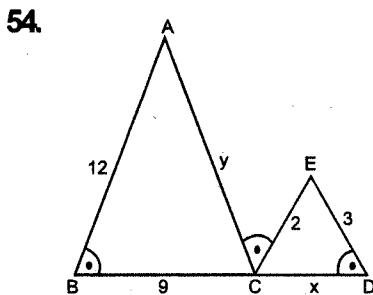
$$x = ?$$

Cevap: 10



ABCD  
dikdörtgen  
 $|BF| < |FC|$   
 $x = ?$

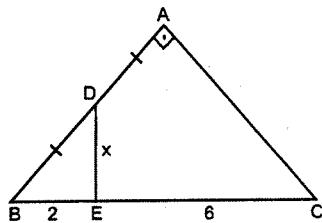
Cevap: 6



$$x + y = ?$$

Cevap: 10

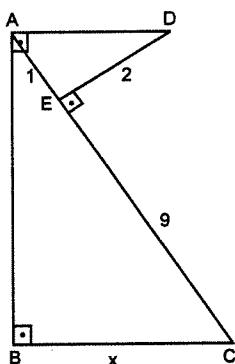
55.



$x = ?$

Cevap: 2

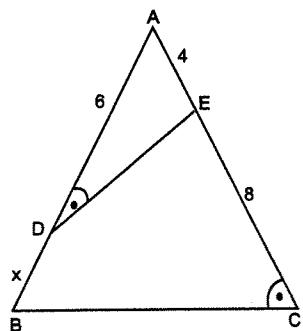
56.



$x = ?$

Cevap:  $2\sqrt{5}$ 

57.



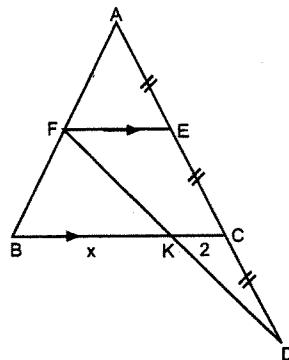
$x = ?$

Cevap: 2

$x = ?$

Cevap: 15

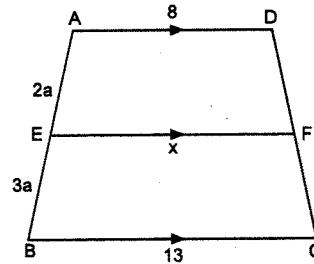
59.



$x = ?$

Cevap: 6

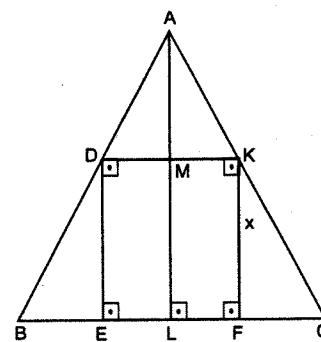
60.



$x = ?$

Cevap: 10

61.



DEFK kare

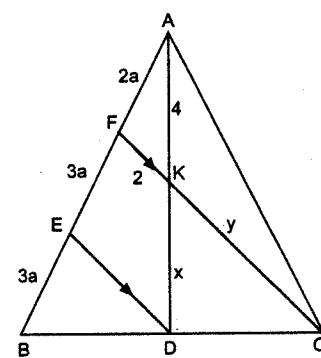
$|AL| = 15$

$|BC| = 20$

$x = ?$

Cevap:  $\frac{60}{7}$ 

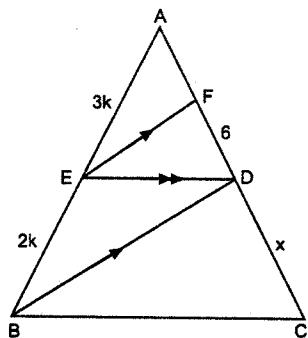
62.



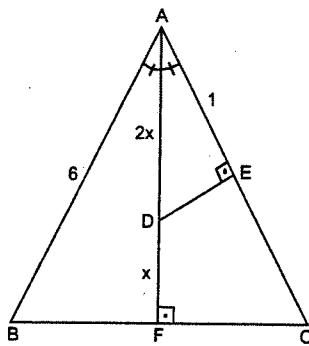
$y - x = ?$

Cevap: 2

63.

 $x = ?$ 

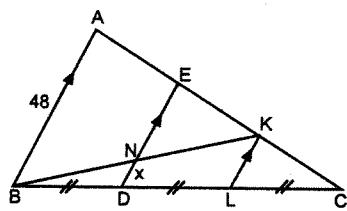
67.

 $x = ?$ 

Cevap: 10

Cevap: 1

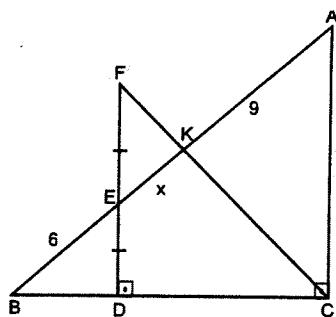
64.

 $x = ?$ 

Cevap: 8

G, ağırlık  
merkezi $x = ?$ 

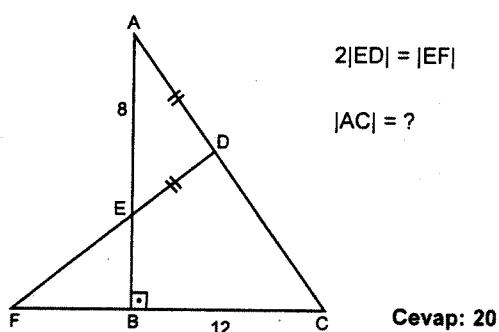
65.

 $x = ?$ 

Cevap: 3

Cevap:  $\frac{34}{3}$ 

66.

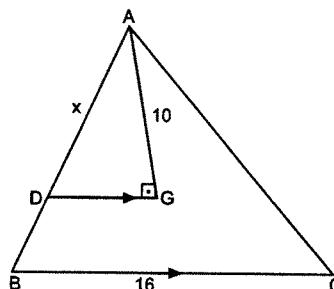


$$2|ED| = |EF|$$

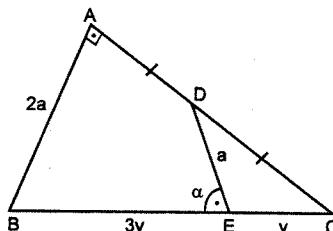
$$|AC| = ?$$

Cevap: 20

68.

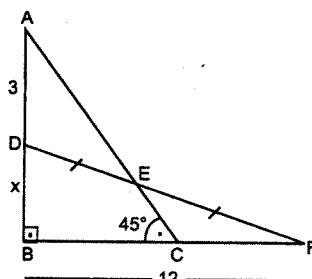
 $\alpha = ?$ 

69.



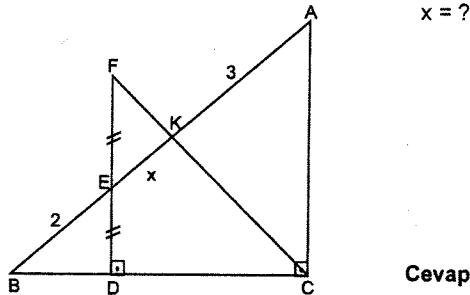
Cevap: 60

70.

 $x = ?$ 

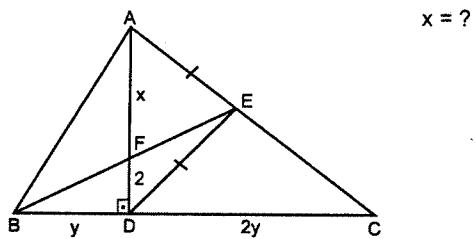
Cevap: 6

71.



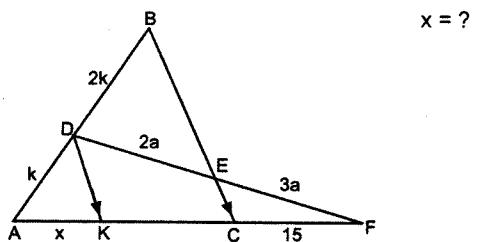
Cevap: 1

72.



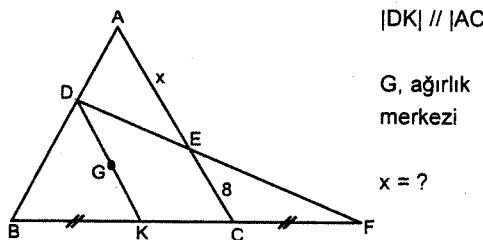
Cevap: 6

73.



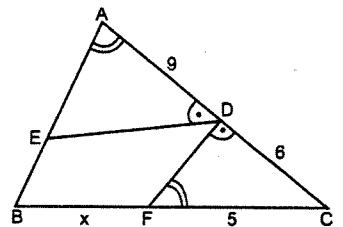
Cevap: 5

74.



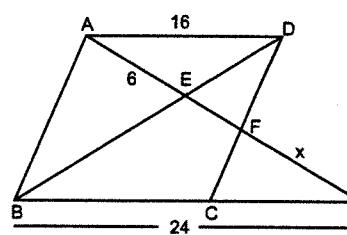
Cevap: 10

75.



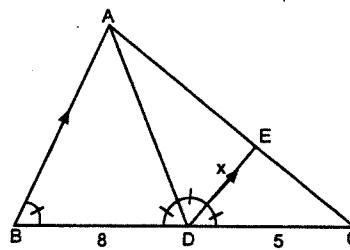
Cevap: 13

76.

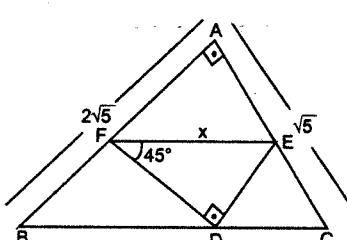


Cevap: 5

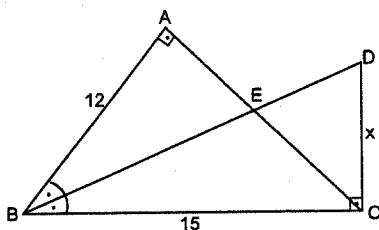
77.

Cevap:  $\frac{40}{13}$ 

78.

Cevap:  $\frac{20}{9}$

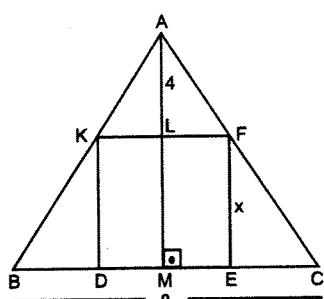
79.



$x = ?$

Cevap: 5

80.

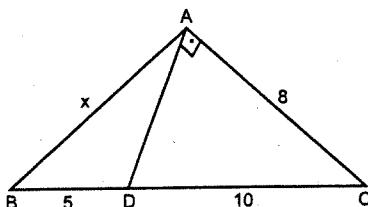


DEFLK kare

$x = ?$

Cevap: 4

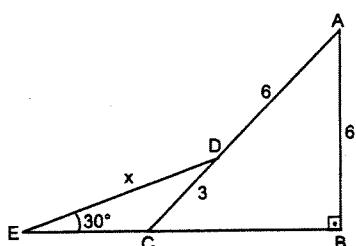
83.



$x = ?$

Cevap:  $\sqrt{97}$ 

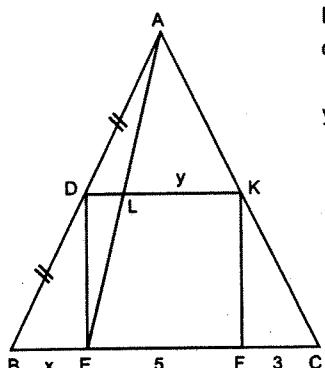
84.



$x = ?$

Cevap: 4

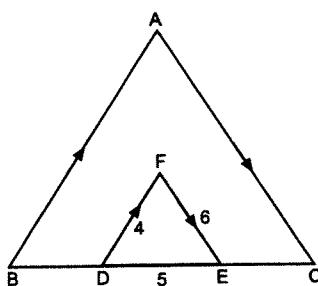
81.

DEFK  
dikdörtgen

$y - x = ?$

Cevap: 2

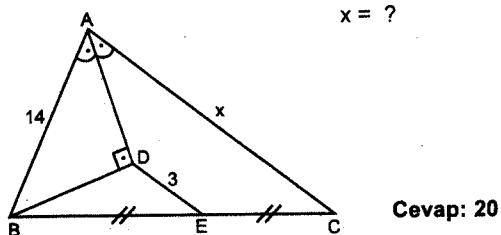
85.

F iç açıortaylarının  
kesim noktası,

$\triangle \text{C}(ABC) = ?$

Cevap: 45

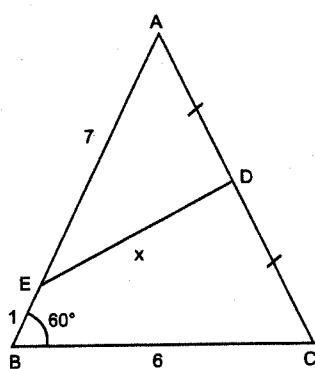
82.



$x = ?$

Cevap: 20

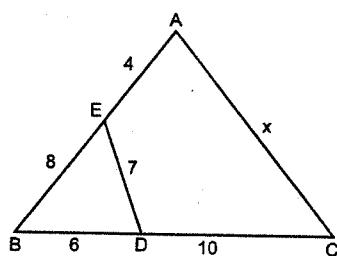
86.



$x = ?$

Cevap:  $3\sqrt{3}$

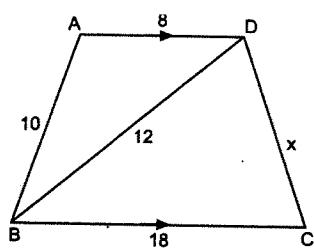
87.



$x = ?$

Cevap: 14

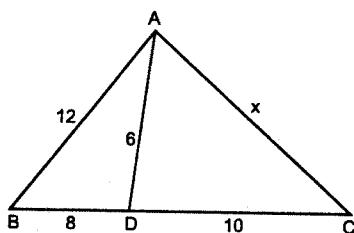
88.



$x = ?$

Cevap: 15

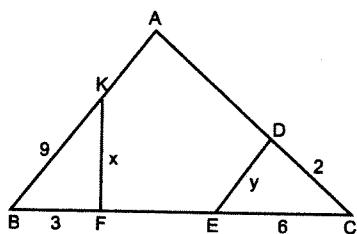
89.



$x = ?$

Cevap: 9

90.

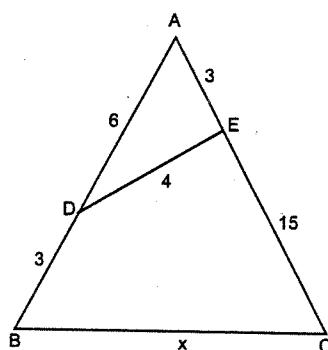


$|AB| = |AC|$

$\frac{x}{y} = ?$

Cevap:  $\frac{3}{2}$ 

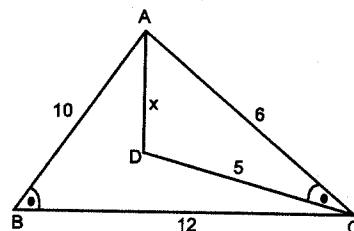
91.



$x = ?$

Cevap: 12

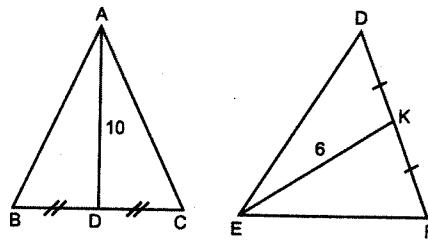
92.



$x = ?$

Cevap: 3

93.

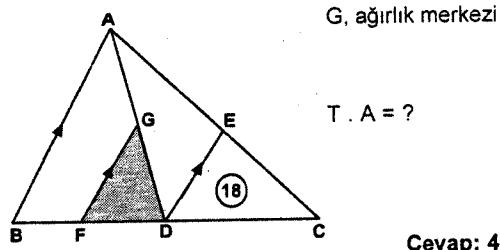


$ABC \sim EDF \Rightarrow$

$\frac{A(\triangle ABC)}{A(\triangle DEF)} = ?$

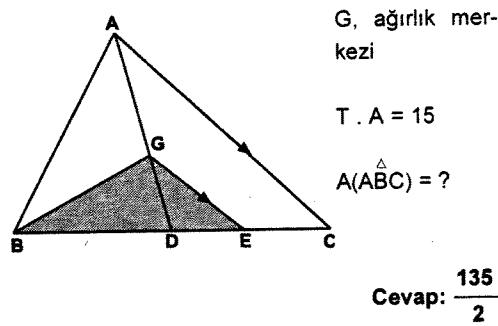
Cevap:  $\frac{25}{9}$

94.

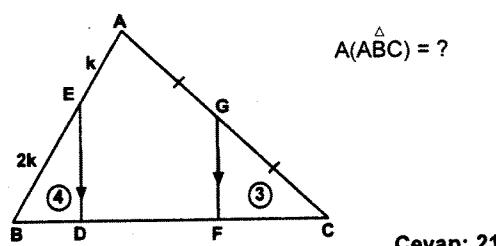


Cevap: 4

95.

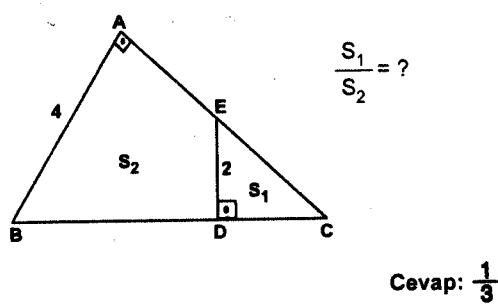
Cevap:  $\frac{135}{2}$ 

96.

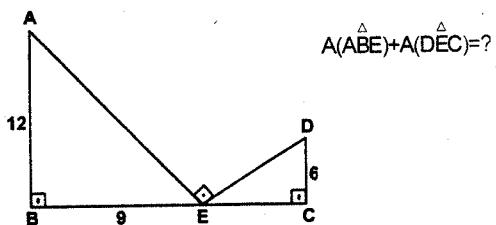


Cevap: 21

97.

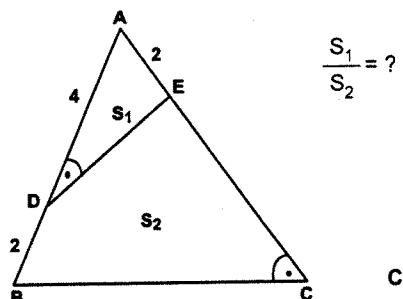
Cevap:  $\frac{1}{3}$ 

98.

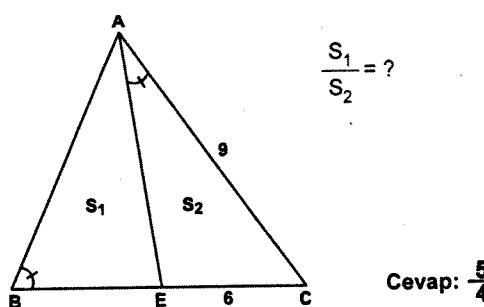


Cevap: 78

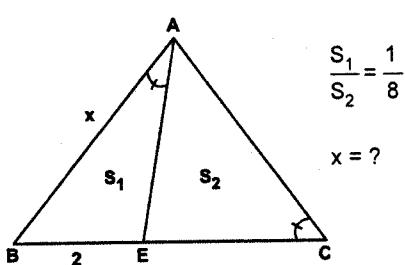
99.

Cevap:  $\frac{1}{8}$ 

100.

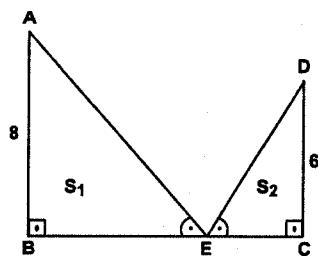
Cevap:  $\frac{5}{4}$ 

101.



Cevap: 6

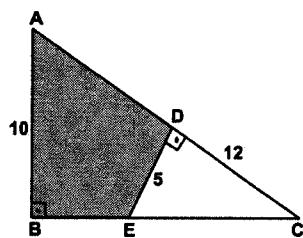
102.



$$\frac{S_1}{S_2} = ?$$

Cevap:  $\frac{16}{9}$

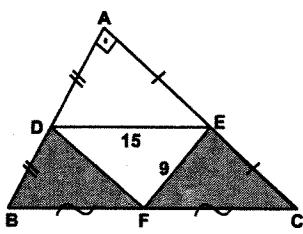
103.



$$T \cdot A = ?$$

Cevap: 90

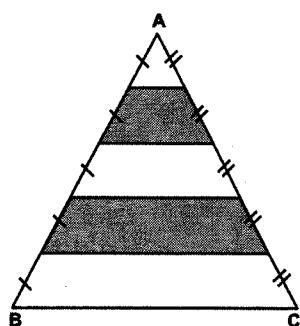
104.



$$T \cdot A = ?$$

Cevap: 108

105.

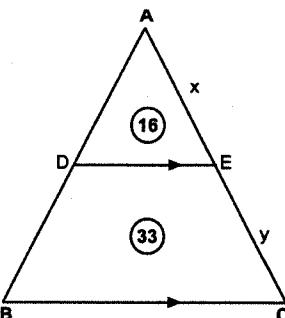


$$T \cdot A = 15 \text{ br}$$

$$\text{Alan}(\triangle ABC) = ?$$

Cevap:  $\frac{75}{2}$

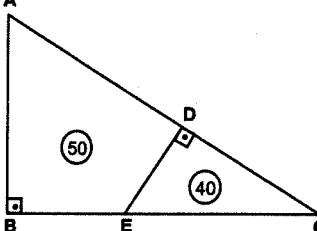
106.



$$\frac{x}{y} = ?$$

Cevap:  $\frac{4}{3}$

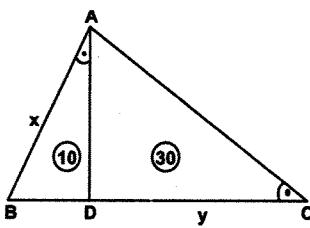
107.



$$\frac{|AB|}{|DE|} = ?$$

Cevap:  $\frac{3}{2}$

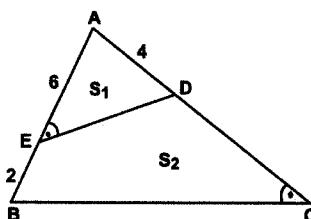
108.



$$\frac{x}{y} = ?$$

Cevap:  $\frac{2}{3}$

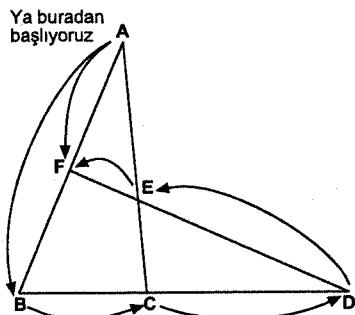
109.



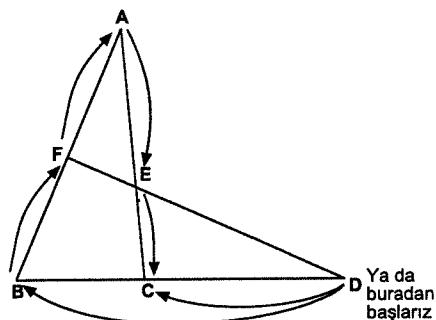
$$\frac{S_1}{S_2} = ?$$

Cevap:  $\frac{1}{3}$

## Meneleus Teoremi

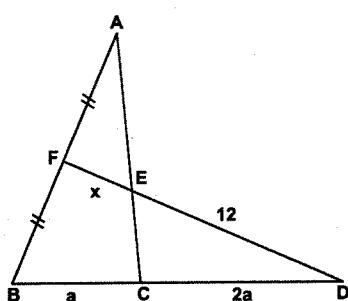


$$\frac{|AF|}{|AB|} \cdot \frac{|BC|}{|CD|} \cdot \frac{|DE|}{|EF|} = 1$$



$$\frac{|DC|}{|DB|} \cdot \frac{|BF|}{|AF|} \cdot \frac{|AE|}{|EC|} = 1$$

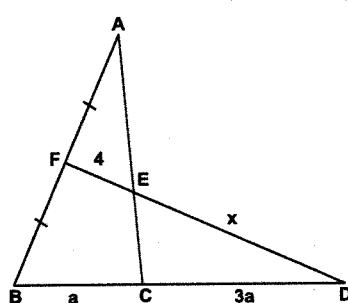
110.



$$x = ?$$

Cevap: 3

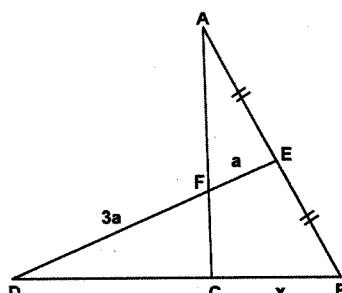
111.



$$x = ?$$

Cevap: 24

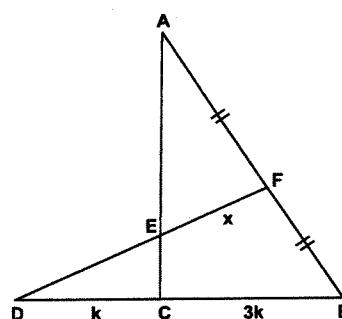
113.



$$|BD| = 15$$

Cevap: 6

114.

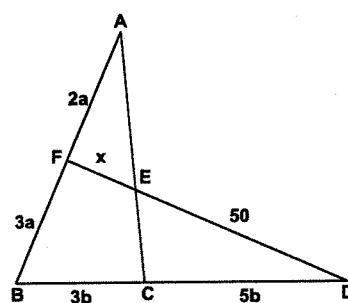


$$|FD| = 20$$

$$x = ?$$

Cevap: 12

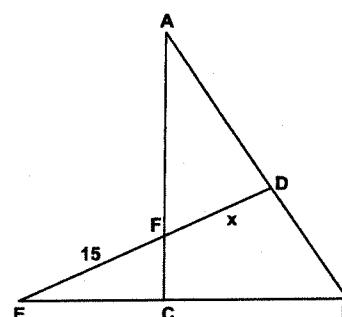
112.



$$x = ?$$

Cevap: 12

115.

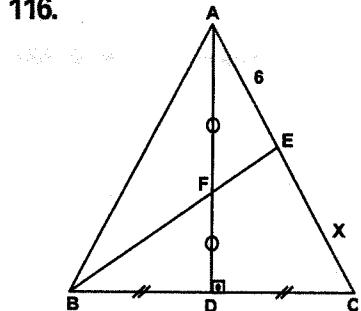


$$\begin{aligned} |AD| &= 4|DB| \\ 2|EC| &= 3|BC| \\ |EF| &= 15 \text{ cm} \end{aligned}$$

$$x = ?$$

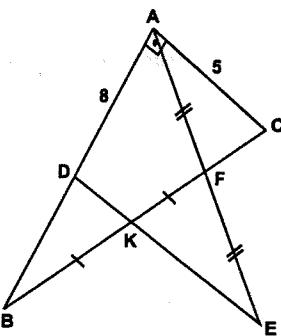
Cevap: 8

116.



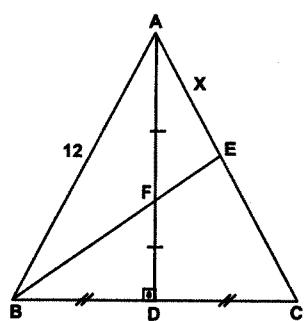
$x = ?$

120.



$|BC| = ?$

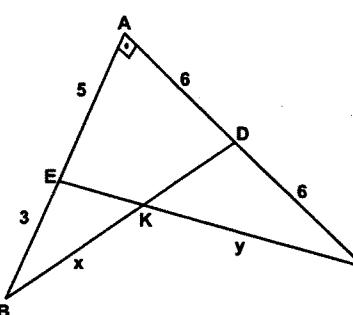
117.



$x = ?$

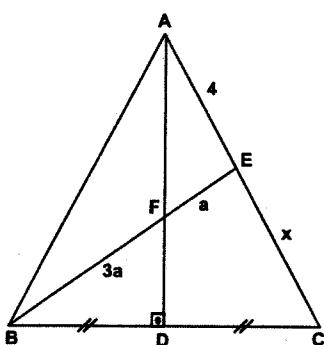
Cevap: 12

121.



$\frac{x}{y} = ?$

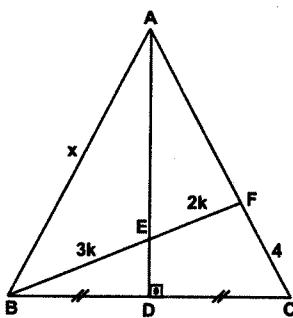
118.



$x = ?$

Cevap: 8

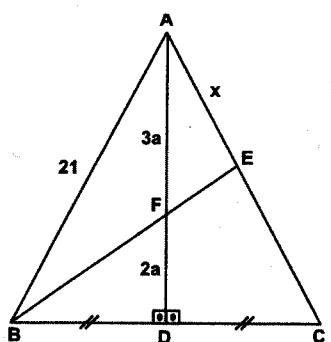
122.



$x = ?$

Cevap: 12

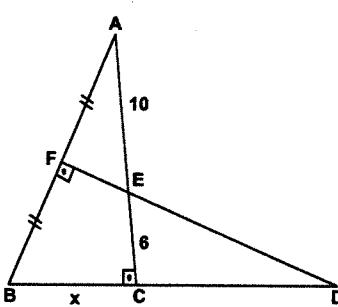
119.



$x = ?$

Cevap: 9

123.



$x = ?$

Cevap: 8

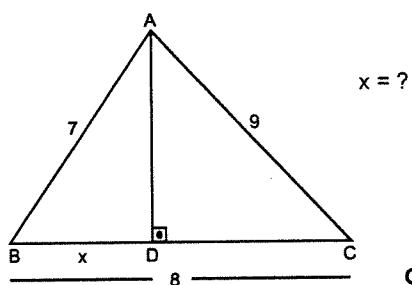
## ÜÇGENLER

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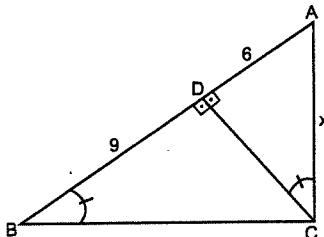
**1.**



$$x = ?$$

Cevap: 2

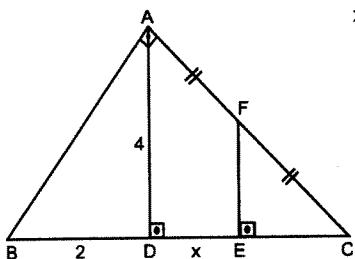
**4.**



$$x = ?$$

Cevap:  $3\sqrt{10}$

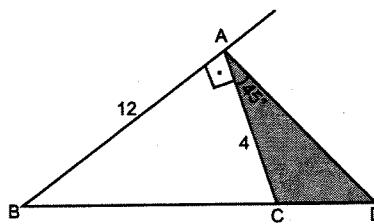
**2.**



$$x = ?$$

Cevap: 4

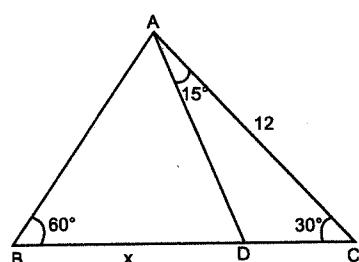
**5.**



$$T \cdot A = ?$$

Cevap: 12

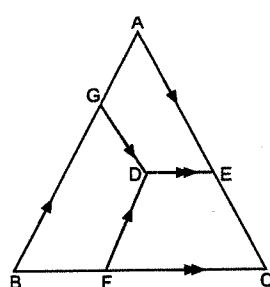
**3.**



$$x = ?$$

Cevap:  $2\sqrt{3} + 6$

**6.**



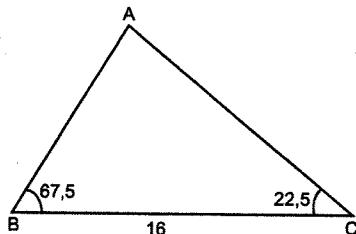
ABC eşkenar üçgen

$$2 \cdot \mathcal{C}(\triangle ABC) = A(\triangle ABC)$$

$$|GD| + |DE| + |DF| = ?$$

Cevap:  $8\sqrt{3}$

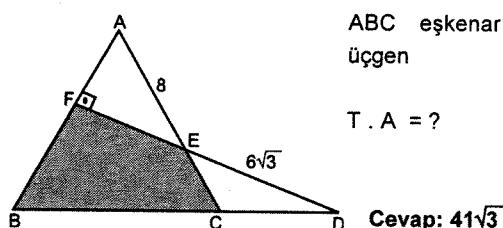
7.



$$A(\triangle ABC) = ?$$

Cevap:  $32\sqrt{2}$

8.

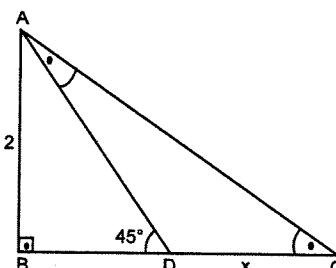


ABC eşkenar üçgen

$$T.A = ?$$

Cevap:  $41\sqrt{3}$

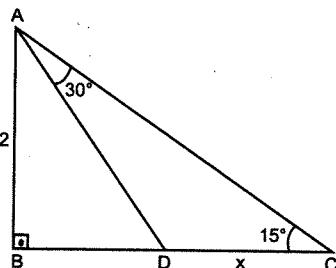
11.



$$x = ?$$

Cevap:  $2\sqrt{2}$

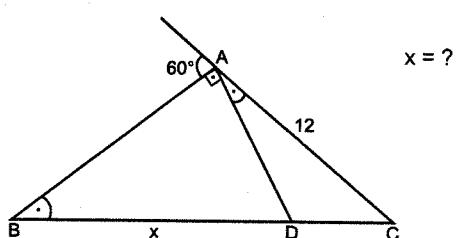
12.



$$x = ?$$

Cevap:  $2\sqrt{3} + 2$

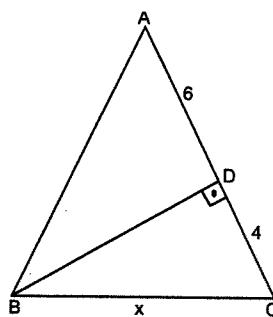
9.



$$x = ?$$

Cevap:  $8\sqrt{3}$

13.

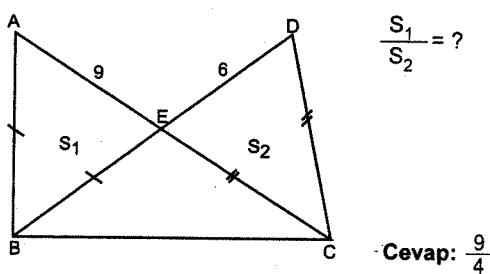


$$x = ?$$

$|AB| = |AC|$

Cevap:  $4\sqrt{5}$

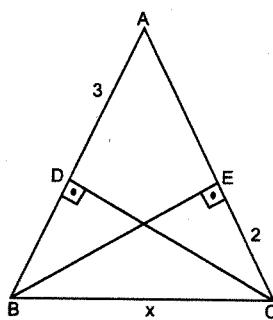
10.



$$\frac{S_1}{S_2} = ?$$

Cevap:  $\frac{9}{4}$

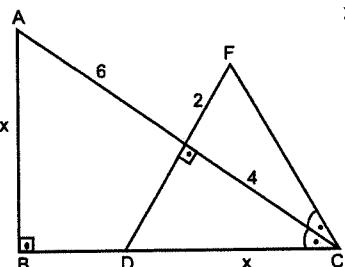
14.



$|DC| = |BE|$

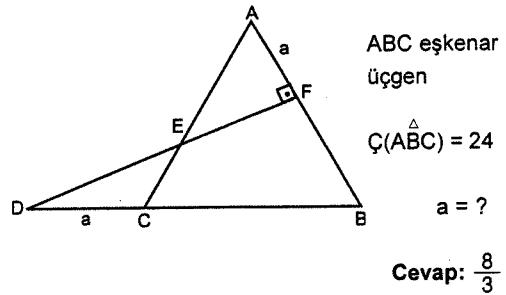
$$x = ?$$

Cevap:  $2\sqrt{5}$

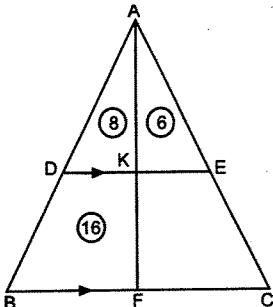
15.   $x = ?$

Cevap:  $2\sqrt{5}$

19.

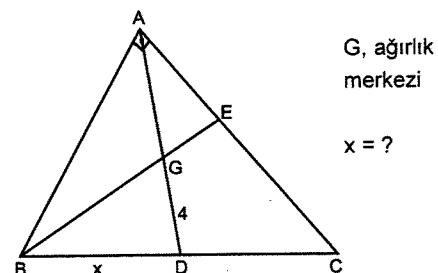


Cevap:  $\frac{8}{3}$

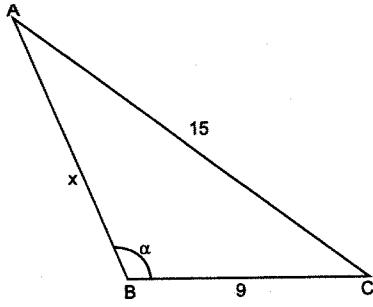
16.   $A(\triangle ABC) = ?$

Cevap: 42

20.

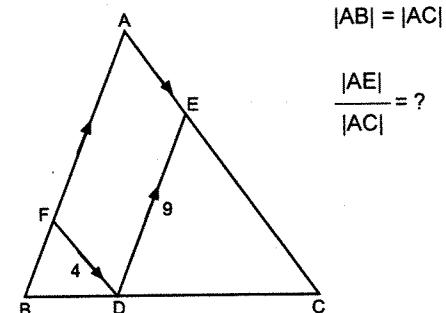


Cevap: 12

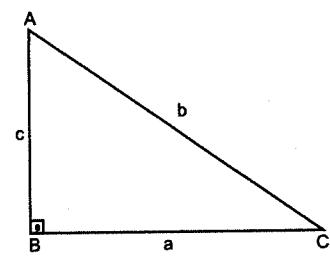
17.   $\alpha > 90^\circ$   
 $x$  in kaç tamsayı değeri vardır?

Cevap: 5

21.

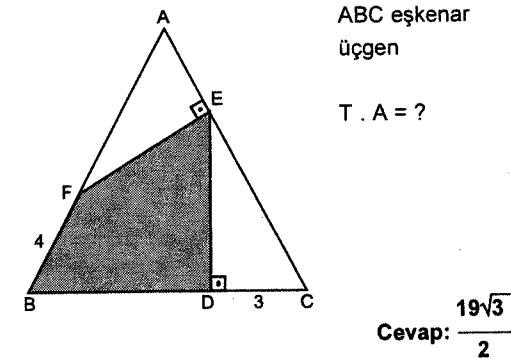


Cevap:  $\frac{4}{13}$

18.   $A(\triangle ABC) = 20$   
 $(a-b+c)(a+c+b) = ?$

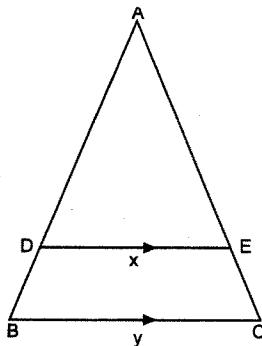
Cevap: 80

22.



Cevap:  $\frac{19\sqrt{3}}{2}$

23.

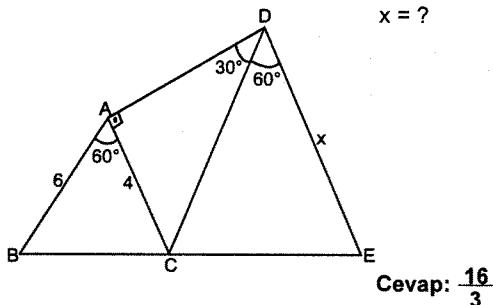


$$3x^2 + xy - 2y^2 = 0$$

$$\frac{A(\triangle ADE)}{A(\triangle ABC)} = ?$$

$$\text{Cevap: } \frac{4}{9}$$

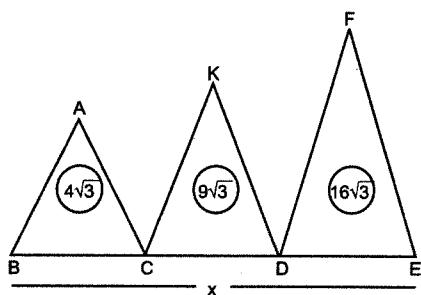
24.



$$x = ?$$

$$\text{Cevap: } \frac{16}{3}$$

25.

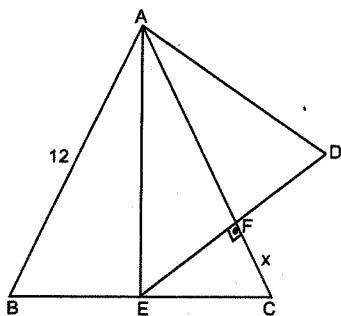


Şekiller eşkanar üçgendir.

$$x = ?$$

$$\text{Cevap: } 18$$

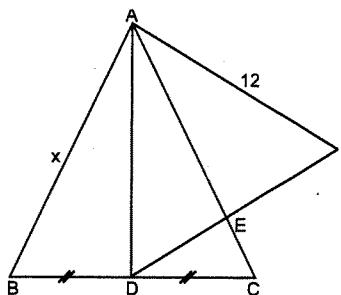
26.



ABC ve AED  
eşkenar üçgenler  
 $x = ?$

$$\text{Cevap: } 3$$

27.

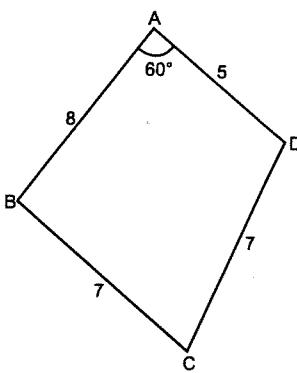


ABC ve DAF  
eşkenar üçgen

$$x = ?$$

$$\text{Cevap: } 8\sqrt{3}$$

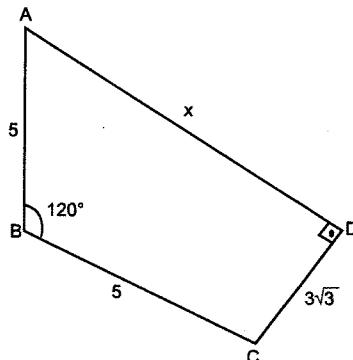
28.



$$A(ABCD) = ?$$

$$\text{Cevap: } \frac{89\sqrt{3}}{4}$$

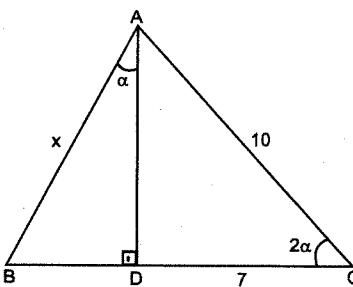
29.



$$x = ?$$

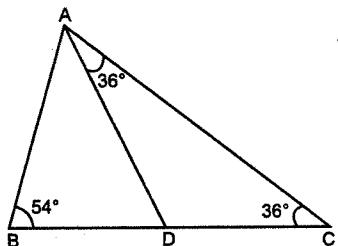
$$\text{Cevap: } 4\sqrt{3}$$

30.



$$x = ?$$

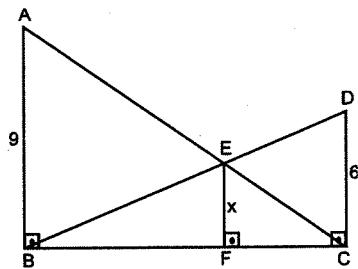
$$\text{Cevap: } 2\sqrt{15}$$

**31.**

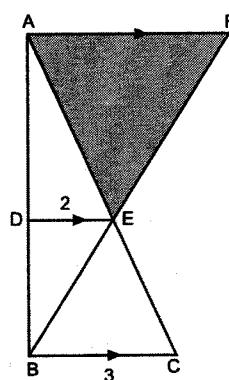
Hangisi yanlıştır?

- A)  $|AD| = |DC|$     B)  $|BD| = |DC|$     C)  $|AD| = |BD|$   
 D)  $|AB| > |DC|$     E)  $|BD| > |AB|$

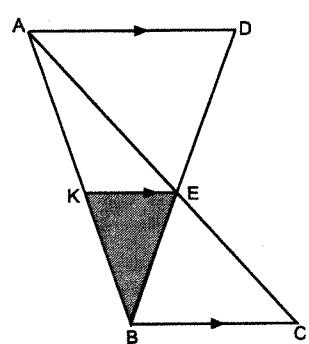
Cevap: E

**32.** $x = ?$ 

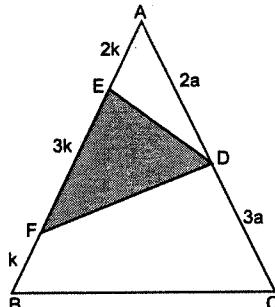
Cevap: 3,6

**33.** $T \cdot A = 12$  $A(\triangle BEC) = ?$ 

Cevap: 3

**34.**

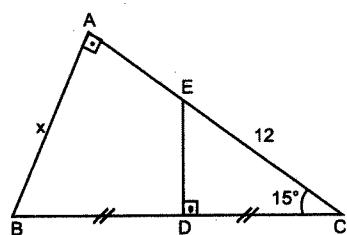
$$\frac{|AE|}{|EC|} = \frac{2}{3}$$

 $T \cdot A = 12$  $A(\triangle AED) = ?$ Cevap:  $\frac{40}{3}$ **35.**

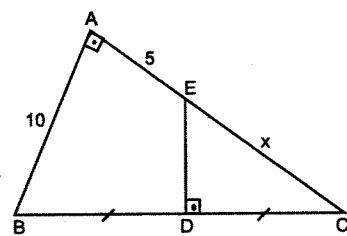
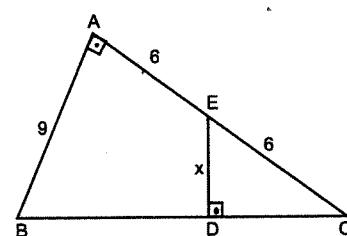
$T \cdot A = 15$

 $A(\triangle ABC) = ?$ 

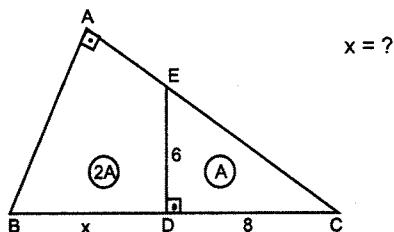
Cevap: 75

**36.** $x = ?$ 

Cevap: 6

**37.** $x = ?$ Cevap:  $5\sqrt{5}$ **38.** $x = ?$ Cevap:  $\frac{18}{5}$

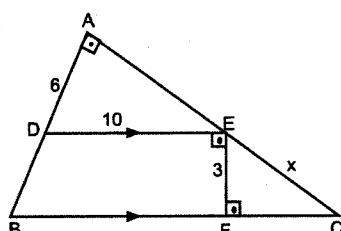
39.



$x = ?$

Cevap:  $10\sqrt{3} - 8$ 

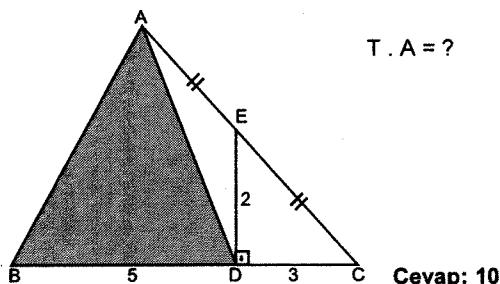
40.



$x = ?$

Cevap: 5

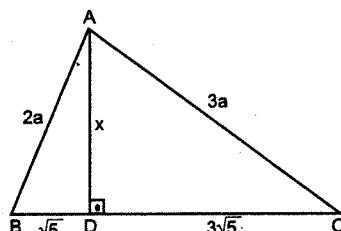
41.



$T.A = ?$

Cevap: 10

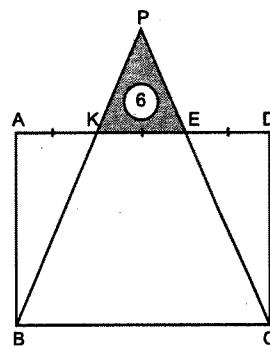
42.



$x = ?$

Cevap:  $3\sqrt{3}$ 

43.

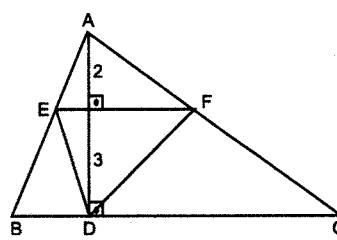


$T.A = 6$

ABCD  
dikdörtgenin  
alanı?

Cevap: 72

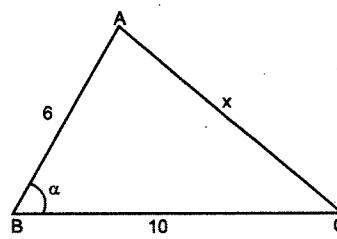
44.



$\frac{A(AEDF)}{A(ABC)} = ?$

Cevap:  $\frac{2}{5}$ 

45.

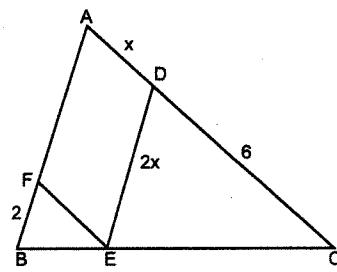


$\alpha > 60^\circ$

x in en küçük  
tamsayı değeri  
kaçtır?

Cevap: 9

46.

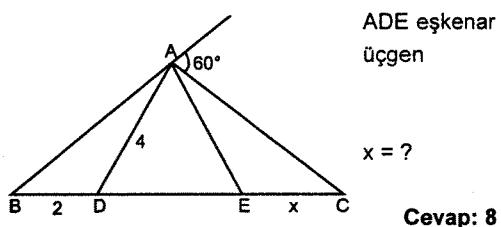
AFED  
paralelkenar

$x = ?$

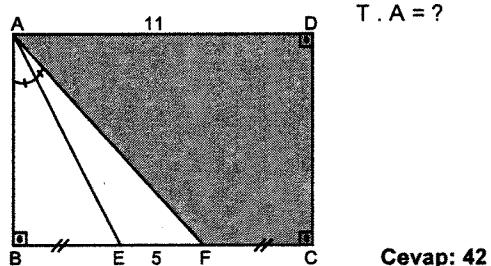
Cevap:  $\sqrt{6}$

- 47.** Bir üçgenin kenar uzunluklarının ikişer ikişer toplamları 7, 8, 9 sayıları ile orantılıdır.  
Bu üçgenin alanı  $54 \text{ cm}^2$  ise çevresi kaç cm dir?

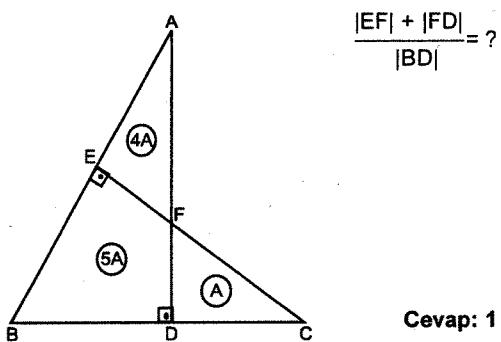
Cevap: 36

**48.**

Cevap: 8

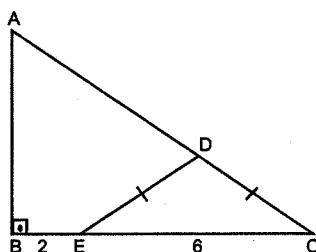
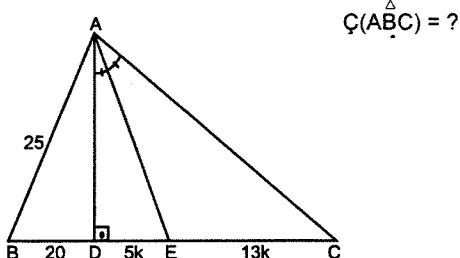
**49.**

Cevap: 42

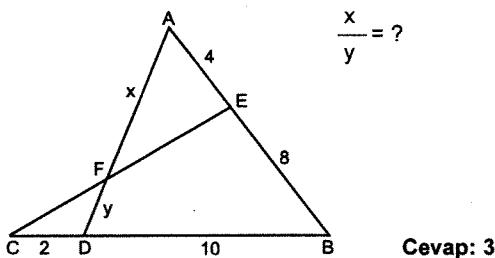
**50.**

Cevap: 1

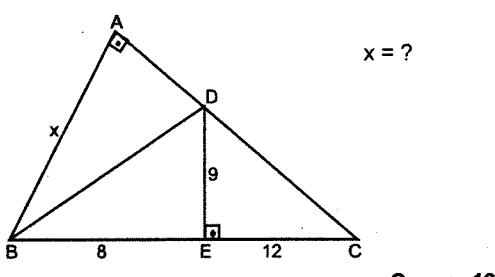
- 51.**  $\frac{|AD|}{|DC|} = ?$

Cevap:  $\frac{5}{3}$ **52.**

Cevap: 120

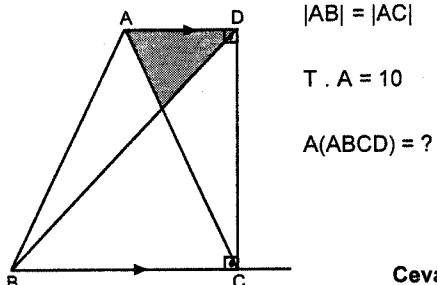
**53.**

Cevap: 3

**54.**

Cevap: 12

55.



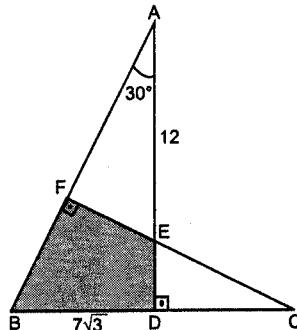
$$|AB| = |AC|$$

$$T \cdot A = 10$$

$$A(ABCD) = ?$$

Cevap: 90

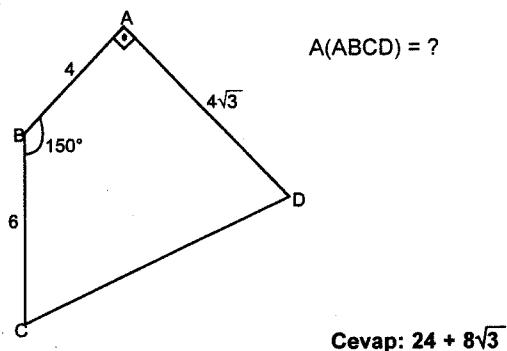
59.



$$T \cdot A = ?$$

$$\text{Cevap: } \frac{111\sqrt{3}}{2}$$

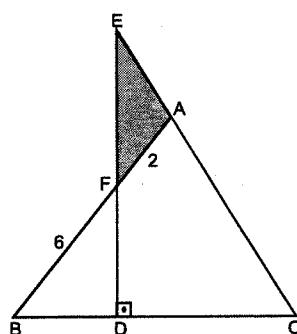
56.



$$A(ABCD) = ?$$

Cevap:  $24 + 8\sqrt{3}$ 

60.

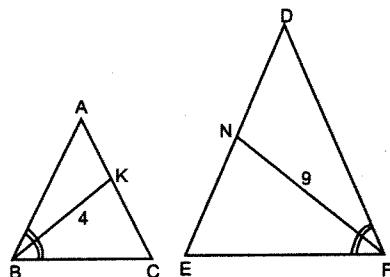


$$\frac{T \cdot A}{A(ABC)} = ?$$

$$|AB| = |AC|$$

$$\text{Cevap: } \frac{1}{16}$$

57.

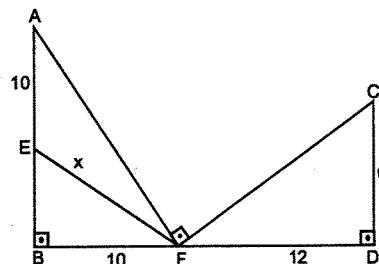


$$\triangle ABC \sim \triangle DFE$$

$$\frac{A(\triangle ABC)}{A(\triangle DFE)} = ?$$

$$\text{Cevap: } \frac{16}{81}$$

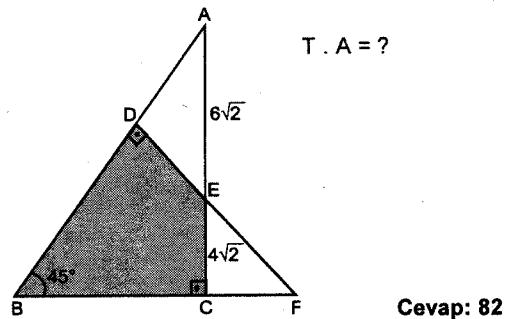
61.



$$x = ?$$

$$\text{Cevap: } 10\sqrt{2}$$

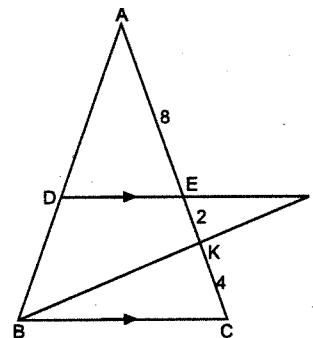
58.



$$T \cdot A = ?$$

Cevap: 82

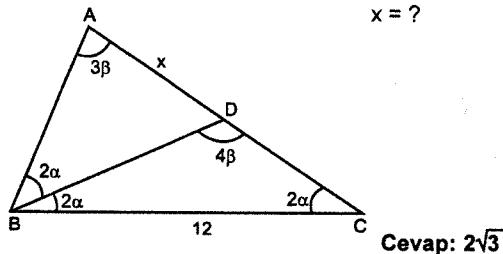
62.



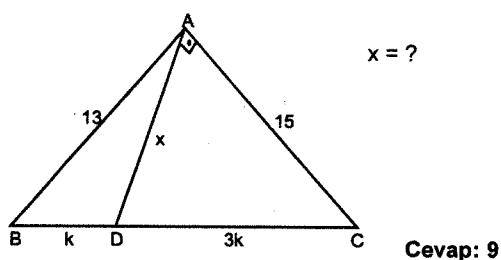
$$\frac{|DE|}{|EF|} = ?$$

$$\text{Cevap: } \frac{8}{7}$$

63.

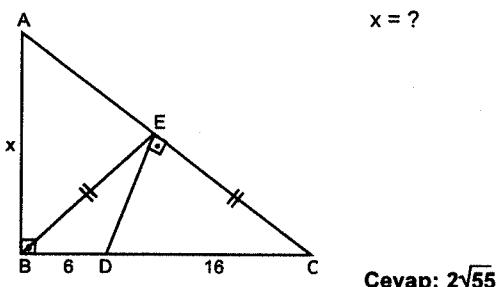
Cevap:  $2\sqrt{3}$ 

64.

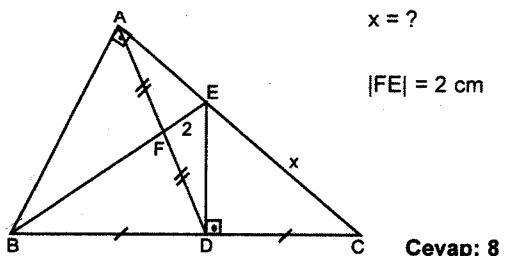


Cevap: 9

65.

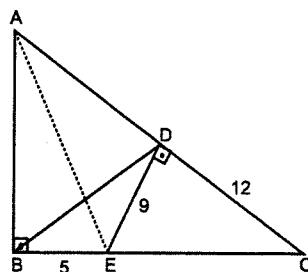
Cevap:  $2\sqrt{55}$ 

66.



Cevap: 8

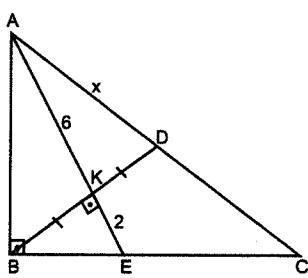
67.



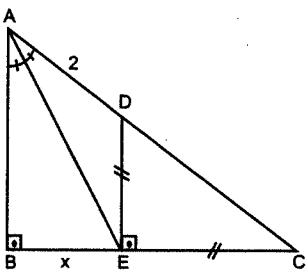
$$\frac{|AE|}{|AD|} = ?$$

Cevap:  $\frac{5\sqrt{10}}{13}$ 

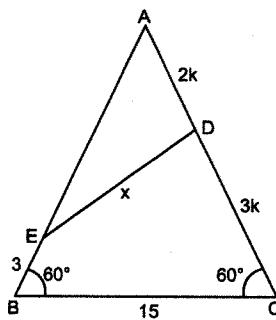
68.

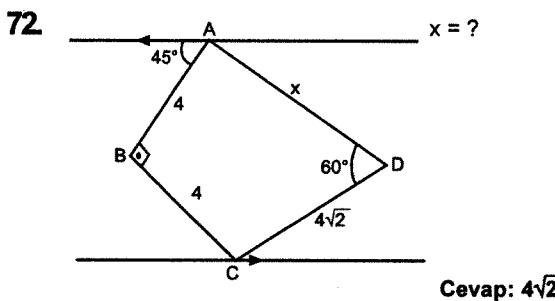
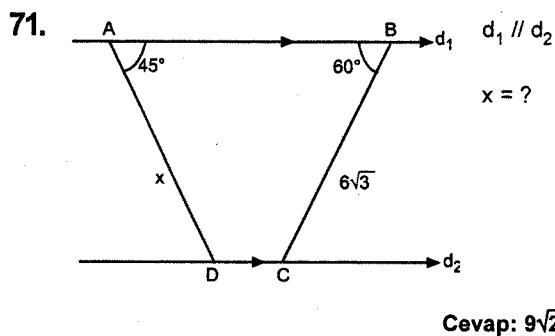
 $x = ?$ Cevap:  $4\sqrt{3}$ 

69.

 $x = ?$ Cevap:  $\sqrt{2}$ 

70.

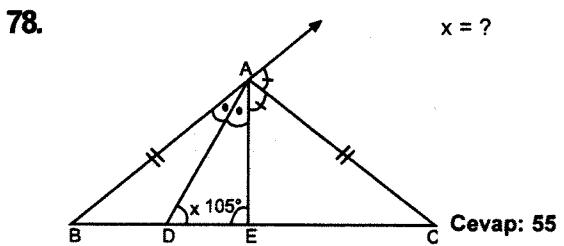
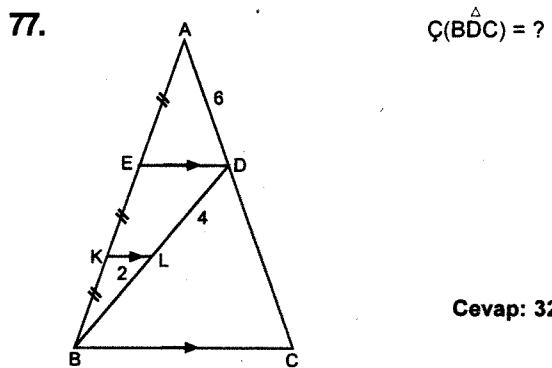
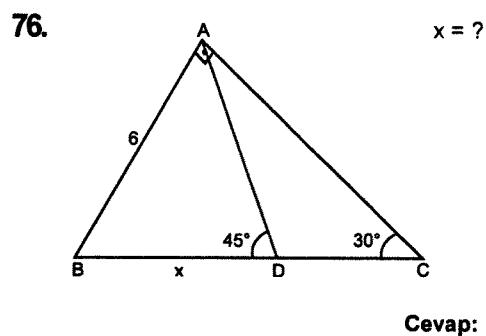
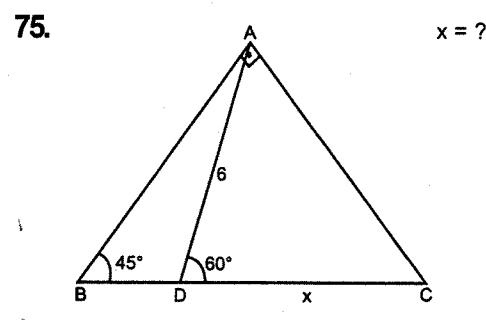
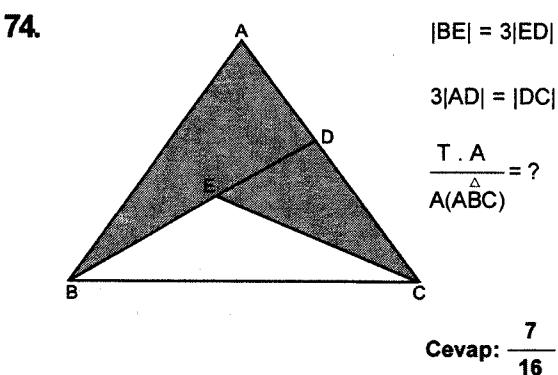
 $x = ?$ Cevap:  $6\sqrt{3}$



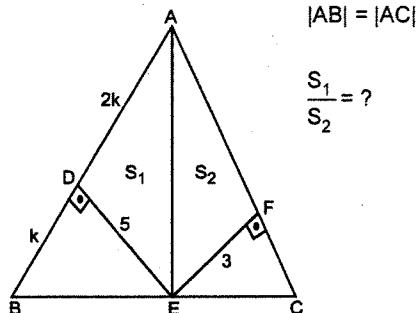
73. 16 cm uzunluğundaki bir merdiven yer ile  $30^\circ$  açı yapacak şekilde, yere dik bir duvara dayandırılıyor.

Eğer  $60^\circ$  lik açı ile duvara dayandırılmış olsaydı, merdivenin duvara temas ettiği noktalar arasındaki uzaklık ne olurdu?

Cevap:  $8\sqrt{3} - 8$

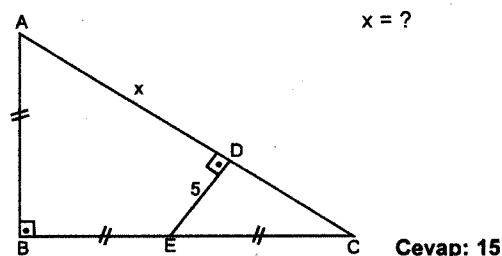


79.

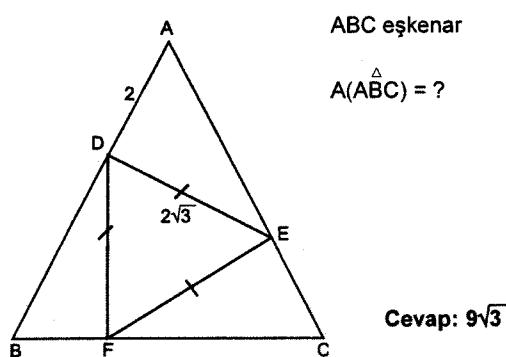


$$\text{Cevap: } \frac{25}{18}$$

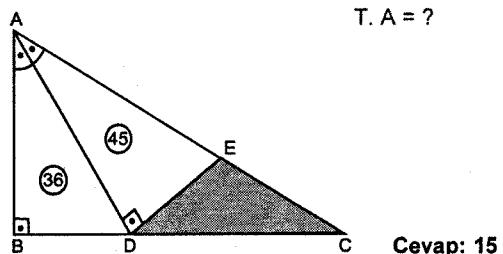
80.



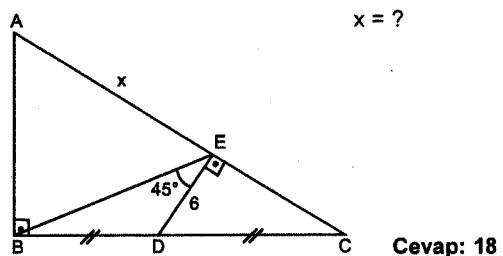
81.



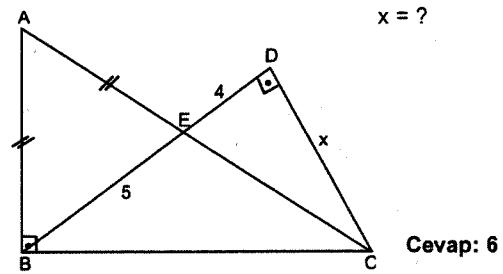
82.



83.



84.



## DÖRTGENLER VE ÇOKGENLER

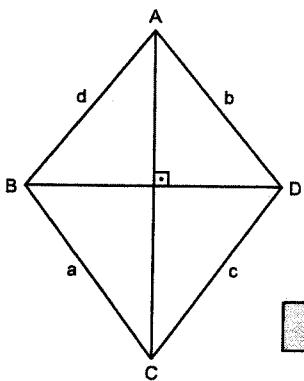
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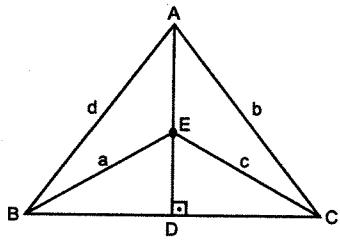
### Dörtgenler

1.



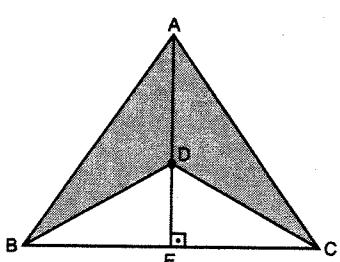
$$a^2 + b^2 = c^2 + d^2$$

2.



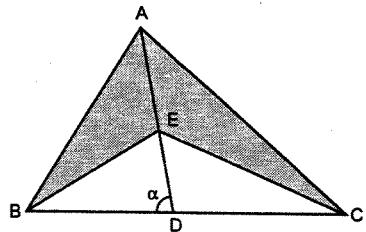
$$a^2 + b^2 = c^2 + d^2$$

3.



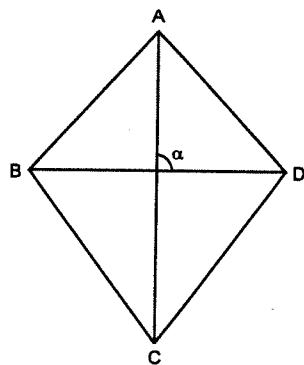
$$\text{Taralı Alan} = \frac{|AD| \cdot |BC|}{2}$$

4.



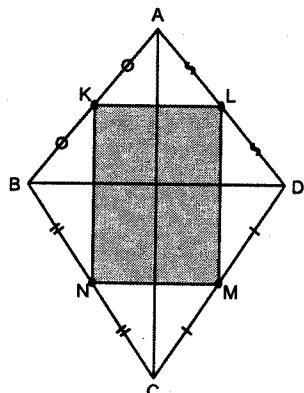
$$\text{Taralı Alan} = \frac{|AE| \cdot |BC|}{2} \cdot \sin\alpha$$

5.



$$\text{Alan(ABCD)} = \frac{|AC| \cdot |BD|}{2} \cdot \sin\alpha$$

6.



$\text{Alan(ABCD)} = 2 \cdot \text{Alan(KLMN)}$   
KLMN paralelkenardır.

$$\text{Çevre(KLMN)} = |AC| + |BD|$$

## Çokgenler

$n$ : Kenar sayısı, açı sayısı, köşe sayısı olmak üzere.

$n$  kenarlı bir çokgenin

1. İç açıları toplamı  $(n-2) \cdot 180^\circ$
2. Dış açıları toplamı  $360^\circ$  dir.
3. Köşegen sayısı  $\frac{n \cdot (n-3)}{2}$  dir.
4. Bir köşesinden çıkan köşegenler çokgeni  $(n-2)$  farklı üçgene ayırr.
5. Bir köşesinden çıkan köşegen sayısı  $(n-3)$  tür.
6. Bir çokgenin tek türlü olarak çizilebilmesi için  $(2n-3)$  tane bağımsız bilgiye ihtiyaç vardır. Bu bilgilerin en az  $(n-2)$ 'si kenar, en çok  $(n-1)$ 'i açı bilgisi olmalıdır.

### Düzgün Çokgen

Tüm iç açıları ve tüm kenarları birbirine eşit olan çokgenlere denir.

Bir dış açı  $360^\circ$  nin kenarsayısına bölünerek elde edilir.

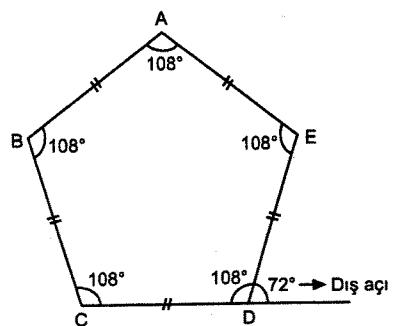
$$\text{Dış açı} = \frac{360^\circ}{n}$$

İç açı ile dış açı toplamı  $180^\circ$  dir.

Eşkenar üçgen, düzgün bir çokgendir.

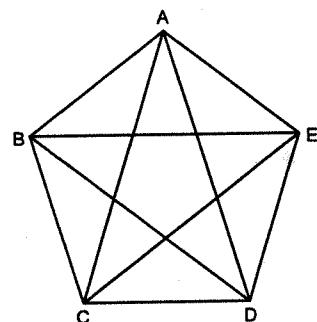
Kare, düzgün bir çokgendir.

### Düzgün Beşgen

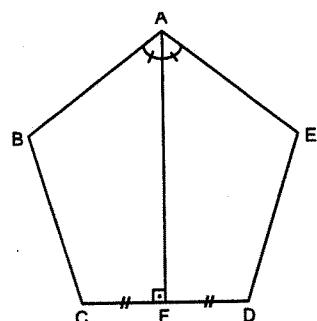


İç açısı  $108^\circ$  dir.

Dış açısı  $72^\circ$  dir.



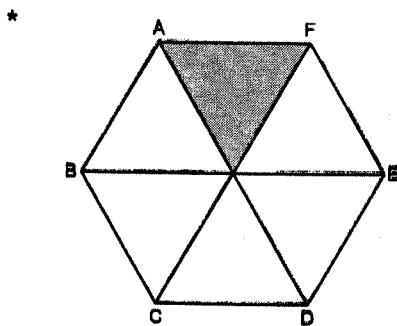
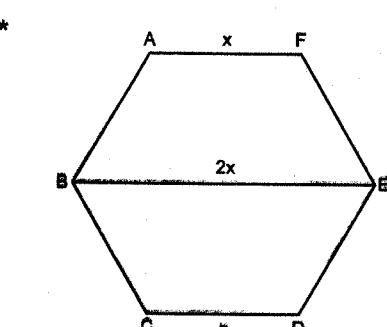
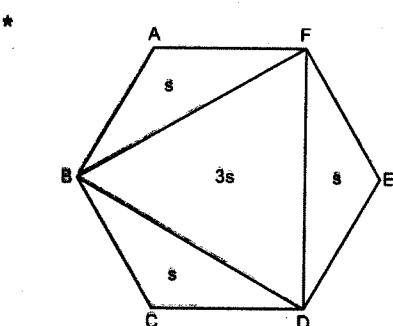
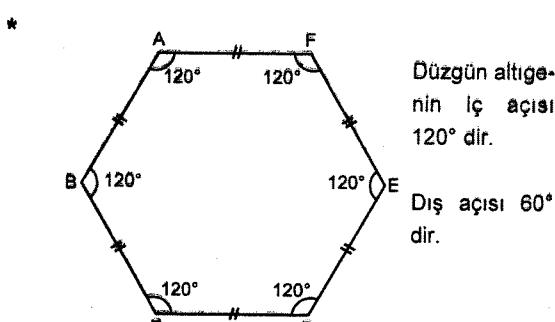
Tüm köşegenleri birbirine eşittir.



Tepeden tabana dik indirdiğimiz zaman taban iki eşit kenara, açı da eşit iki parçaya ayrılır.

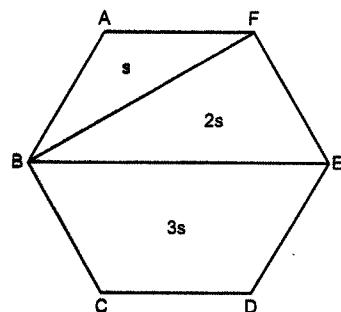
**Not:** Açı sorularında tüm kenarların eşit olduğunu mutlaka gösterin.

## Düzungün Altıgen



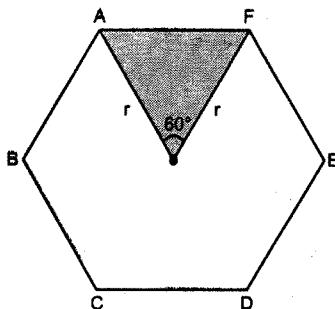
Bütün üçgenler eşkenar üçgendir.

$$A(ABCDEF) = \frac{6 \cdot x^2 \sqrt{3}}{4}$$



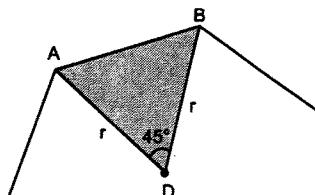
Her düzungün çokgenin etrafından bir çember geçer. Bu çemberin merkezi çokgenin ağırlık merkezidir. Bu merkezden köşelere çizilen çizgiler çemberin yarıçap uzunluğunu verir. Düzungün altıgen, düzungün sekizgen ve düzungün onikigenin alanları sorulabilir.

## Düzungün Altıgen



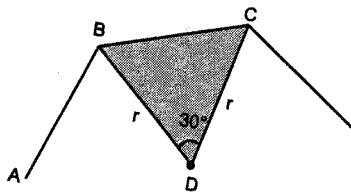
$$A(ABCDEF) = 6 \cdot \left(\frac{1}{2} \cdot r \cdot r \cdot \sin 60^\circ\right)$$

## Düzungün Sekizgen

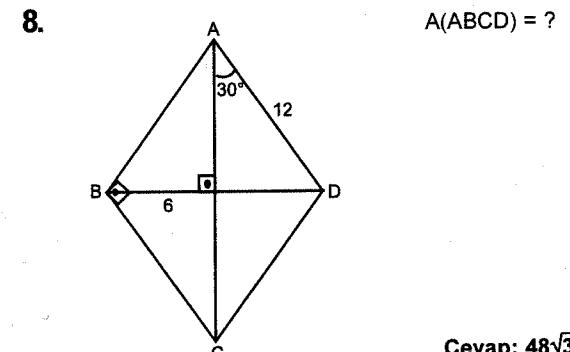
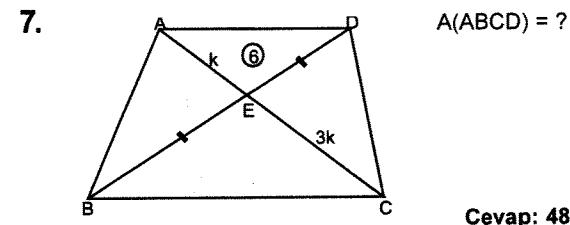
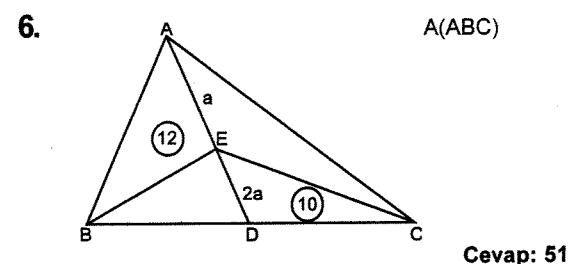
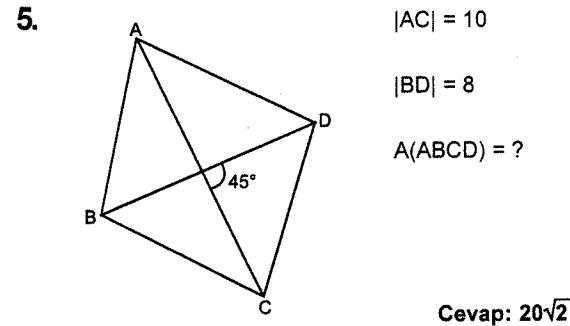
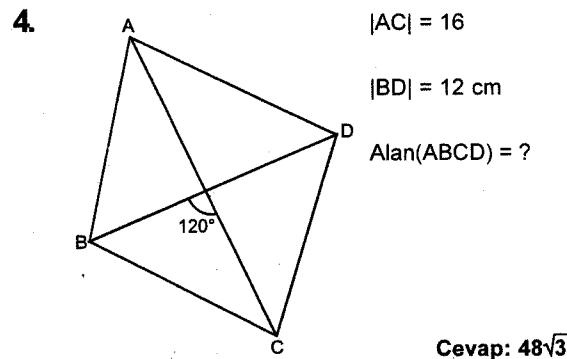
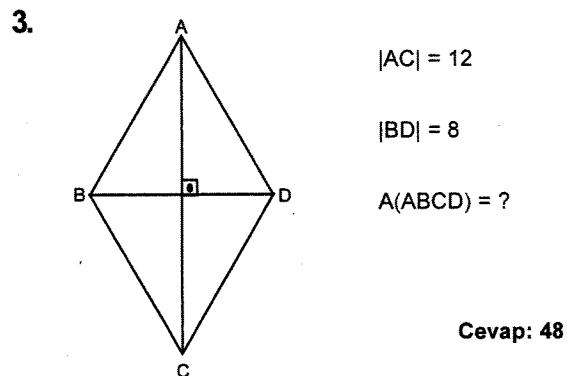
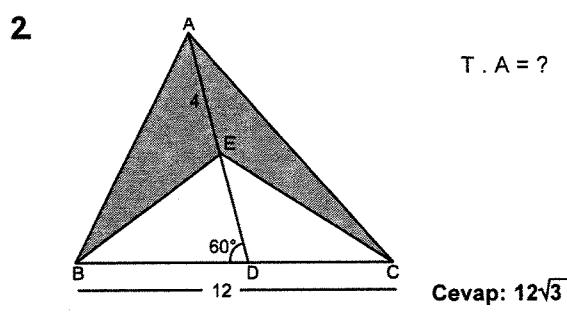
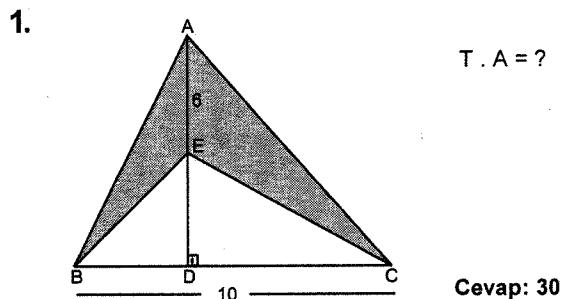


$$\text{Alan} = 8 \cdot \frac{1}{2} \cdot r \cdot r \cdot \sin 45^\circ$$

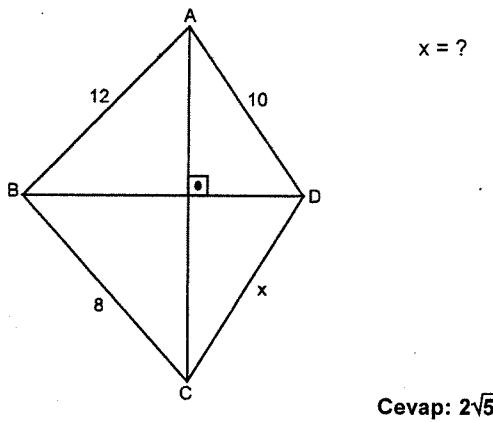
## Düzungün Onikigen



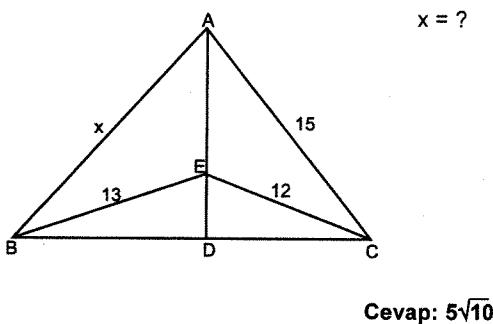
$$\text{Alan} = 12 \cdot \frac{1}{2} \cdot r \cdot r \cdot \sin 30^\circ$$



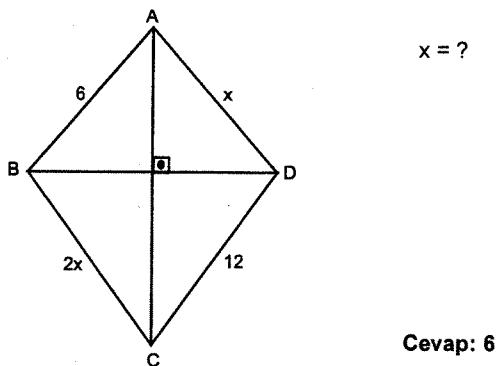
9.



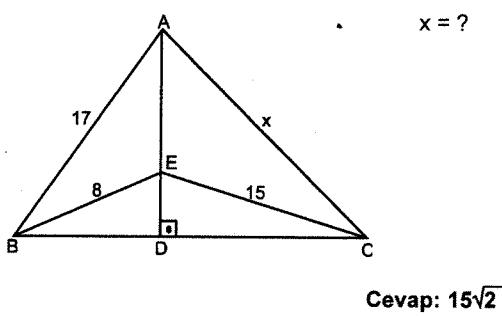
10.



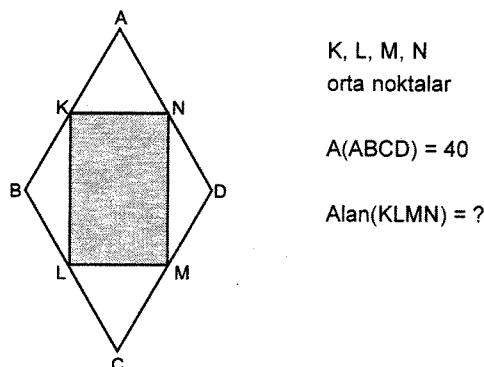
11.



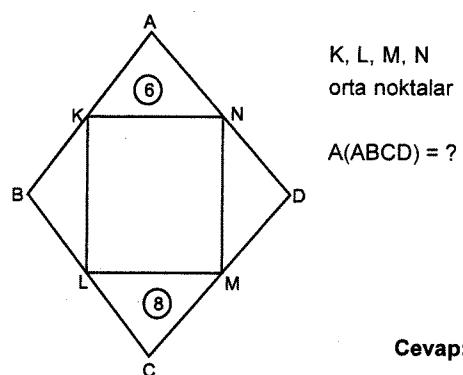
12.



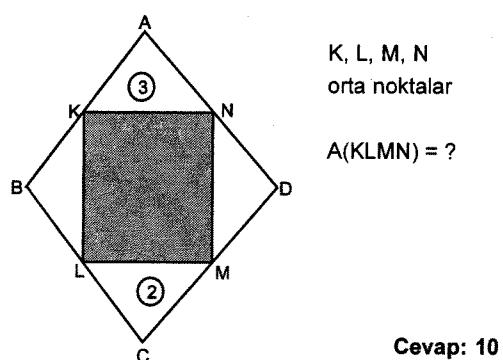
13.



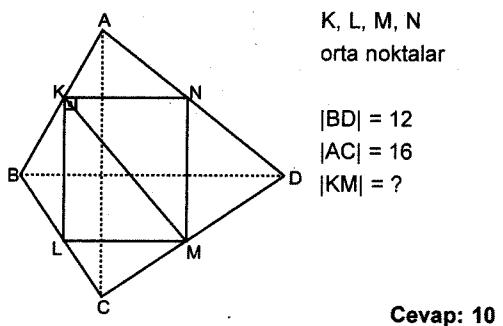
14.

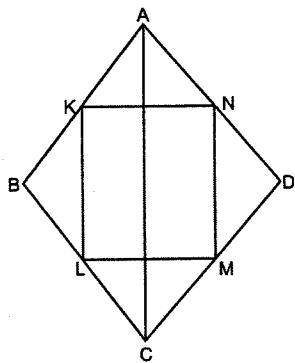


15.



16.



**17.**

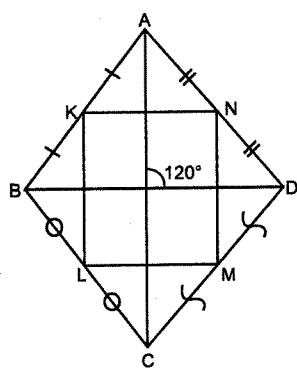
K, L, M, N  
orta noktalar

KLMN kare

$$|AC| = 12$$

$$A(ABCD) = ?$$

Cevap: 72

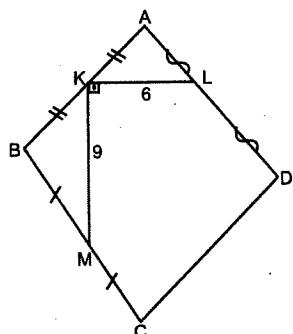
**18.**

$$|AC| = |BD|$$

$$|KN| = 6$$

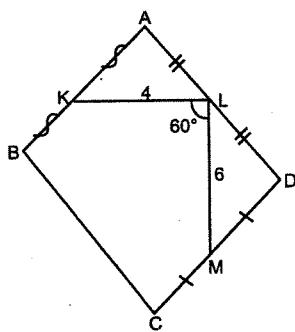
$$A(ABCD) = ?$$

Cevap:  $36\sqrt{3}$

**19.**

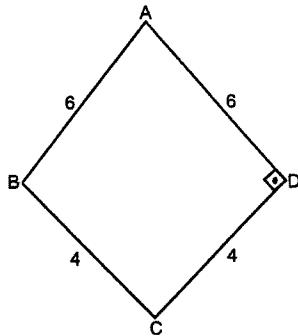
$$A(ABCD) = ?$$

Cevap: 108

**20.**

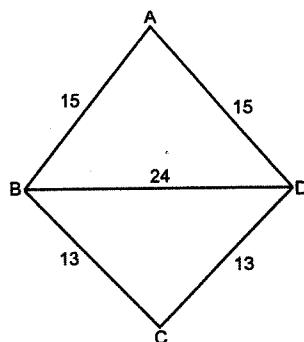
$$A(ABCD) = ?$$

Cevap:  $24\sqrt{3}$

**21.**

$$A(ABCD) = ?$$

Cevap: 24

**22.**

$$A(ABCD) = ?$$

Cevap: 168

- 23.** Dışbükey bir çokgenin iç açılarından bazıları  $120^\circ$ ,  $130^\circ$ ,  $140^\circ$  ve  $150^\circ$  dir. Diğer iç açıları eşit olup  $160^\circ$  dir.  
Bu çokgenin kenar sayısı kaçtır?

Cevap: 13

- 24.** Dış açıları  $1 : 2 : 3$  ve  $4$  ile orantılı bir dörtgenin iç açıları hangi sayılarla orantılıdır?

Cevap:  $4 : 3 : 2 : 1$

**25.** 12 kenarlı bir çokgenin köşegen sayısı kaçtır?

Cevap: 54

**26.** İç açısı  $144^\circ$  olan bir düzgün çokgenin köşegen sayısı kaçtır?

Cevap: 35

**27.** İç açısı  $165^\circ$  olan bir düzgün çokgenin köşegen sayısı kaçtır?

Cevap: 252

**28.** İç açısı dış açısının 4 katından  $20^\circ$  eksik olan düzgün çokgenin kenar sayısı kaçtır?

Cevap: 9

**29.** İç açısı ile dış açısının farkı  $120^\circ$  olan düzgün çokgenin kenar sayısı kaçtır?

Cevap: 12

**30.** İç açısı  $168^\circ$  olan düzgün çokgenin bir köşesinden çıkan köşegenler çokgeni kaç farklı üçgene ayırrır?

Cevap: 28

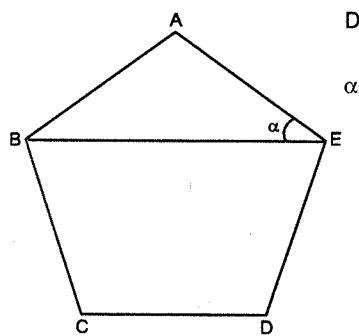
**31.** Köşegen sayısının kenar sayısına oranı 6 olan düzgün çokgenin iç açısı kaçtır?

Cevap: 156

**32.** İç açısı  $172^\circ$  olan düzgün bir çokgenin köşegen sayısının kenar sayısına oranı kaçtır?

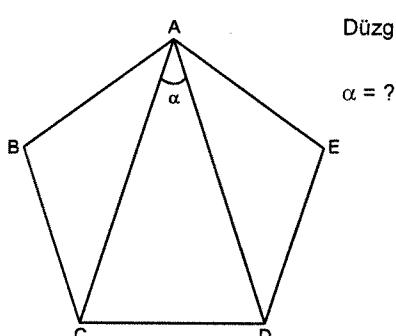
Cevap: 21

**33.** Düzgün beşgen  $\alpha = ?$



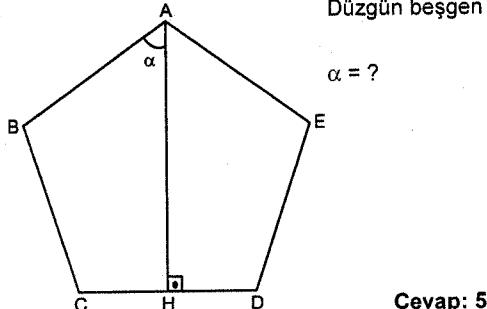
Cevap: 36

**34.** Düzgün beşgen  $\alpha = ?$



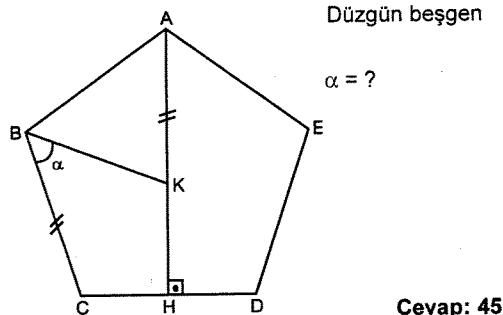
Cevap: 36

35.



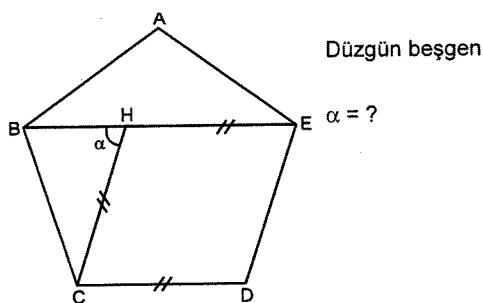
Cevap: 54

36.



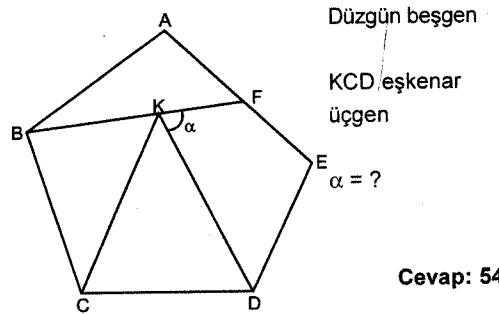
Cevap: 45

37.



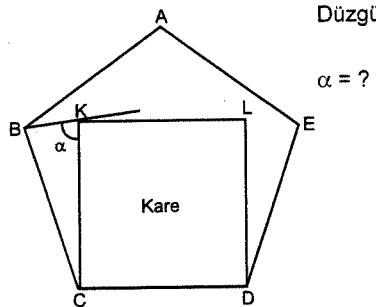
Cevap: 72

38.



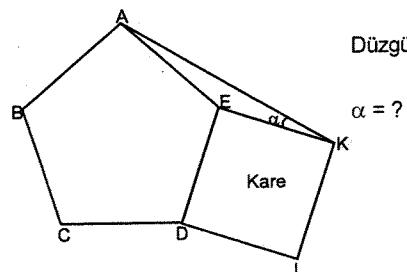
Cevap: 54

39.



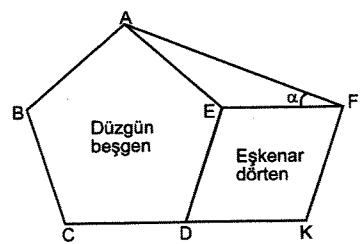
Cevap: 81

40.



Cevap: 9

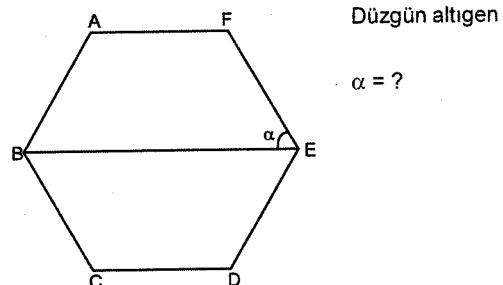
41.



Cevap: 18

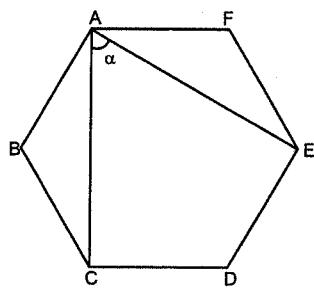
Not: (42-58) soruları içerisindeki şekiller DÜZGÜN ALTİGEN'dır.

42.



Cevap: 60

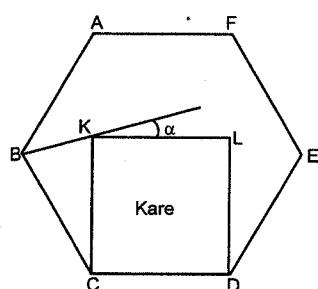
43.



$\alpha = ?$

Cevap: 60

44.

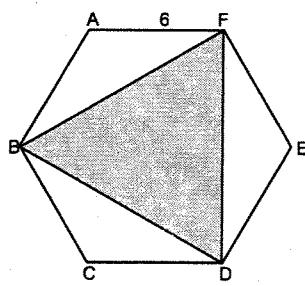


$\alpha = ?$

Kare

Cevap: 15

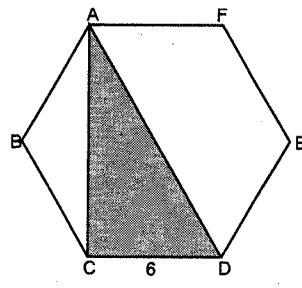
45.



$T \cdot A = ?$

Cevap:  $27\sqrt{3}$ 

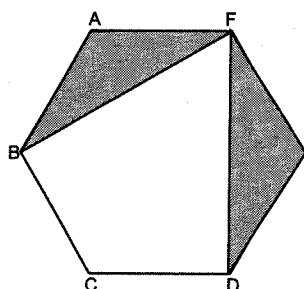
47.



$T \cdot A = ?$

Cevap:  $18\sqrt{3}$ 

48.

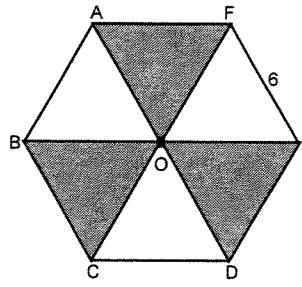


$T \cdot A = 8\sqrt{3}$

$\mathcal{C}(ABCDEF) = ?$

Cevap: 24

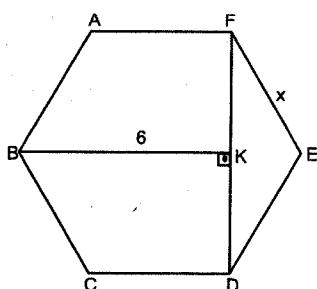
49.



$T \cdot A = ?$

Cevap:  $27\sqrt{3}$ 

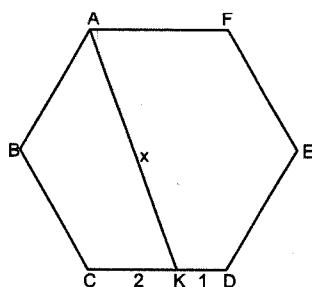
46.



$x = ?$

Cevap: 4

50.



$x = ?$

Cevap:  $\sqrt{31}$

51.

$x = ?$

- 52

$\frac{a}{b} = ?$

53.

$T \cdot A = ?$

Cevap:  $4\sqrt{3}$

- 54.**

$x = ?$

55.

$T \cdot A = 18\sqrt{3}$

$x = ?$

Cevap: 6

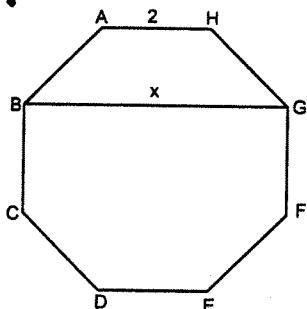
56.

- 

58.

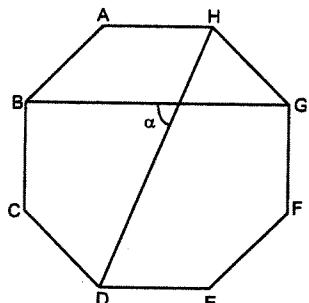
**Not:** (59-67) soruları içerisindeki şekiller DÜZGÜN SEKİZGEN'dır.

59.  $x = ?$



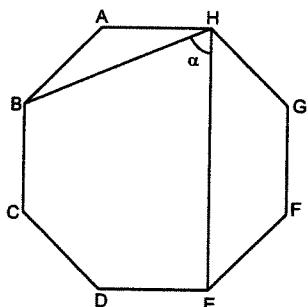
Cevap:  $2\sqrt{2} + 2$

60.  $\alpha = ?$



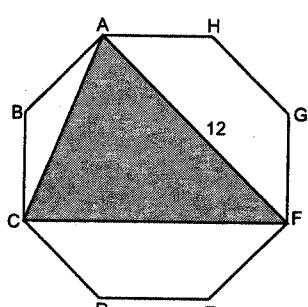
Cevap: 67,5

61.  $\alpha = ?$



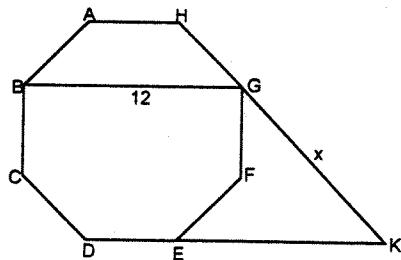
Cevap: 67,5

62.  $T \cdot A = ?$



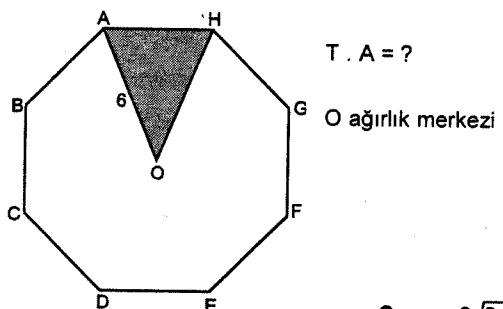
Cevap:  $36\sqrt{2}$

63.  $x = ?$



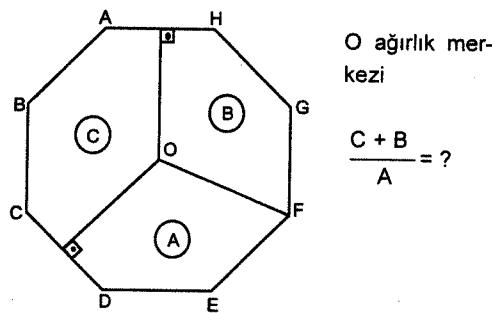
Cevap: 12

64.  $T \cdot A = ?$



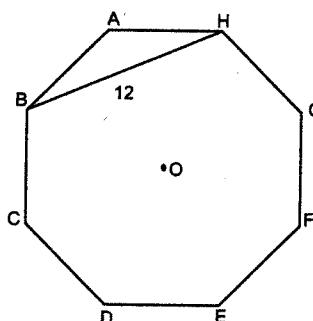
Cevap:  $9\sqrt{2}$

65.  $O$  ağırlık merkezi  
 $\frac{C + B}{A} = ?$



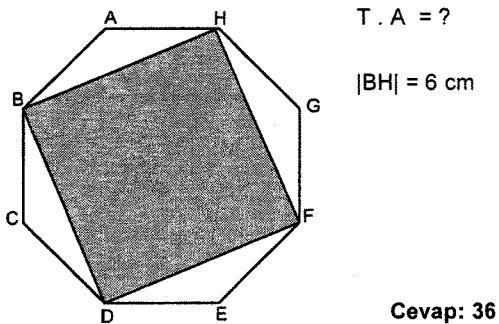
Cevap:  $\frac{11}{5}$

66.  $A(ABCDEFGH) = ?$



Cevap:  $144\sqrt{2}$

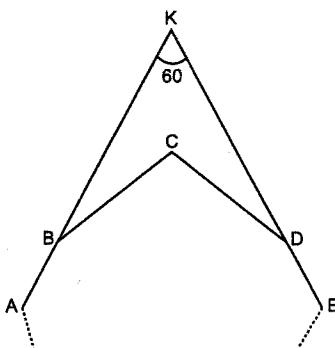
67.



$T \cdot A = ?$

$|BH| = 6 \text{ cm}$

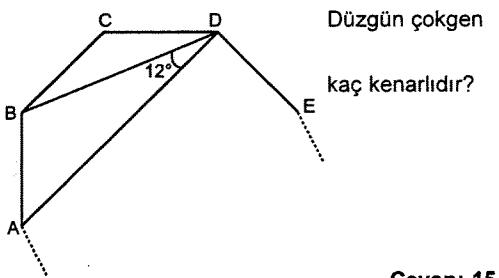
71.



ABCDE  
Düzenli  
çokgen  
kaç kenarlıdır?

Cevap: 9

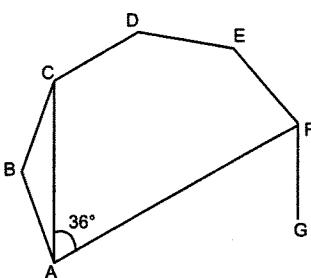
68.



Düzenli çokgen  
kaç kenarlıdır?

Cevap: 15

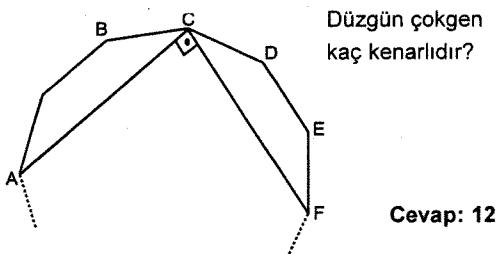
72.



Düzenli çokgen  
kaç kenarlıdır?

Cevap: 15

69.



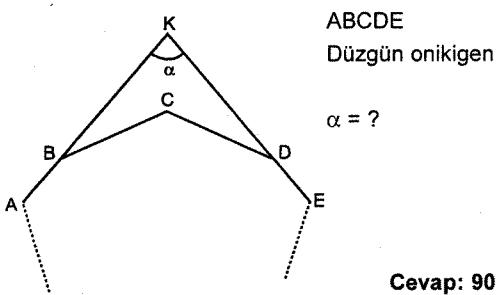
Düzenli çokgen  
kaç kenarlıdır?

Cevap: 12

73. İç teğet çemberinin yarıçapı  $4\sqrt{3}$  cm olan düzgün altigenin alanı kaç  $\text{cm}^2$  dir?

Cevap:  $96\sqrt{3}$ 

70.



ABCDE  
Düzenli onikigen

$\alpha = ?$

Cevap: 90

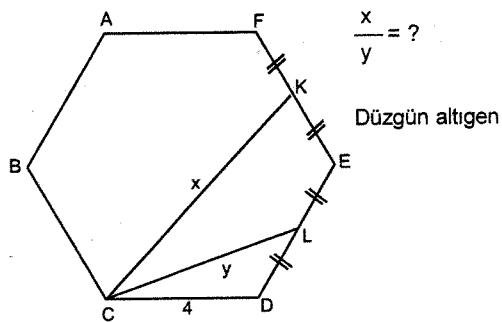
74. Çevrel çemberin yarıçapı 4 cm olan düzgün sekizgenin alanı kaçtır?

Cevap:  $32\sqrt{2}$ 

75. Çevrel çemberin yarıçapı 4 cm olan düzgün onikigenin alanı kaçtır?

Cevap: 48

76.

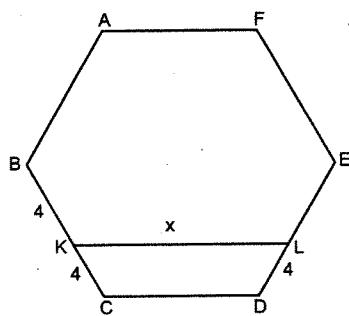


$$\frac{x}{y} = ?$$

Düzgün altigen

$$\text{Cevap: } \frac{\sqrt{13}}{\sqrt{7}}$$

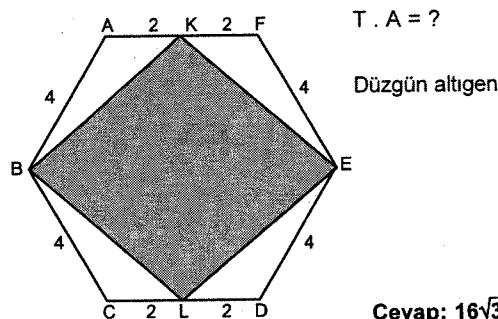
79.



ABCDEF  
Düzgün altigen  
 $x = ?$

Cevap: 12

77.

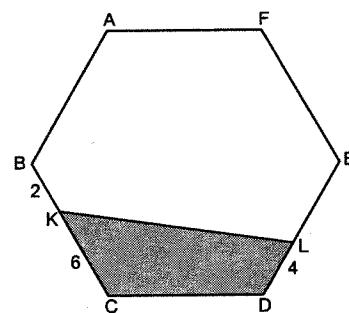


$$T.A = ?$$

Düzgün altigen

$$\text{Cevap: } 16\sqrt{3}$$

80.

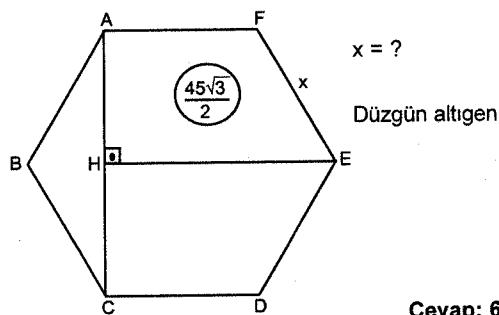


ABCDEF  
Düzgün altigen

$$T.A = ?$$

Cevap:  $26\sqrt{3}$ 

78.

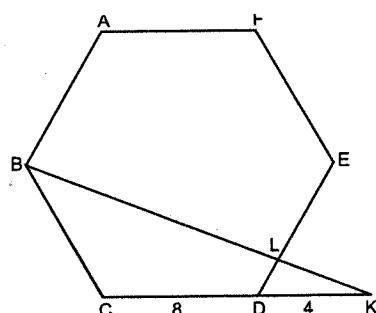


$$x = ?$$

Düzgün altigen

Cevap: 6

81.



ABCDEF

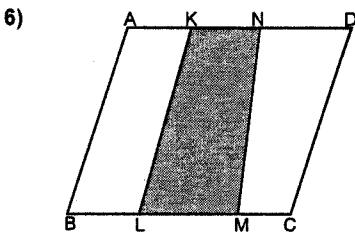
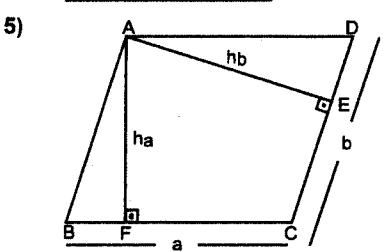
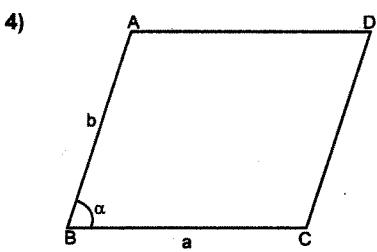
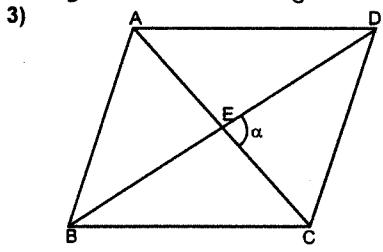
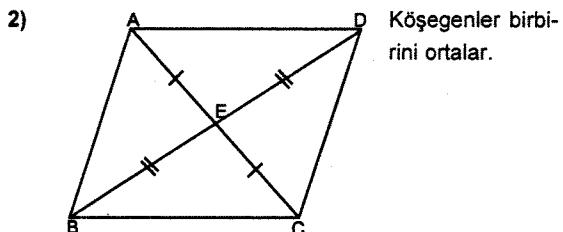
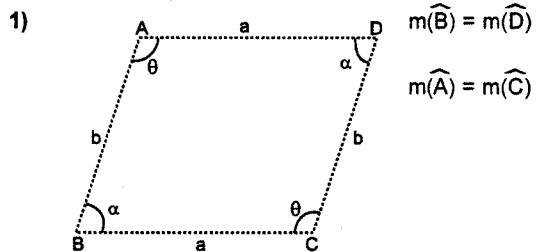
Düzgün altigen

$$\frac{|LE|}{|LD|} = ?$$

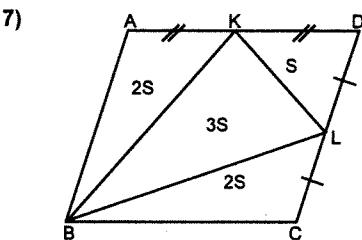
Cevap: 4

## PARALELKENAR

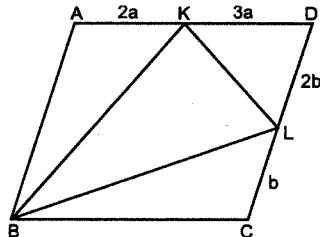
Karşılıklı kenarları birbirine paralel ve eşit olan dörgenе paralelkenar denir.



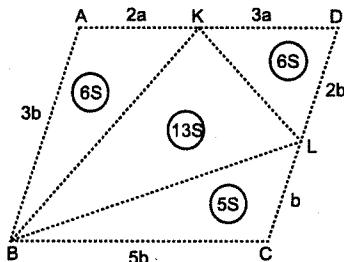
$$\frac{\text{Alan}(ABCD)}{\text{Alan}(KLMN)} = \frac{|AD|+|BC|}{|LM|+|KN|}$$



Örnek



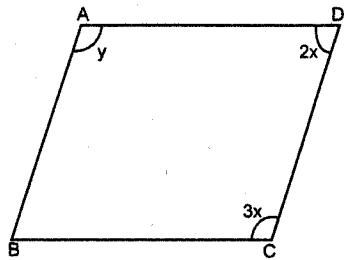
Şimdi bu bölgeleri S'liyelim.



$$\begin{aligned} A(\hat{ABK}) &= 2a \cdot 3b = 6ab = 6S \\ A(\hat{KDL}) &= 3a \cdot 2b = 6ab = 6S \\ A(\hat{BCL}) &= 5a \cdot b = 5ab = 5S \end{aligned} \quad \left| \begin{array}{l} 17S \end{array} \right.$$

$$A(ABCD) = (3b \cdot 5a) \times 2 = 30ab = 30S$$

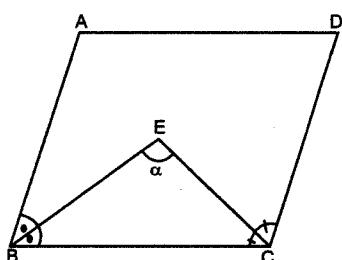
1.



$$y - x = ?$$

Cevap: 72

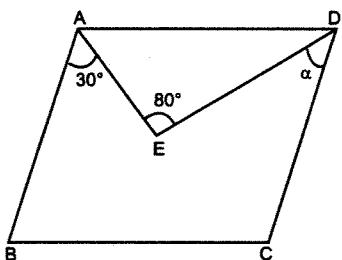
2.



$$\alpha = ?$$

Cevap: 90

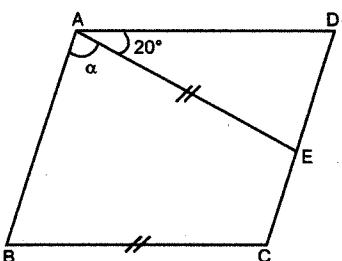
3.



$$\alpha = ?$$

Cevap: 50

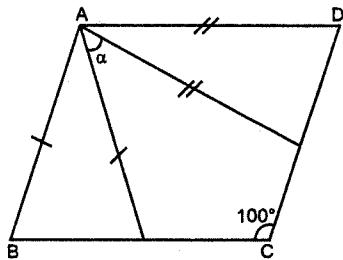
4.



$$\alpha = ?$$

Cevap: 80

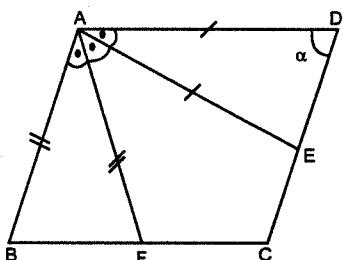
5.



$$\alpha = ?$$

Cevap: 60

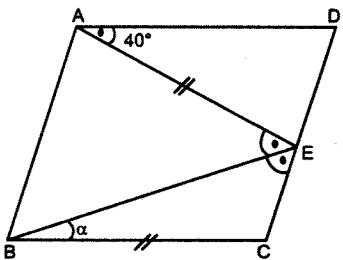
6.



$$\alpha = ?$$

Cevap: 72

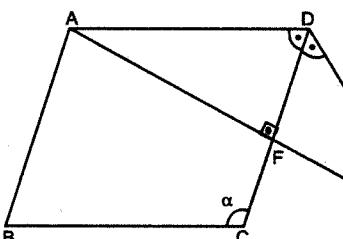
7.



$$\alpha = ?$$

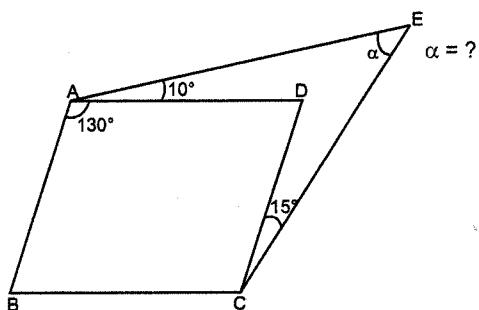
Cevap: 15

8.

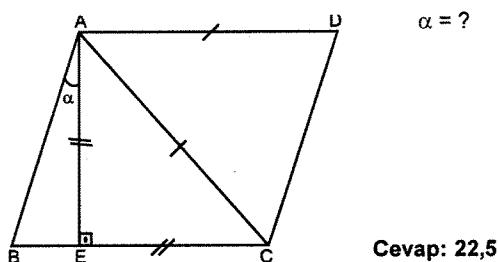


$$\alpha = ?$$

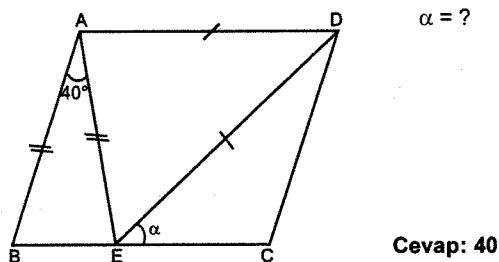
Cevap: 126

**9.**

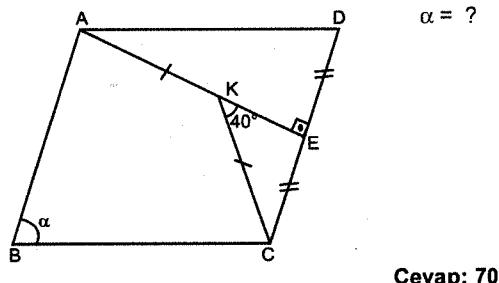
Cevap: 25

**10.**

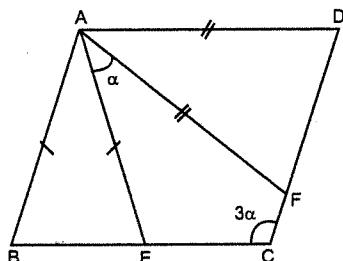
Cevap: 22,5

**11.**

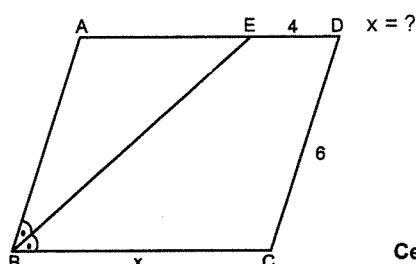
Cevap: 40

**12.**

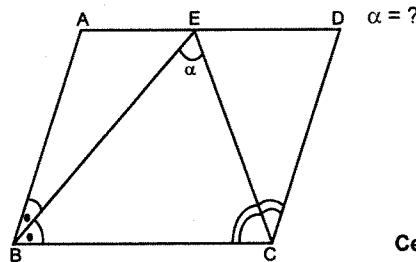
Cevap: 70

**13.** $\alpha = ?$ 

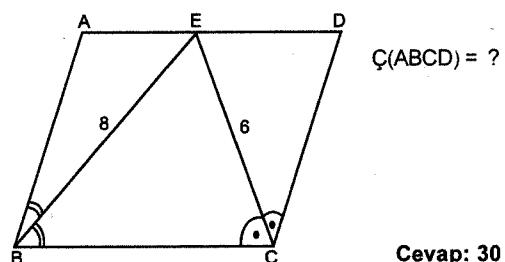
Cevap: 36

**14.** $x = ?$ 

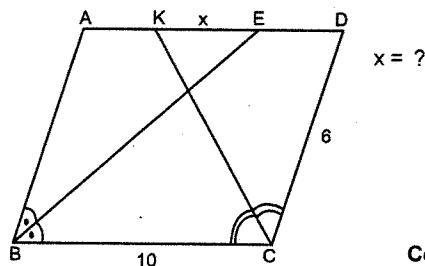
Cevap: 10

**15.** $\alpha = ?$ 

Cevap: 90

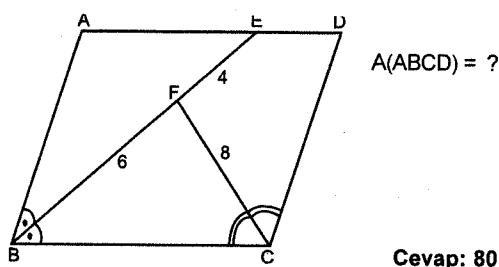
**16.** $\angle(ABCD) = ?$ 

Cevap: 30

**17.**

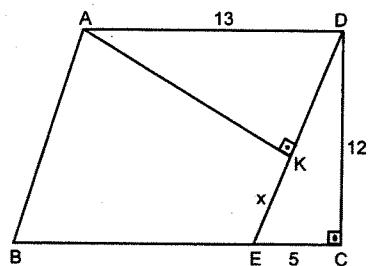
$$x = ?$$

Cevap: 2

**18.**

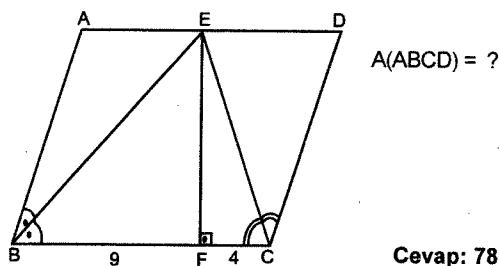
$$A(ABCD) = ?$$

Cevap: 80

**19.**

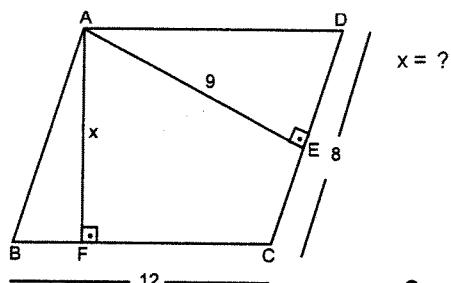
$$x = ?$$

Cevap: 8

**20.**

$$A(ABCD) = ?$$

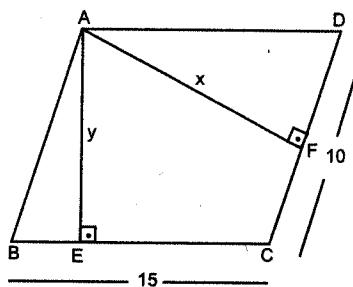
Cevap: 78

**21.**

$$12$$

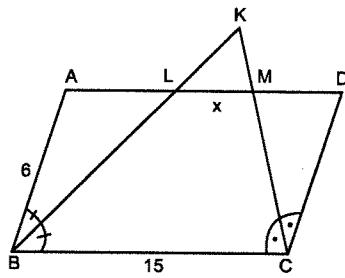
$$x = ?$$

Cevap: 6

**22.**

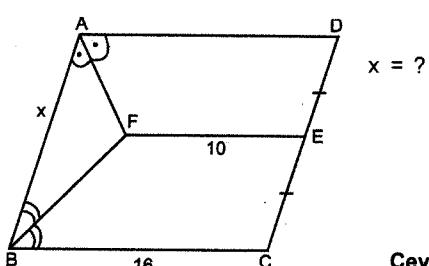
$$y = ?$$

Cevap: 8

**23.**

$$15$$

Cevap: 3

**24.**

$$16$$

$$x = ?$$

Cevap: 12

- 25.
- 
- $x = ?$

 $x = ?$ 

Cevap: 8

- 26.
- 
- T. A = ?

T. A = ?

Cevap: 12

- 27.
- 
- $x = ?$

 $x = ?$ 

Cevap: 7

- 28.
- 
- A(ABCD) = ?

A(ABCD) = ?

Cevap: 50

- 29.
- 
- $A(ABCD) = ?$

 $A(ABCD) = ?$ 

Cevap: 110

- 30.
- 
- $|BD| = 18$

 $|BD| = 18$  $x = ?$ 

Cevap: 6

- 31.
- 
- $|AC| = 14$

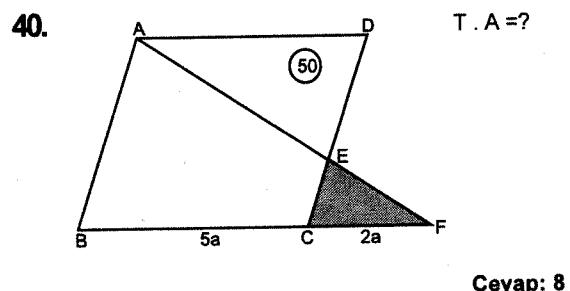
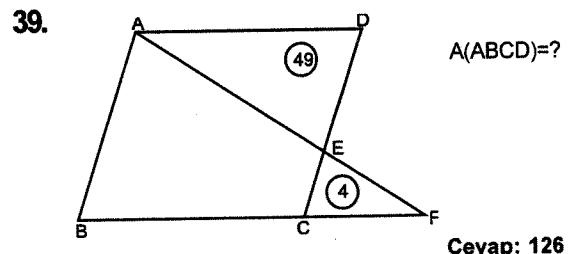
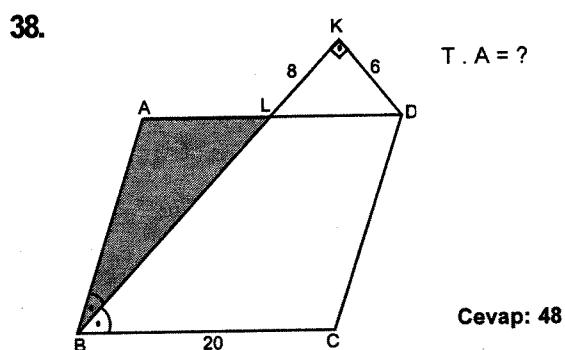
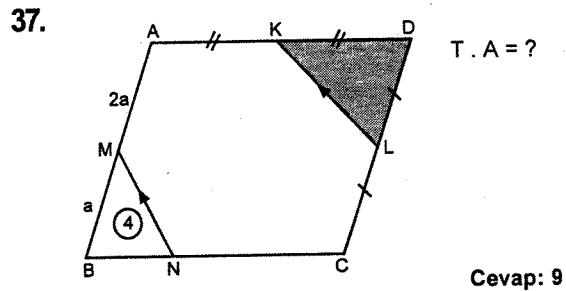
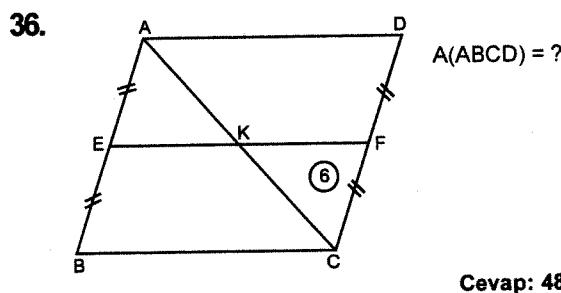
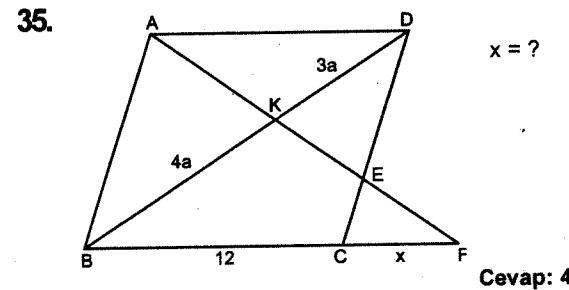
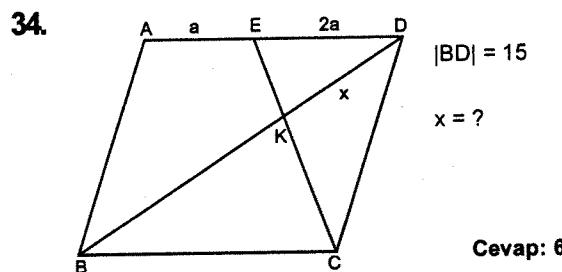
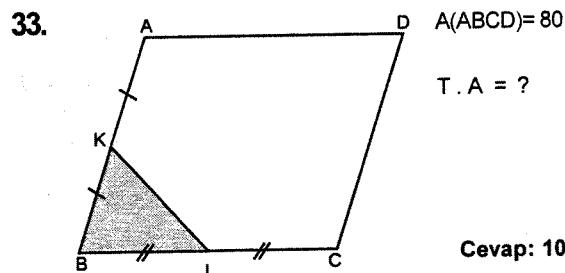
 $|AC| = 14$  $x = ?$ 

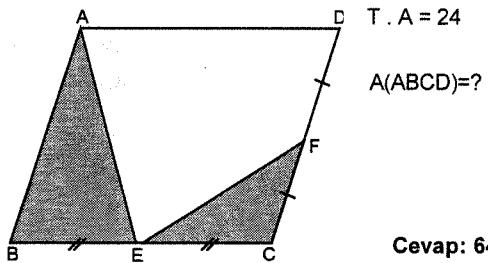
Cevap: 8

- 32.
- 
- $x = ?$

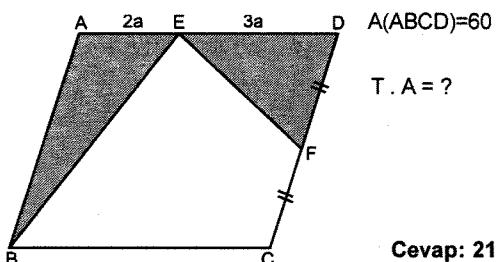
 $x = ?$ 

Cevap: 3

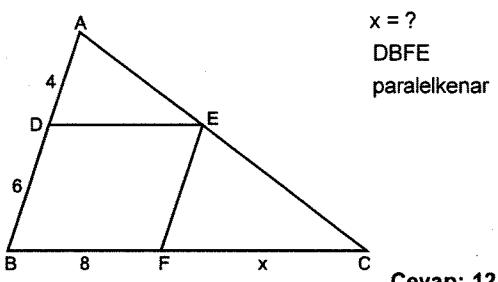


**41.**

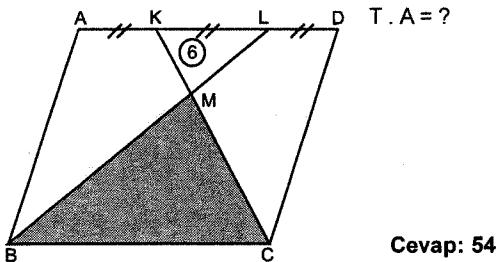
Cevap: 64

**42.**

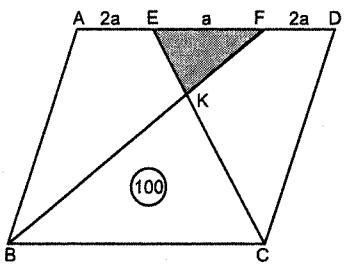
Cevap: 21

**43.**

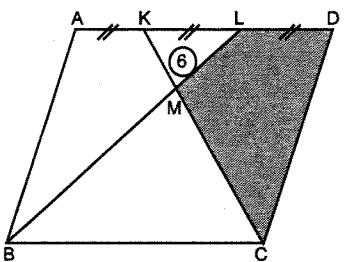
Cevap: 12

**44.**

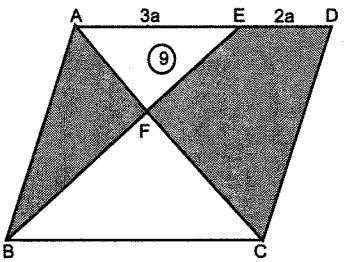
Cevap: 54

**45.**

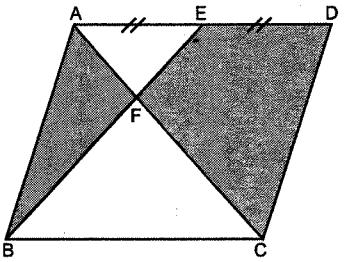
Cevap: 4

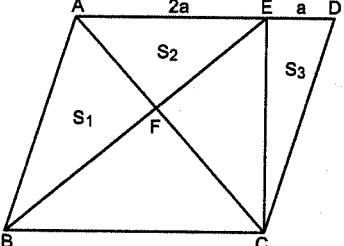
**46.**

Cevap: 42

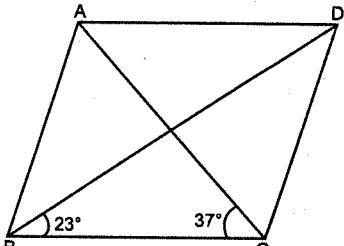
**47.**

Cevap: 46

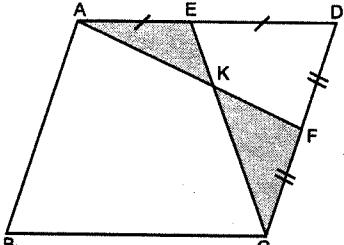
**48.**Cevap:  $\frac{7}{12}$

49. 

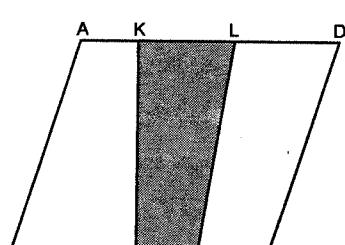
Cevap: 2

53. 

Cevap: 8

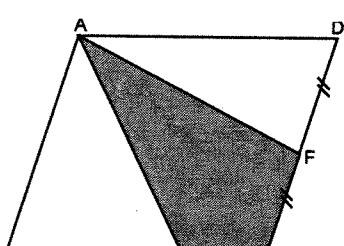
50. 

Cevap: 24

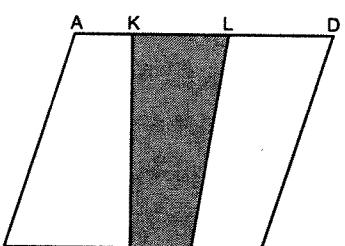
54. 

A(ABCD) = 48

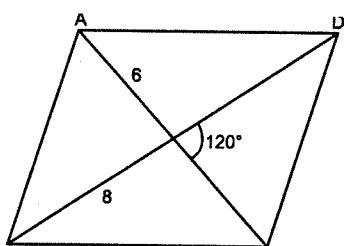
Cevap: 20

51. 

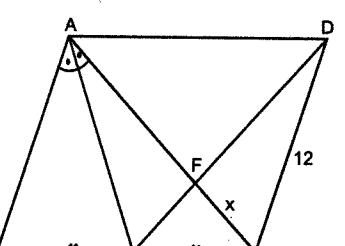
Cevap: 32

55. 

Cevap: 32

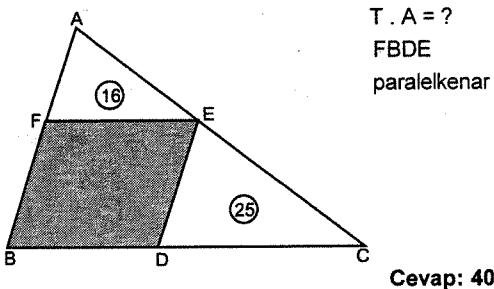
52. 

Cevap:  $48\sqrt{3}$ 

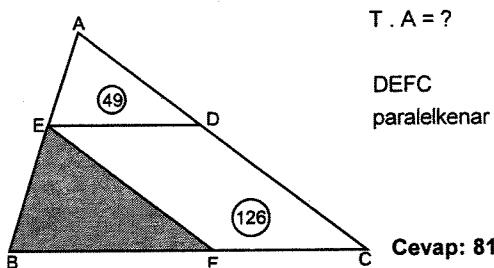
56. 

Cevap: 4

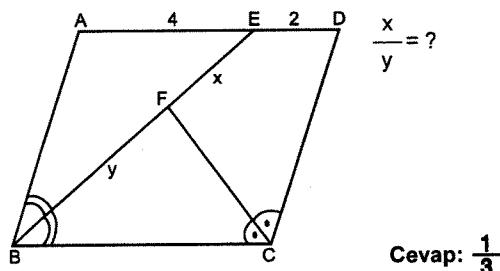
57.



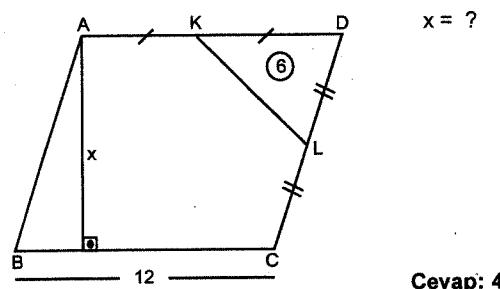
58.



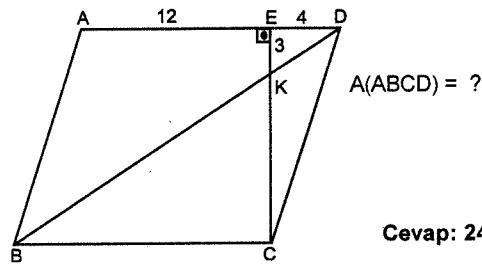
59.



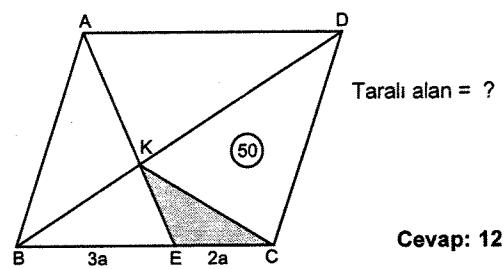
60.



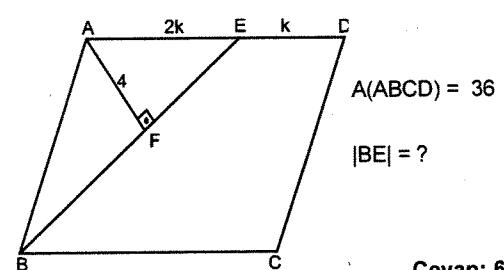
61.



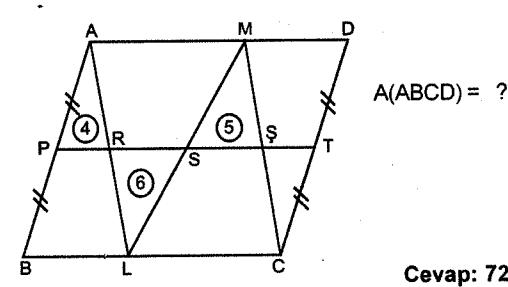
62.



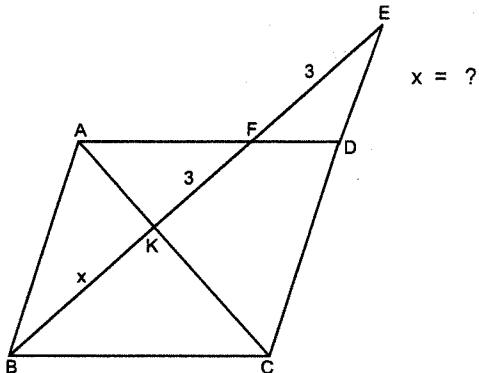
63.



64.

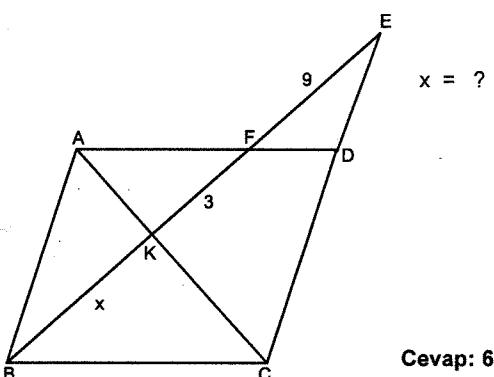


65.



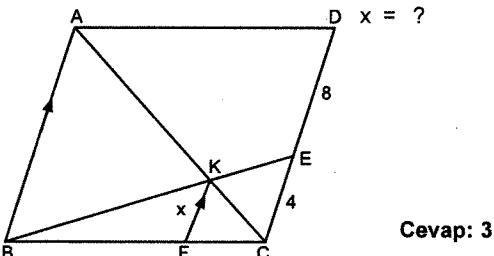
$$\text{Cevap: } 3\sqrt{2}$$

66.



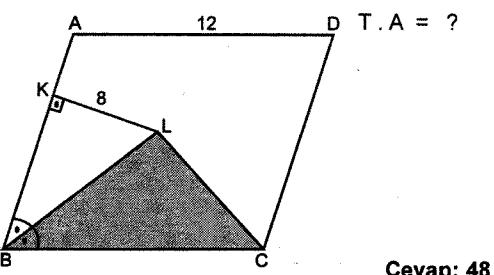
$$\text{Cevap: } 6$$

67.



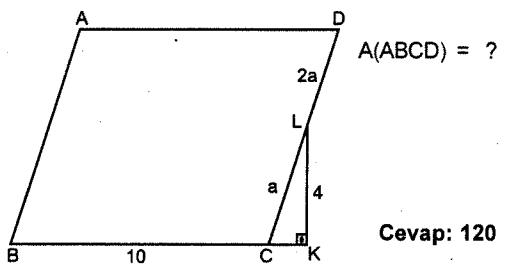
$$\text{Cevap: } 3$$

68.



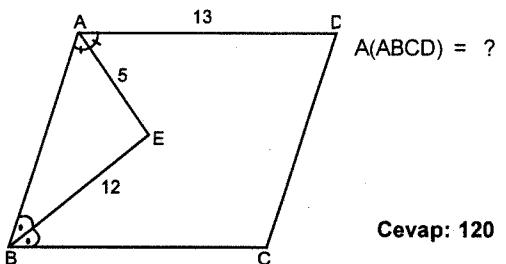
$$\text{Cevap: } 48$$

69.



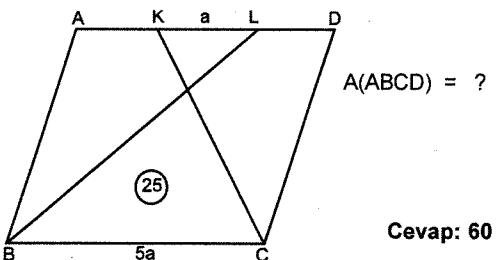
$$\text{Cevap: } 120$$

70.



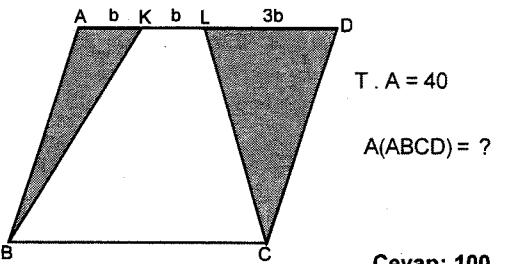
$$\text{Cevap: } 120$$

71.



$$\text{Cevap: } 60$$

72.

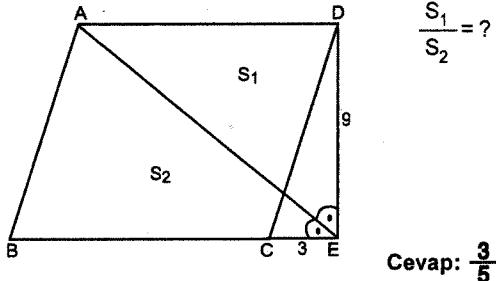


$$\text{T.A} = 40$$

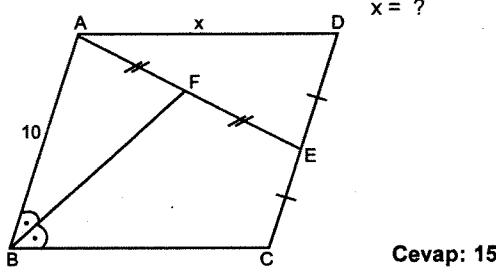
$$\text{A(ABCD)} = ?$$

$$\text{Cevap: } 100$$

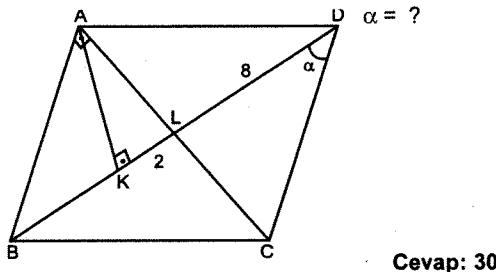
73.



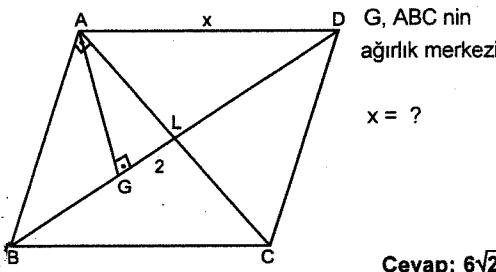
74.



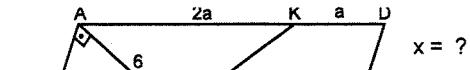
75.



76.

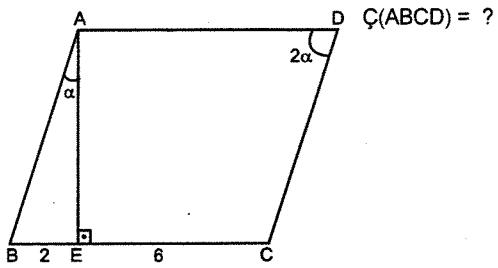


77.



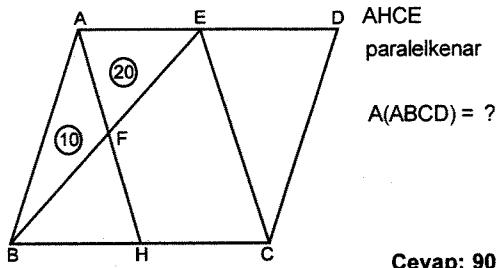
Cevap: 17

78.



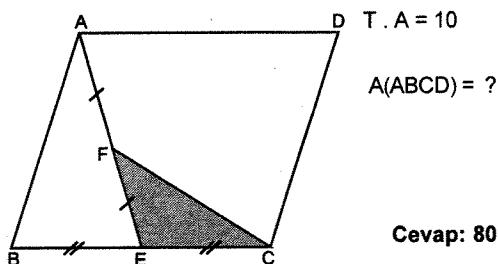
Cevap: 24

79.

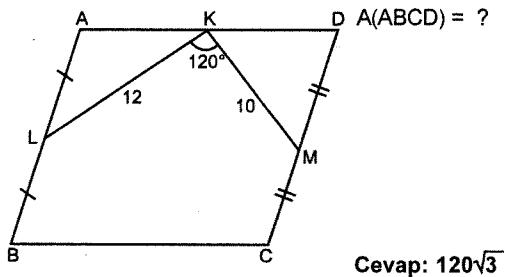


Cevap: 90

80.



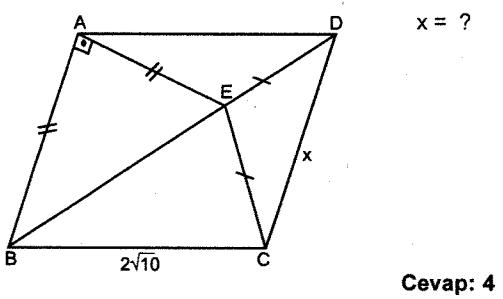
81.



A(ABCD) = ?

Cevap:  $120\sqrt{3}$ 

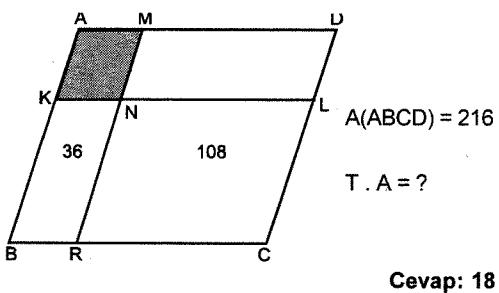
82.



x = ?

Cevap: 4

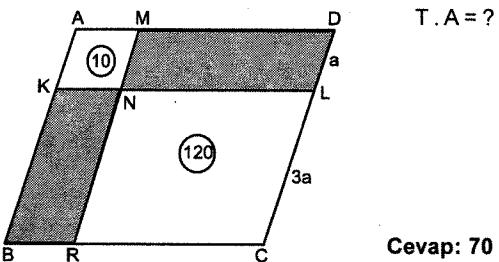
83.



T.A = ?

Cevap: 18

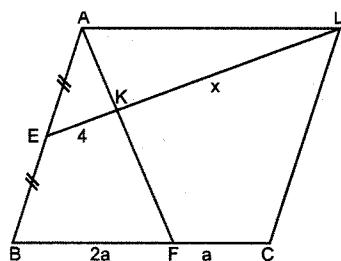
84.



T.A = ?

Cevap: 70

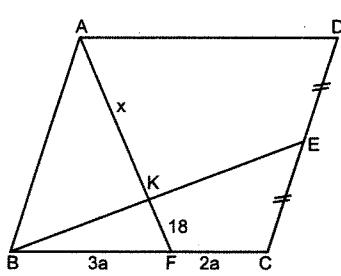
85.



x = ?

Cevap: 12

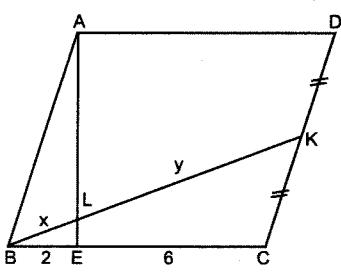
86.



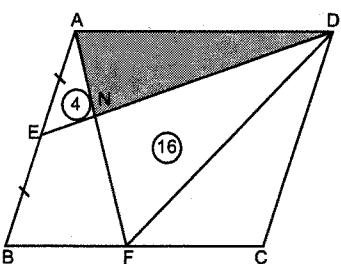
x = ?

Cevap: 60

87.

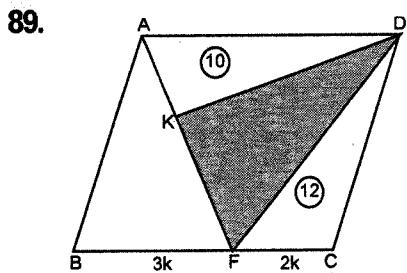
 $\frac{x}{y} = ?$ Cevap:  $\frac{2}{7}$ 

88.



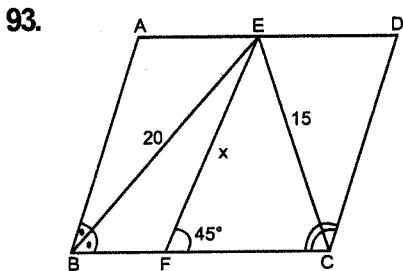
T.A = ?

Cevap: 8

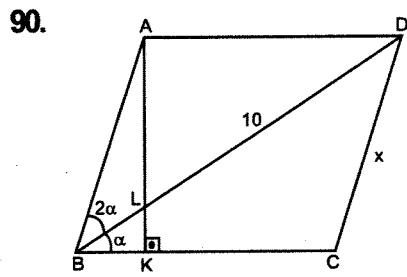


T. A = ?

Cevap: 20

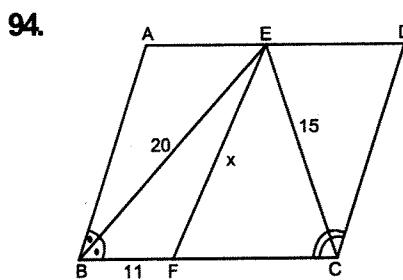


x = ?

Cevap:  $12\sqrt{2}$ 

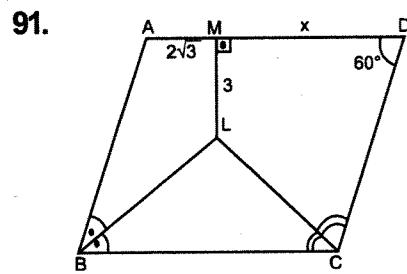
x = ?

Cevap: 5

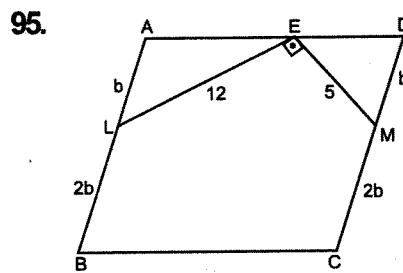


x = ?

Cevap: 13

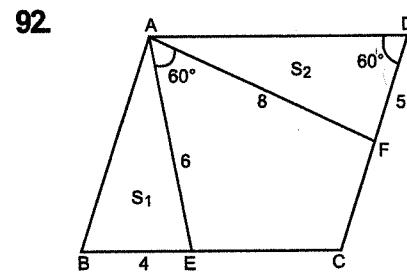
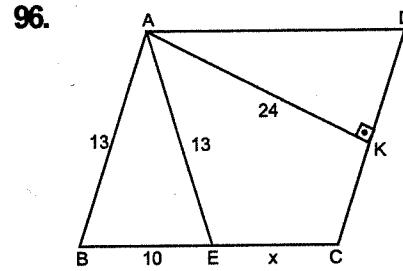


x = ?

Cevap:  $4\sqrt{3}$ 

A(ABCD) = ?

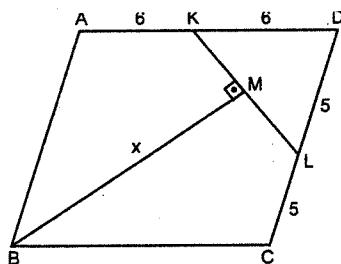
Cevap: 180

 $\frac{S_1}{S_2} = ?$ Cevap:  $\frac{3}{5}$ 

x = ?

Cevap: 16

97.

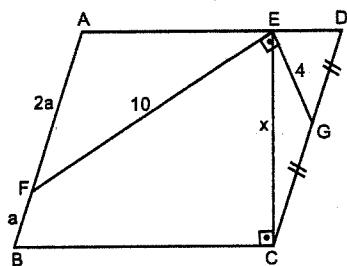


$$|KL| = 5$$

$$x = ?$$

Cevap: 14,4

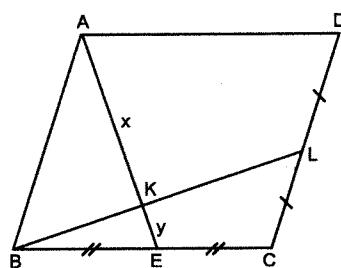
101.



$$x = ?$$

$$\text{Cevap: } \frac{120}{17}$$

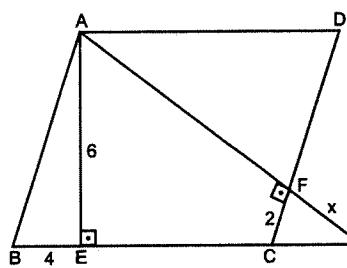
98.



$$\frac{x}{y} = ?$$

Cevap: 4

102.

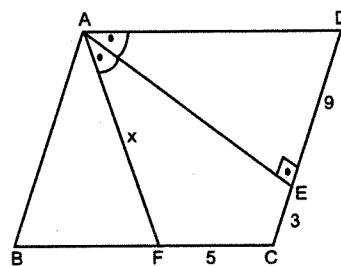


$$x = ?$$

Paralelkenar

Cevap: 3

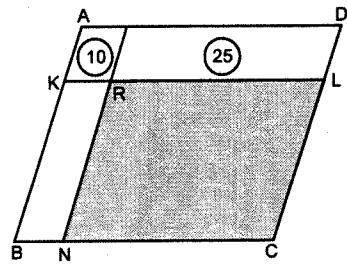
99.



$$x = ?$$

Cevap: 10

103.

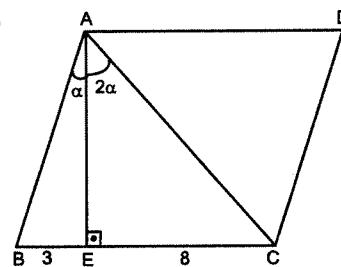


$$(ABCD) = 105$$

T. A = ?

Cevap: 50

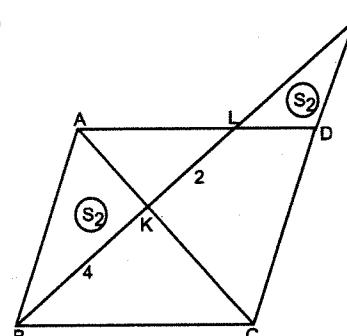
100.



$$A(ABCD) = ?$$

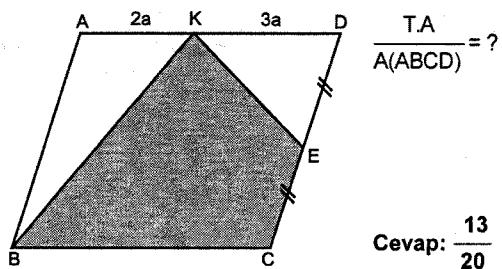
Cevap: 66

104.

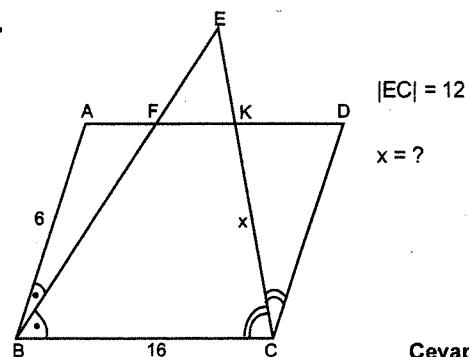


$$\frac{S_1}{S_2} = ?$$

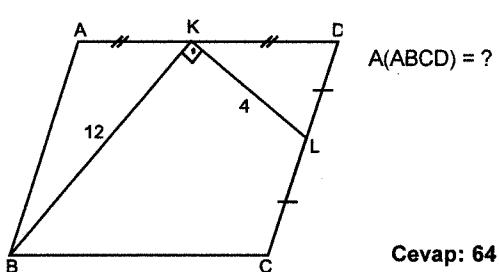
Cevap:  $\frac{2}{3}$

**105.**

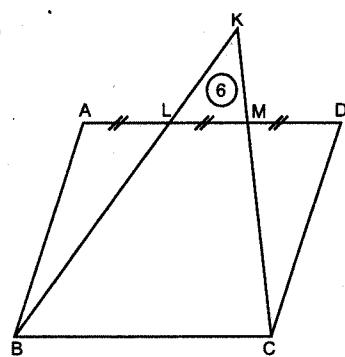
$$\text{Cevap: } \frac{13}{20}$$

**108.**

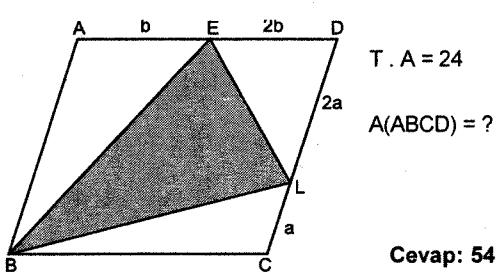
$$\text{Cevap: } 9$$

**106.**

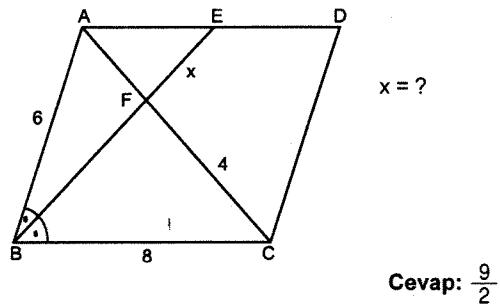
$$\text{Cevap: } 64$$

**109.**

$$\text{Cevap: } 72$$

**107.**

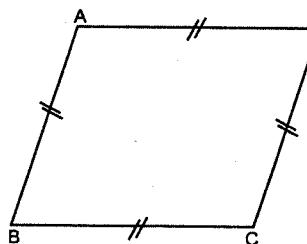
$$\begin{aligned} T.A &= 24 \\ A(ABCD) &=? \\ \text{Cevap: } 54 \end{aligned}$$

**110.**

$$\text{Cevap: } \frac{9}{2}$$

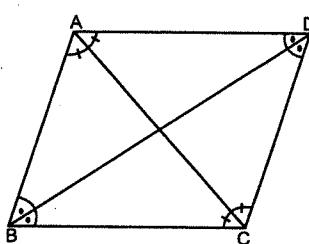
## EŞKENAR DÖRTGEN

\*



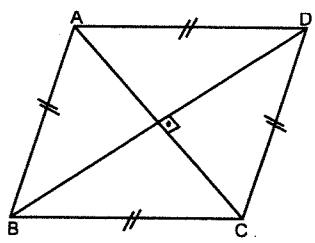
Tüm kenarları eşittir ve paralelkenara ait tüm özelliklerini taşır.

\*



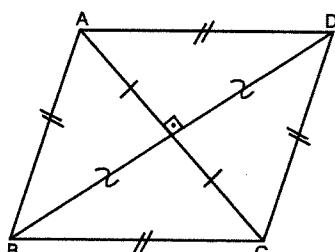
Köşegenler açı ortaydır.

\*



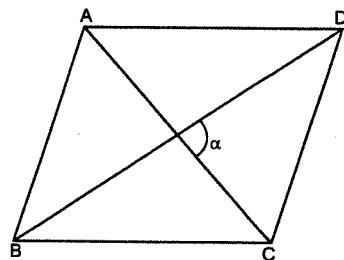
Köşegenler dik kesişir.

\*



$$\text{Alan(ABCD)} = \frac{|AC| \cdot |BD|}{2}$$

1.

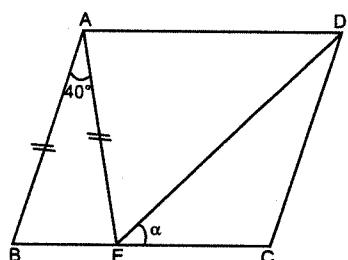


ABCD  
eşkenar  
dörtgen

$$\alpha = ?$$

Cevap: 90

2.

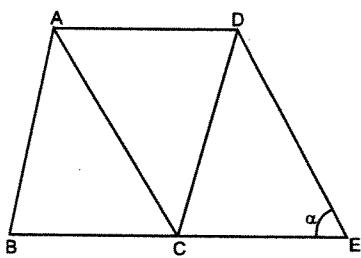


ABCD  
eşkenar  
dörtgen

$$\alpha = ?$$

Cevap: 55

3.

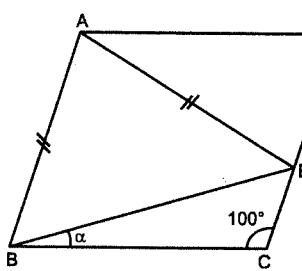


ABCD ve  
ACED  
eşkenar  
dörtgen

$$\alpha = ?$$

Cevap: 60°

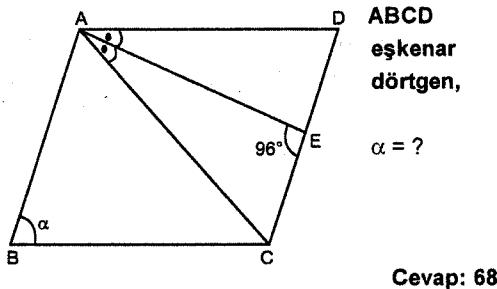
4.



ABCD  
eşkenar  
dörtgen,  
 $\alpha = ?$

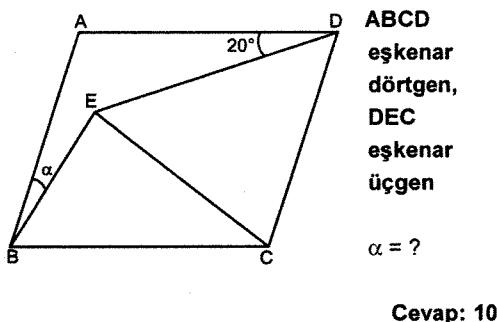
Cevap: 30

5.



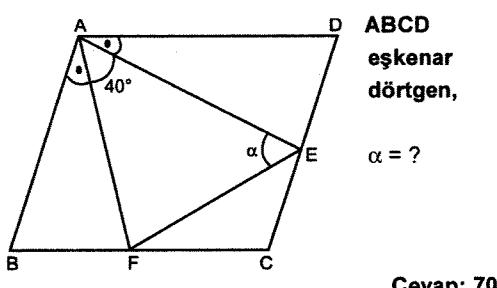
Cevap: 68

6.



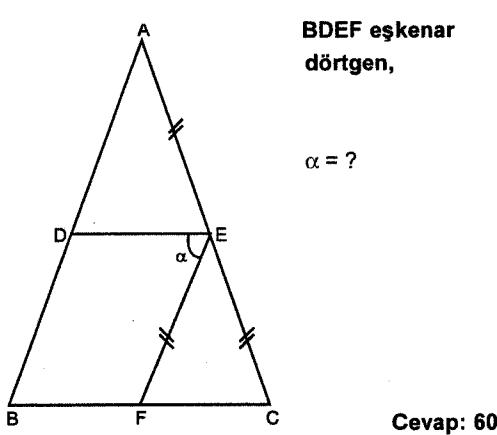
Cevap: 10

7.



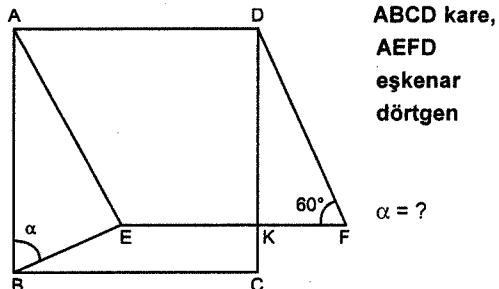
Cevap: 70

8.



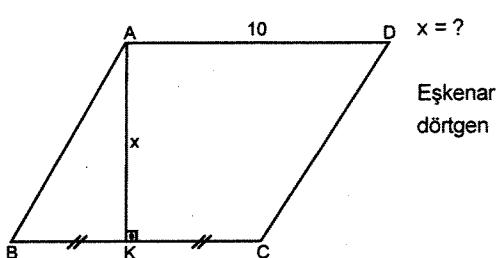
Cevap: 60

9.

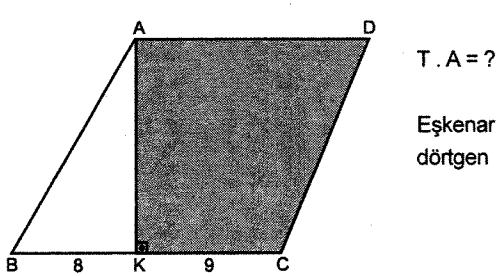


Cevap: 75

10.

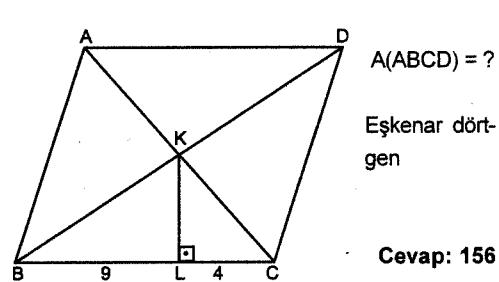
Cevap:  $5\sqrt{3}$ 

11.



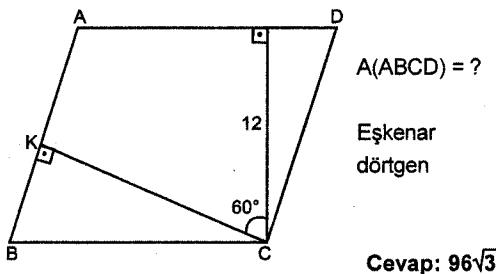
Cevap: 195

12.

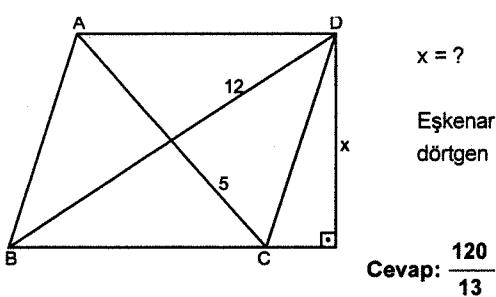


Cevap: 156

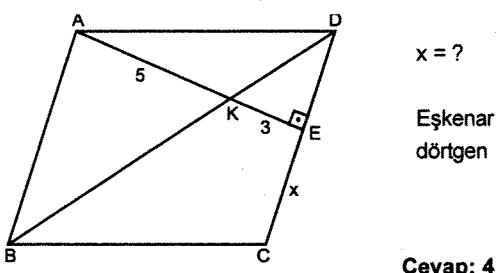
13.



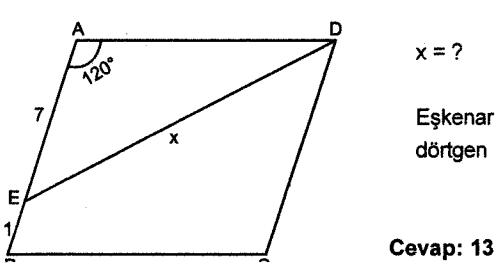
14.



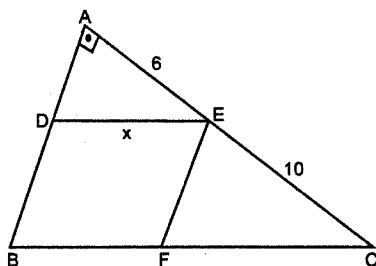
15.



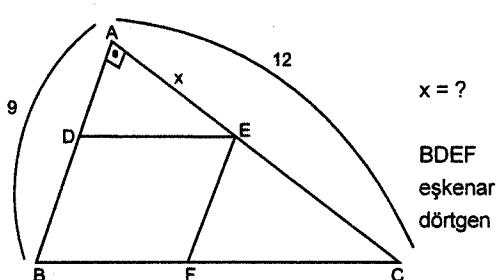
16.



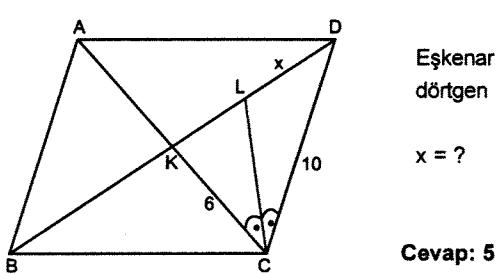
17.



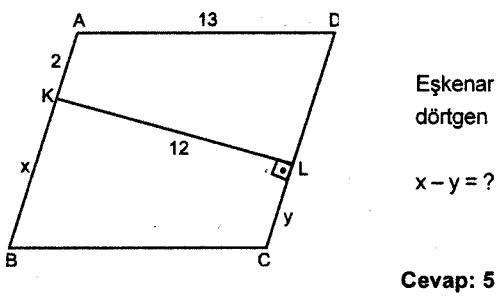
18.



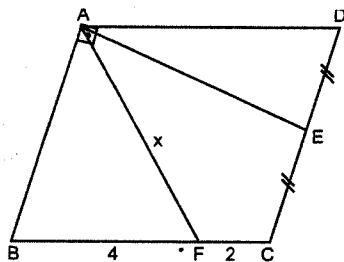
19.



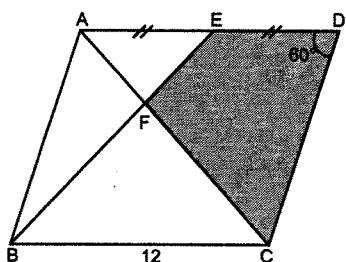
20.



21.

Eşkenar  
dörtgen $x = ?$ Cevap:  $2\sqrt{7}$ 

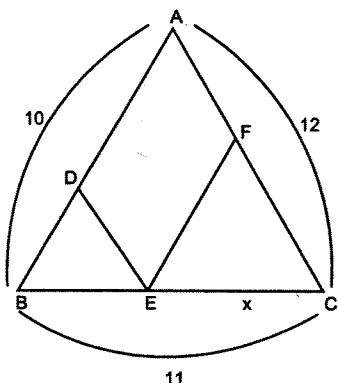
22.



T . A = ?

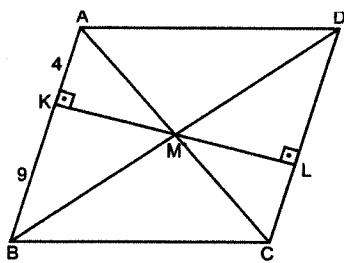
Eşkenar  
dörtgen?Cevap:  $30\sqrt{3}$ 

23.

ADEF  
eşkenar  
dörtgen  
 $x = ?$ 

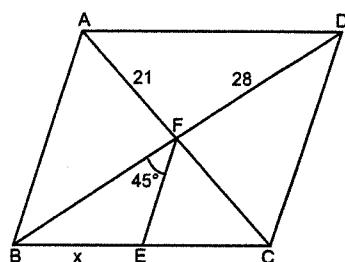
Cevap: 6

24.

Eşkenar  
dörtgen $|KL| = ?$ 

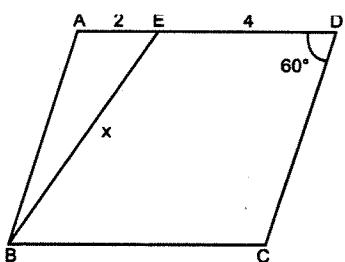
Cevap: 12

25.

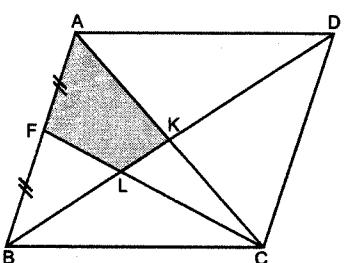
Eşkenar  
dörtgen $x = ?$ 

Cevap: 20

26.

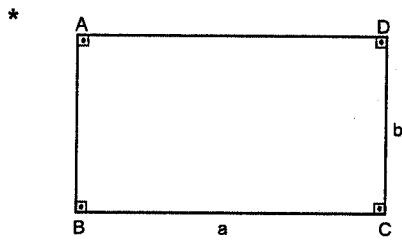
Eşkenar  
dörtgen $x = ?$ Cevap:  $2\sqrt{13}$ 

27.

Eşkenar  
dörtgen $|BD| = 18$  $|AC| = 12$  $T . A = ?$ 

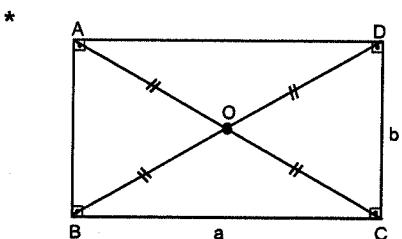
Cevap: 18

## DİKDÖRTGEN

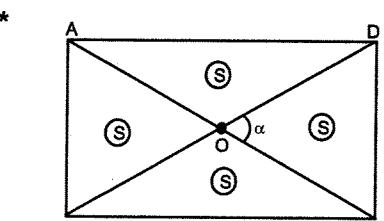


$$\text{Alan(ABCD)} = a \cdot b$$

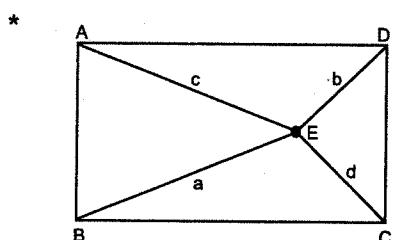
$$\text{Çevre(ABCD)} = 2a + 2b$$



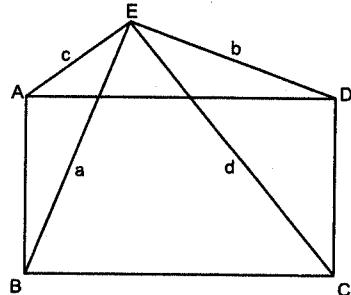
- Dikdörtgende köşegen uzunlukları birbirine eşittir.  
 $|AC| = |BD|$
- O, noktası Dikdörtgenin ağırlık merkezidir.
- Köşegenlerden biri verildiği zaman, diğer köşegeni çizerkeniz yukarıdaki gibi köşegenlerin birbirini ortalağını mutlaka göstermelisiniz.



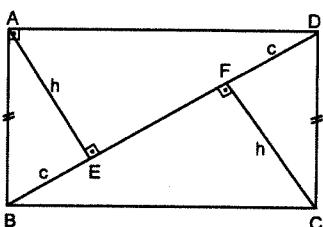
$$\text{Alan(ABCD)} = \frac{|AC| \cdot |BD|}{2} \cdot \sin \alpha$$



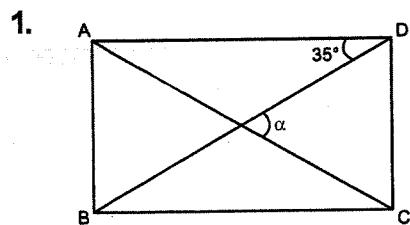
$$(a^2 + b^2 = c^2 + d^2)$$



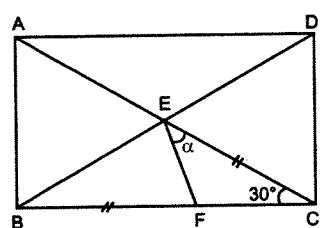
$$(a^2 + b^2 = c^2 + d^2)$$



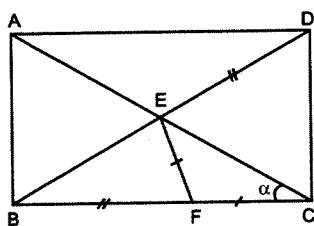
- A ve C köşelerinden köşegene indirilen dikmeler birbirine eşittir.  $|EB| = |FD|$  ve  $|AE| = |FC|$
- Ayrıca şekil içinde öklid bağıntısına dikkat edin.
- Paralelkenara ait bütün özellikler dikdörtgen içinde geçerlidir.
- Bu kuralların olmadığı yerlerde dikmeler ikiden fazla ise orada ( $\alpha$ ,  $\theta$ , 90°) benzerliği vardır. Yani herhangi bir açıya  $\alpha$ , sonra  $\theta$  yazın. Kenarlarında dikkat ederek benzer üçgen, eş üçgen bulmaya çalışın.
- Kelebek benzerliğine dikkat edin.
- Normal alan formülünden çıkmayan sorularda köşegen çizip, köşegenler arasında çıkan  $\alpha$  açısı (30, 45, 60 veya bunların bütünüleyenleri ise) köşegenler çarpımının yarısı çarpı aradaki açının sinüsü ile bu alanı bulabilirsiniz.

 $\alpha = ?$ 

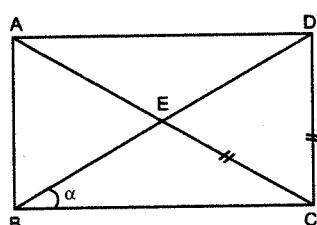
Cevap: 70

 $\alpha = ?$ 

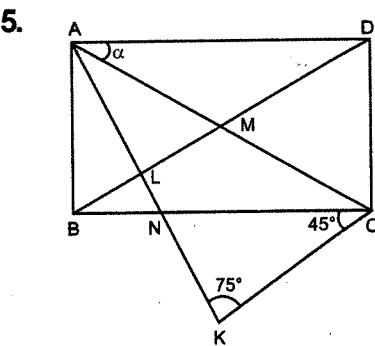
Cevap: 45

 $\alpha = ?$ 

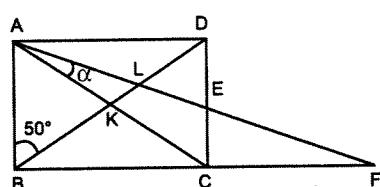
Cevap: 36

 $\alpha = ?$ 

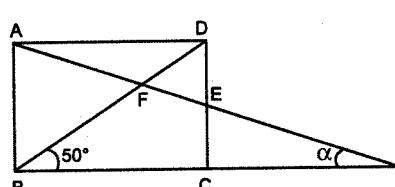
Cevap: 30

 $|AK| = |BD|$  $\alpha = ?$ 

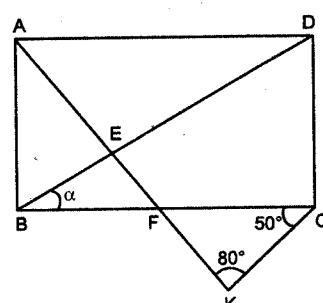
Cevap: 30

 $|BD| = |CF|$  $\alpha = ?$ 

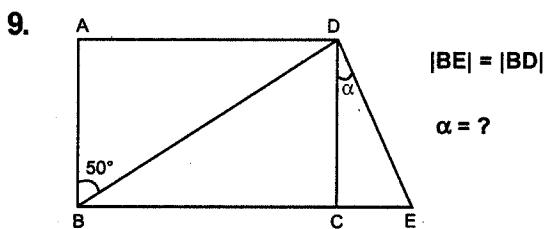
Cevap: 20°

 $|BD| = |CK|$  $\alpha = ?$ 

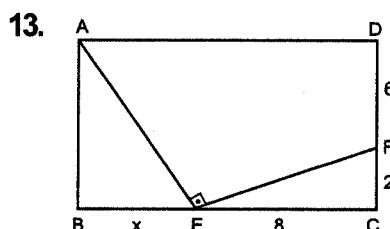
Cevap: 25

 $|BD| = |AK|$  $\alpha = ?$ 

Cevap: 30°

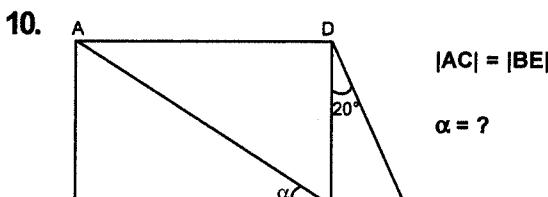


Cevap: 20

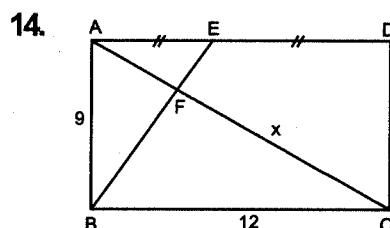


x = ?

Cevap: 2

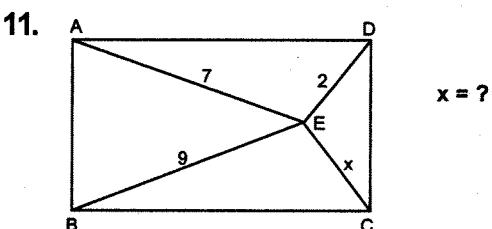


Cevap: 40

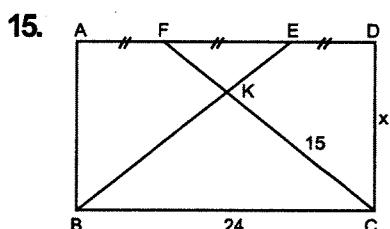


x = ?

Cevap: 10

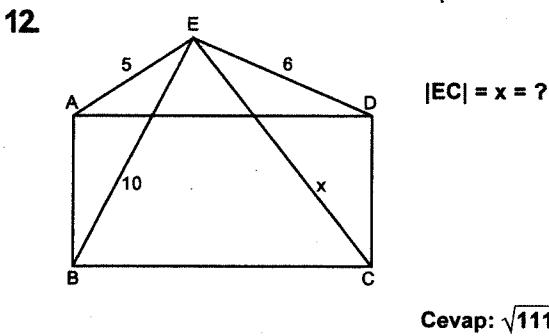
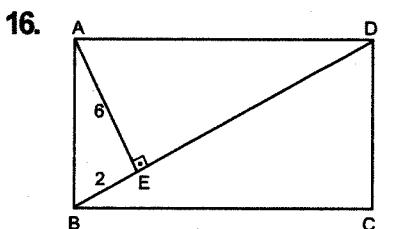


Cevap: 6

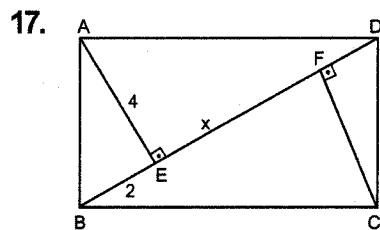


x = ?

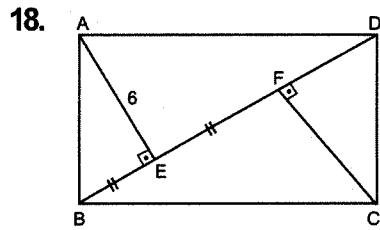
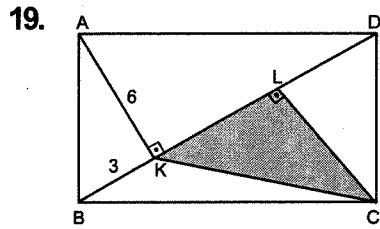
Cevap: 12

Cevap:  $\sqrt{111}$ 

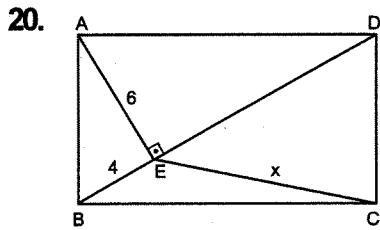
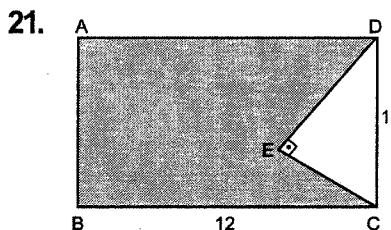
Cevap: 120

 $x = ?$ 

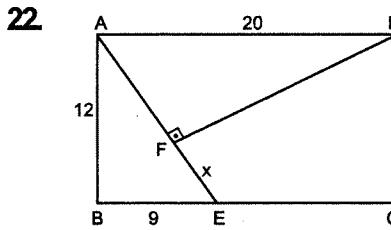
Cevap: 6

 $|BD| = ?$ Cevap:  $9\sqrt{2}$  $T.A = ?$ 

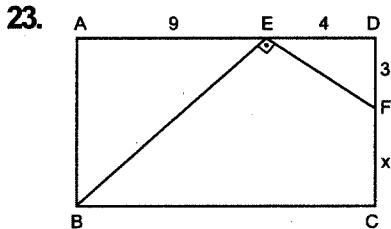
Cevap: 27

 $x = ?$ Cevap:  $\sqrt{61}$  $\mathcal{C}(DEC) = 24$  $T.A = ?$ 

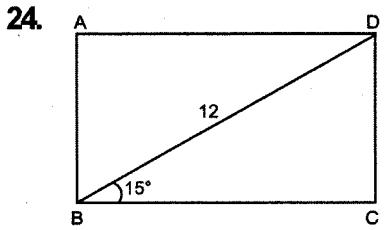
Cevap: 96

 $x = ?$ 

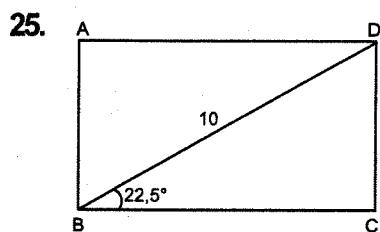
Cevap: 3

 $x = ?$ 

Cevap: 9

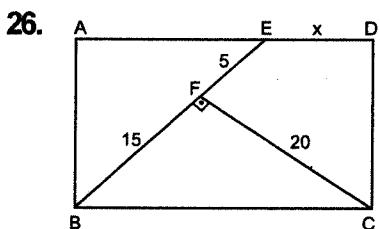
 $A(ABCD) = ?$ 

Cevap: 36



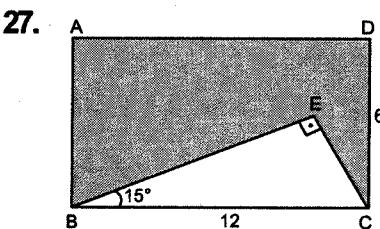
$$A(ABCD) = ?$$

$$\text{Cevap: } 25\sqrt{2}$$



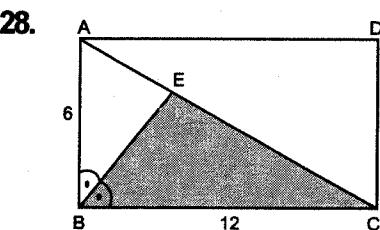
$$x = ?$$

$$\text{Cevap: } 13$$



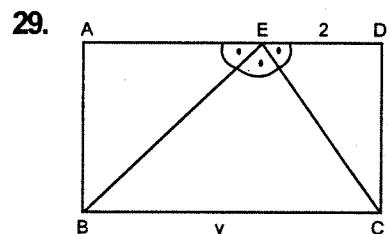
$$T.A = ?$$

$$\text{Cevap: } 54$$



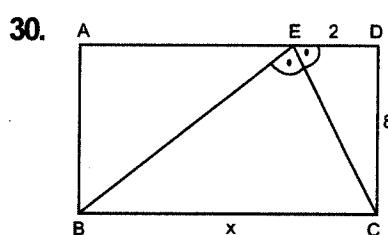
$$T.A = ?$$

$$\text{Cevap: } 24$$



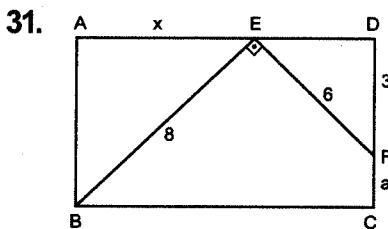
$$x.y = ?$$

$$\text{Cevap: } 8\sqrt{3}$$



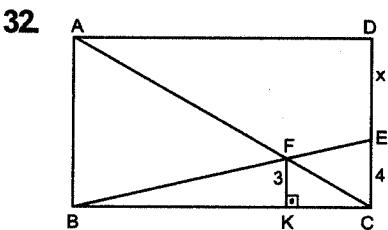
$$x = ?$$

$$\text{Cevap: } 17$$



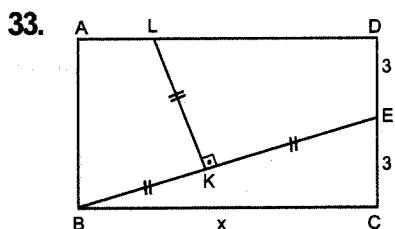
$$x = ?$$

$$\text{Cevap: } 4\sqrt{2}$$



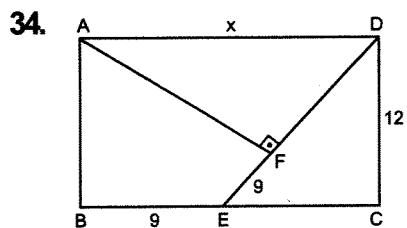
$$x = ?$$

$$\text{Cevap: } 8$$



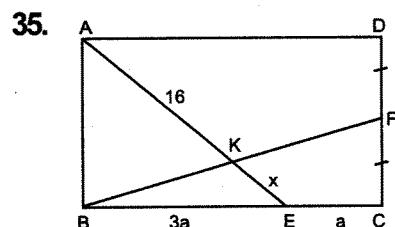
$$x = ?$$

Cevap: 9



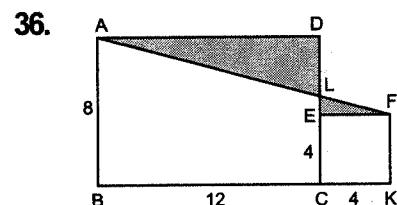
$$x = ?$$

Cevap:  $\frac{25}{2}$



$$x = ?$$

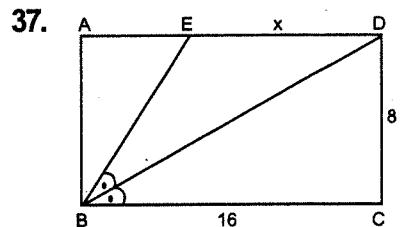
Cevap: 6



ECKF kare

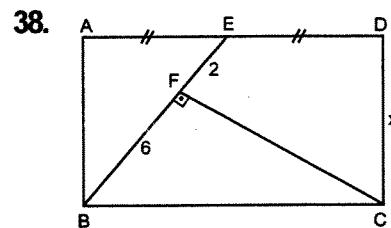
T.A = ?

Cevap: 20



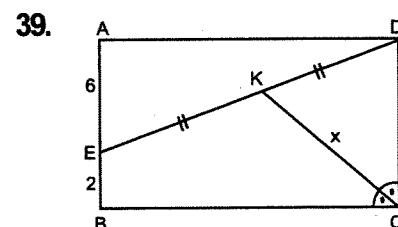
$$x = ?$$

Cevap: 10



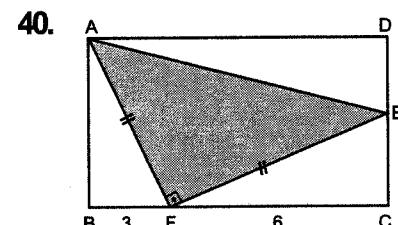
$$x = ?$$

Cevap:  $2\sqrt{10}$



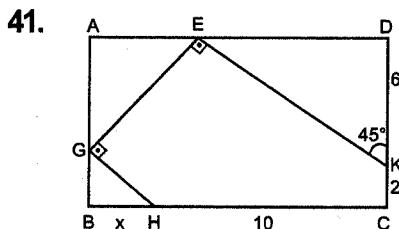
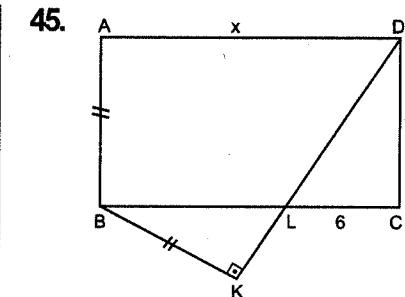
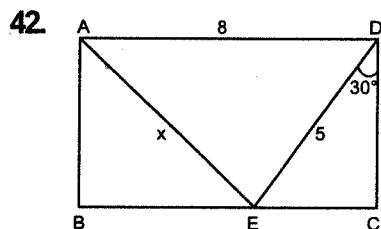
$$x = ?$$

Cevap:  $5\sqrt{2}$

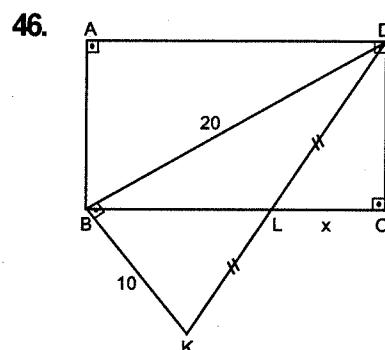
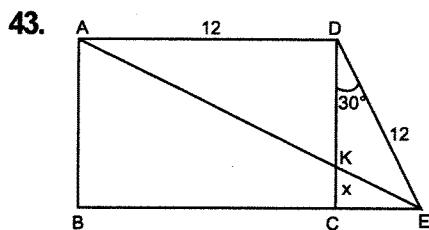
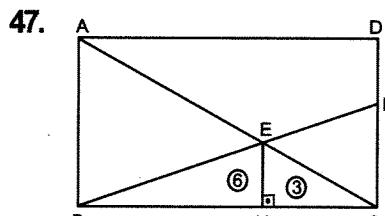


T.A = ?

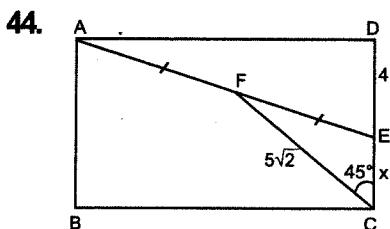
Cevap:  $\frac{45}{2}$

 $x = ?$  $x = ?$  $x = ?$ 

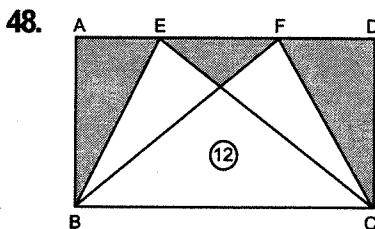
Cevap: 7

 $x = ?$ Cevap:  $3\sqrt{5}$  $x = ?$ Cevap:  $2\sqrt{3}$  $A(ABCD) = ?$ 

Cevap: 54

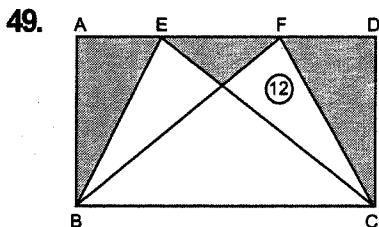
 $x = ?$ 

Cevap: 3



T.A = ?

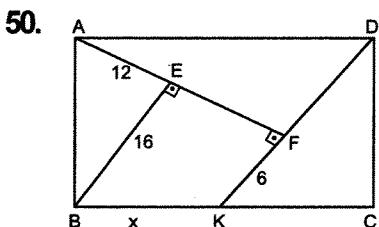
Cevap: 12



$$A(ABCD) = 144$$

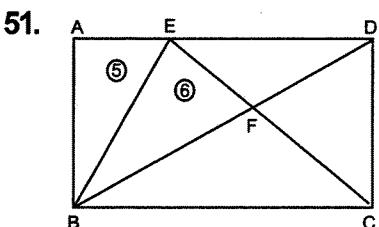
T.A = ?

Cevap: 60



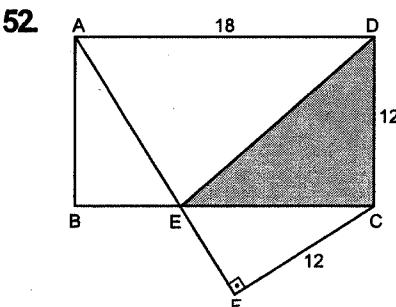
X = ?

Cevap:  $\frac{50}{3}$



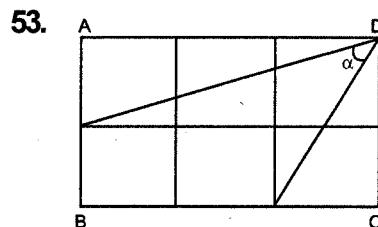
$$A(ABCD) = ?$$

Cevap: 30



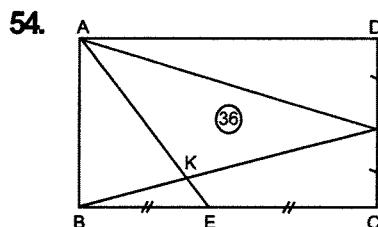
T.A = ?

Cevap: 78



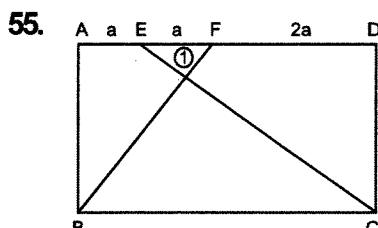
$\alpha = ?$

Cevap: 45



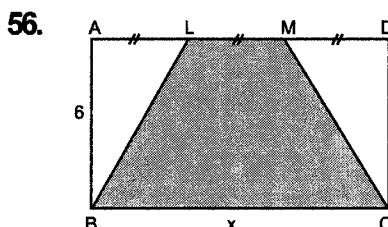
$$A(ABCD) = ?$$

Cevap: 120



$$A(ABCD) = ?$$

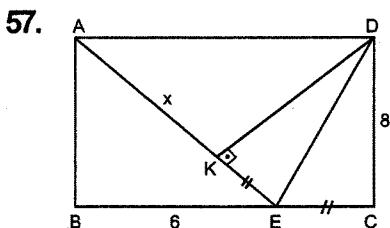
Cevap: 40



$$A(BCML) = 40$$

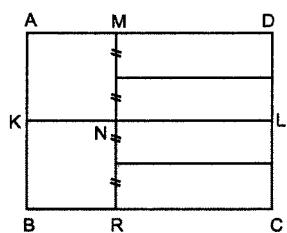
$x = ?$

Cevap: 10



$x = ?$

Cevap: 6

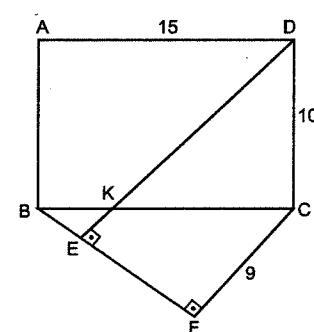


Şekildeki dikdörtgen ve karelerin çevreleri eşit olup

$A(ABCD) = 80$

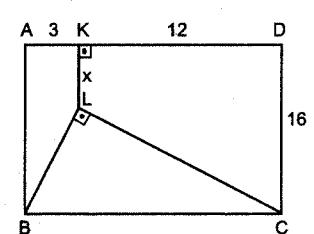
$C(ABCD) = ?$

Cevap: 36

ABCD  
dikdörtgen

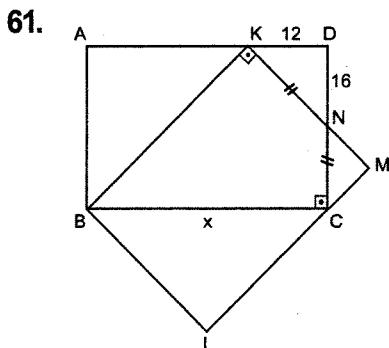
$|ED| = ?$

Cevap: 17

ABCD  
dikdörtgen

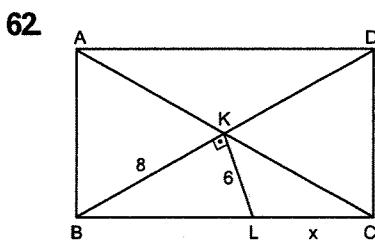
$x = ?$

Cevap: 10

ABCD ve BKML  
dikdörtgen

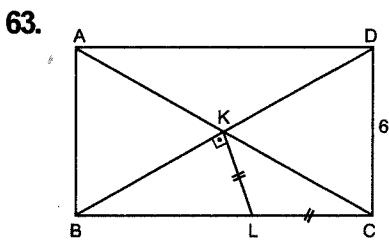
$x = ?$

Cevap: 60

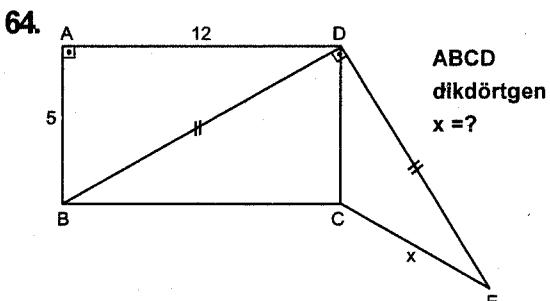


$x = ?$

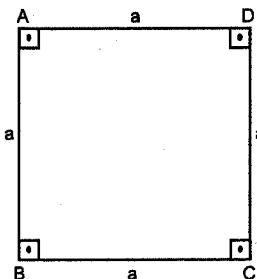
Cevap: 2,8



Alan(ABCD)=?

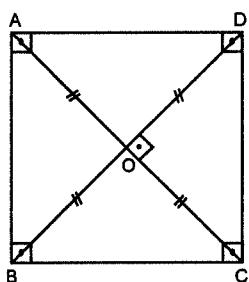
Cevap:  $36\sqrt{3}$ ABCD  
dikdörtgen  
 $x = ?$ Cevap:  $\sqrt{74}$

## KARE



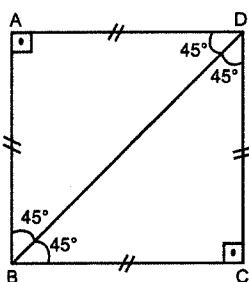
$$\text{Alan(ABCD)} = a^2$$

$$\text{Çevre(ABCD)} = 4a$$



Köşegenlerin kesim noktası **ağırlık merkezidir.**

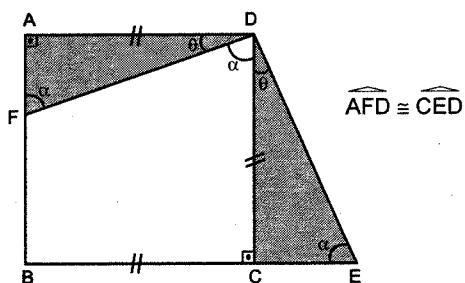
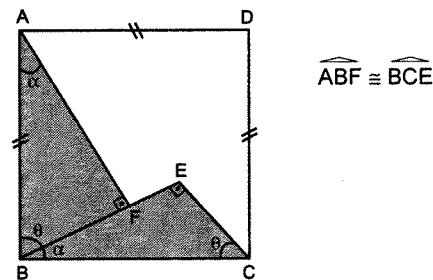
Köşegenler birbirini ortalar birbirine eşit ve dik keserler.



Kare sorularında köşegenlerden biri verilirse orada ikizkenar dik üçgen vardır.  $45^\circ$  leri mutlaka şekilde gösterin. Yazabildığınız kadar  $45^\circ - 45^\circ - 90^\circ$  yazın.

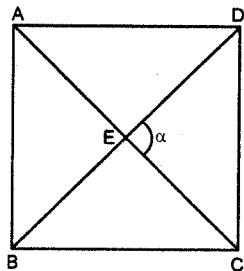
Soruların birçoğunda köşegenlerden biri verildiğinde diğerini kendimiz çizip köşegenlerin kesiştiği yerde  $90^\circ$  olduğunu gösterdiğimiz zaman özel üçgenler çıkıyor. Buradan soruyu rahat bir şekilde çözebiliriz.

- Yukarıdaki gibi soru çıkmıyorsa benzerliği deneyin.
- $90^\circ$ lerin çok olduğu yerde açılarla isim takın ( $\alpha, \theta$ ) gibi... sonra böyle çözmeye çalışın. Buradanda çıkmıyorsa Öklid bağıntısına dikkat edin. Ne bileyim Kelebek benzerliğine bakın. Ama mutlaka şekilde oynayın.
- Alan sorularında S'leme (okunuşu esleme) yapın. Benzer iki üçgenin alanları oranı, benzerlik oranının karesine eşittir. Kuralını yapmaya çalışın.
- Karenin tüm kenarlarının eşit olduğunu gösterin ve karenin bir kenarını görecek şekilde bir çizgi uzatıp eş üçgenlerden soruyu çözün.



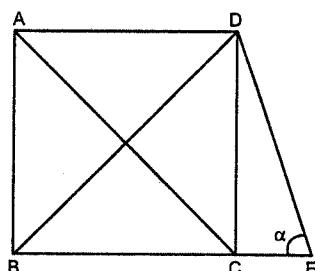
gibi

1.

 $\alpha = ?$ 

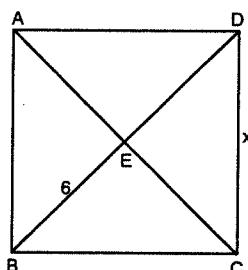
Cevap: 90

5.

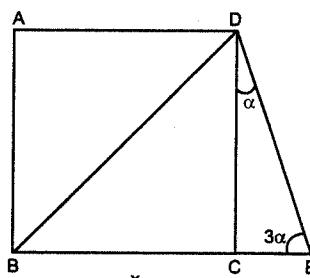
 $|AC| = |BE|$  $\alpha = ?$ 

Cevap: 67,5

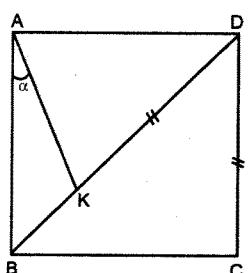
2.

 $x = ?$ Cevap:  $6\sqrt{2}$ 

6.

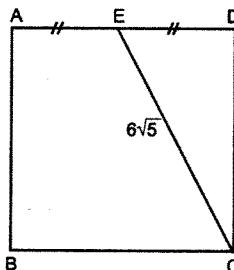
 $A(ABCD) = 64$  $x = ?$ Cevap:  $8\sqrt{2}$ 

3.

 $\alpha = ?$ 

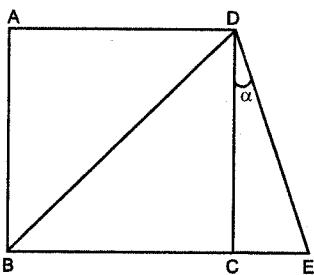
Cevap: 22,5

7.

 $A(ABCD) = ?$ 

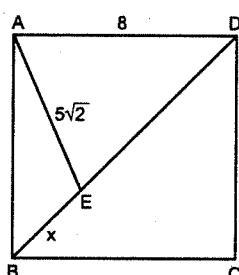
Cevap: 144

4.

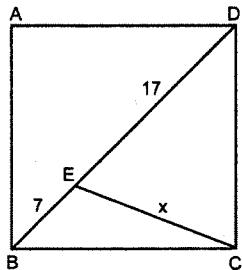
 $|BD| = |BE|$  $\alpha = ?$ 

Cevap: 22,5

8.

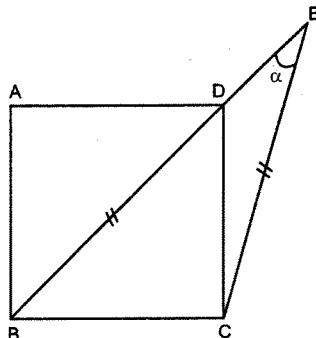
 $x = ?$ Cevap:  $\sqrt{2}$

9.



$x = ?$

13.

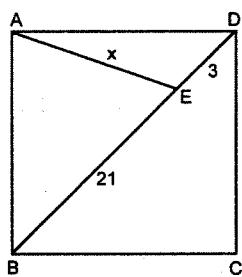


$|BD| = |EC|$

$\alpha = ?$

Cevap: 30

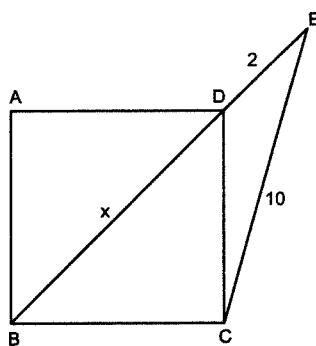
10.



$x = ?$

Cevap: 15

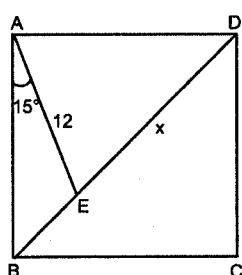
14.



$x = ?$

Cevap: 12

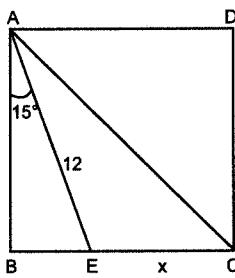
11.



$x = ?$

Cevap:  $6\sqrt{3} + 6$ 

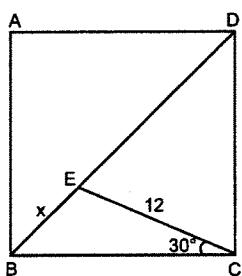
15.



$x = ?$

Cevap:  $6\sqrt{2}$ 

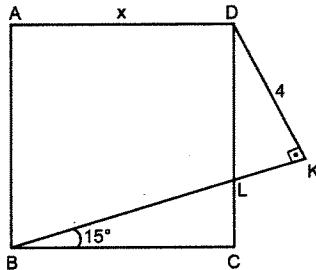
12.



$x = ?$

Cevap:  $6\sqrt{2}$ 

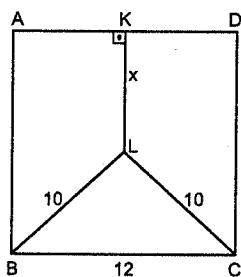
16.



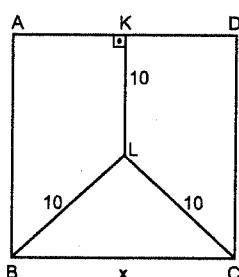
$x = ?$

Cevap:  $4\sqrt{2}$

17.

 $x = ?$ 

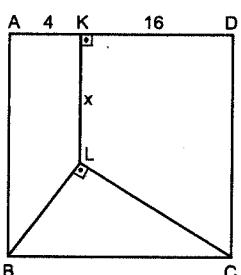
21.

 $x = ?$ 

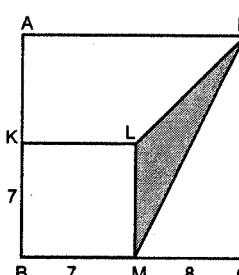
Cevap: 4

Cevap: 16

18.

 $x = ?$ 

22.

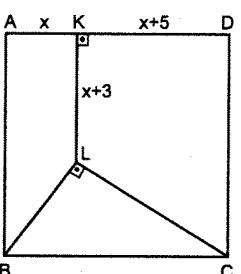


T.A = ?

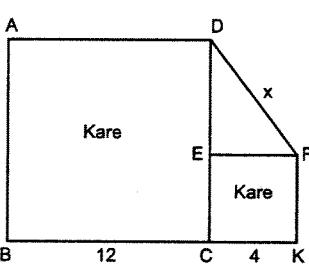
Cevap: 12

Cevap: 28

19.

 $x = ?$ 

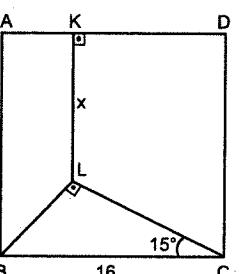
23.

 $x = ?$ 

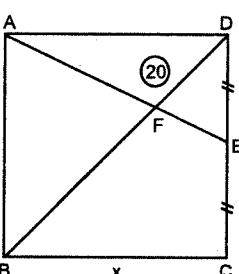
Cevap: 4

Cevap:  $4\sqrt{5}$ 

20.

 $x = ?$ 

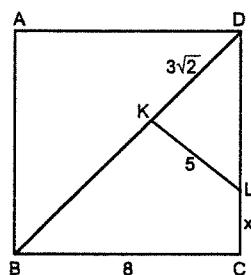
24.

 $x = ?$ 

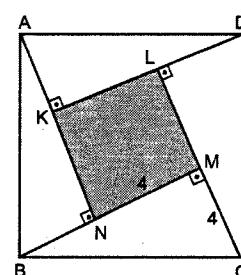
Cevap: 12

Cevap:  $2\sqrt{30}$

25.

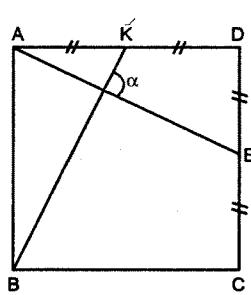
 $x = ?$ 

29.

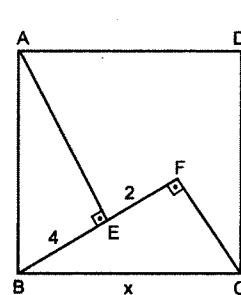
 $T.A = ?$ 

Cevap: 1

26.

 $\alpha = ?$ 

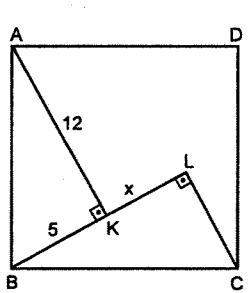
30.

 $x = ?$ 

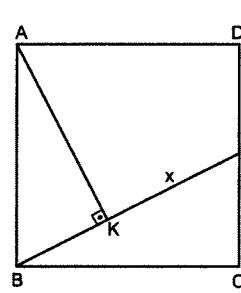
Cevap: 90

Cevap:  $2\sqrt{13}$ 

27.

 $x = ?$ 

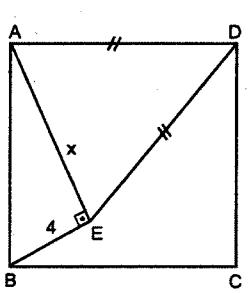
31.

 $x = ?$ 

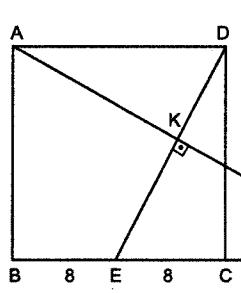
Cevap: 7

Cevap:  $3\sqrt{5}$ 

28.

 $x = ?$ 

32.

 $x = ?$ 

Cevap: 8

Cevap: 16

33.

**Cevap: 4**

34.

**Cevap: 30**

35.

$x = ?$

**Cevap: 9**

36.

Cevap:  $4\sqrt{10}$

37.

**Cevap:12**

38.

**Cevap: 1**

- 

Cevap: 65

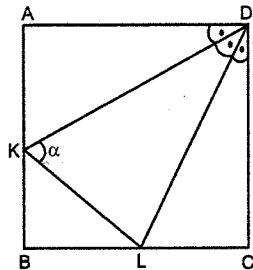
- 

T<sub>A</sub> = 20

$$A(ABCD) = ?$$

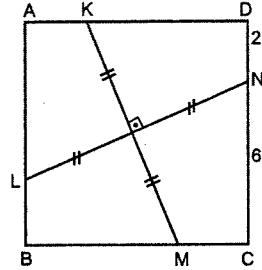
Cevap: 48

41.



$\alpha = ?$

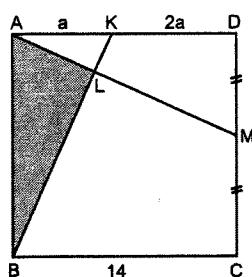
45.



$|KM| = ?$

Cevap:  $4\sqrt{5}$ 

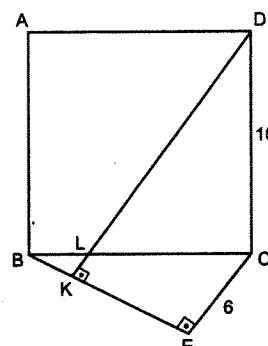
42.



$T.A = ?$

Cevap: 28

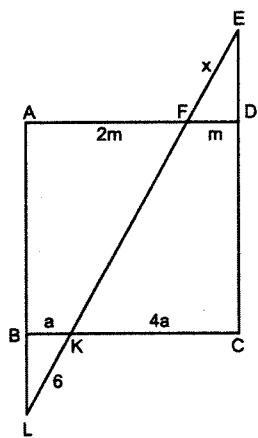
46.



$|DK| = ?$

Cevap: 14

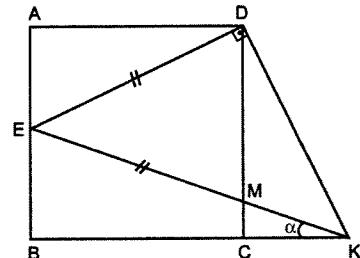
43.



$x = ?$

Cevap: 10

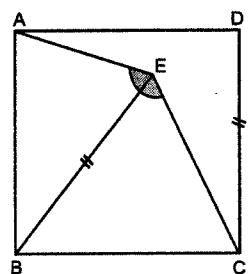
47.



$\alpha = ?$

Cevap: 22,5

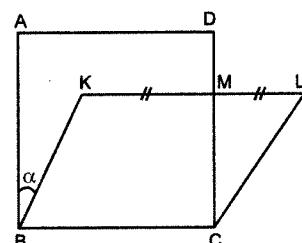
44.



$m(\widehat{AEC}) = ?$

Cevap: 135

48.

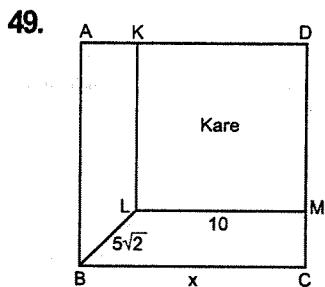


KBCL eşkenar dörtgen

ABCD kare

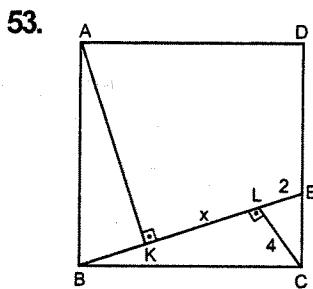
$\alpha = ?$

Cevap: 30



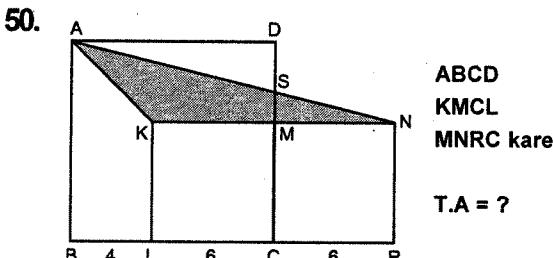
$x = ?$   
ABCD kare

Cevap: 15



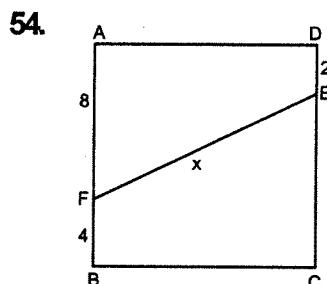
$x = ?$   
ABCD kare

Cevap: 4



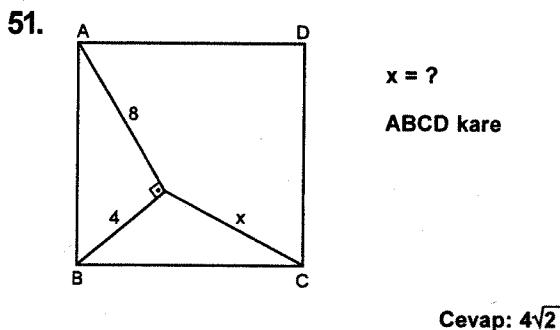
ABCD  
KMCL  
MNRC kare  
T.A = ?

Cevap: 24



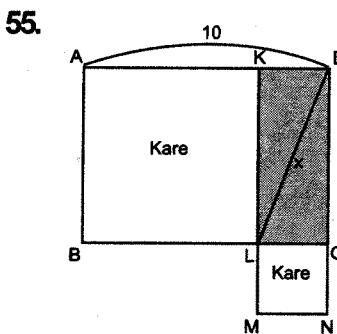
$x = ?$   
ABCD kare

Cevap:  $6\sqrt{5}$



$x = ?$   
ABCD kare

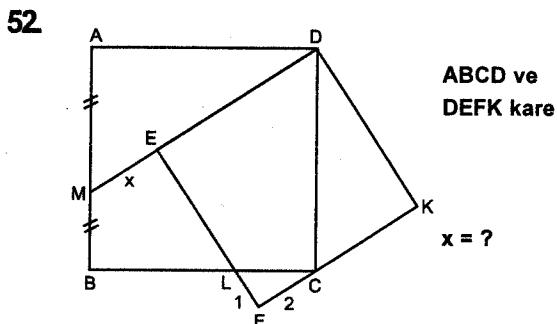
Cevap:  $4\sqrt{2}$



T.A = 18  
ABLK ve  
LMNC kare

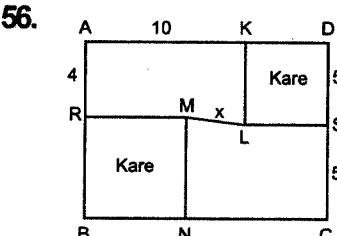
$x = ?$

Cevap: 8



ABCD ve  
DEFK kare

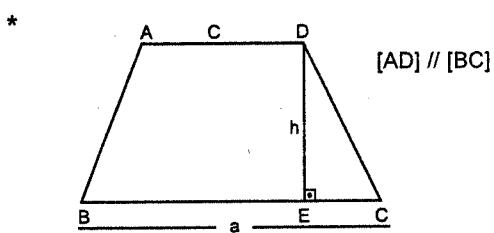
Cevap: 1



ABCD dikdörtgen  
 $x = ?$

Cevap:  $\sqrt{17}$

## YAMUK

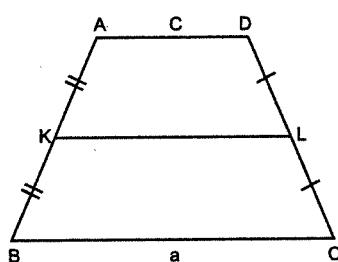


$$\text{Alan(ABCD)} = \frac{(a+c) \cdot h}{2}$$

$|AD| = c$  : üst taban

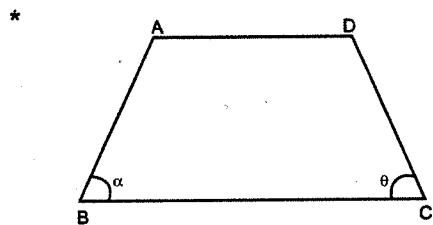
$|BC| = a$  : alt taban

$|DE| = h$  : yükseklik



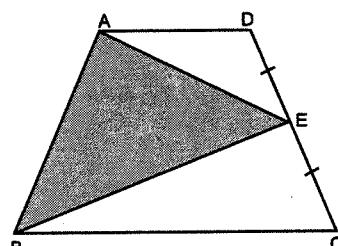
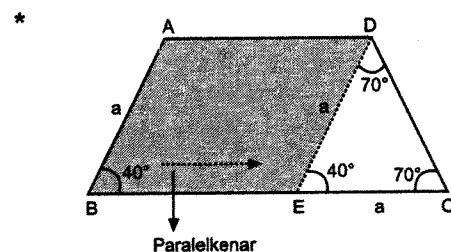
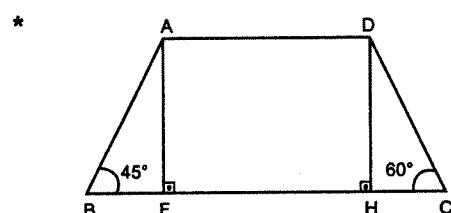
$$|KL| : \text{orta tabandır} = \frac{a+c}{2}$$

$$(\text{Alan(ABCD)}) = \text{ortataban} \times \text{yükseklik}$$

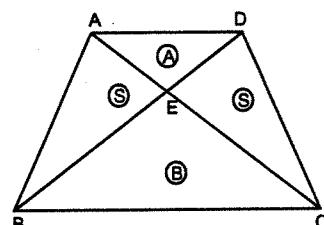


$\alpha, \theta$  tanıdık açılar ise ( $30^\circ, 45^\circ, 60^\circ$ ) gibi bu açıların karşısına dik indirilir.

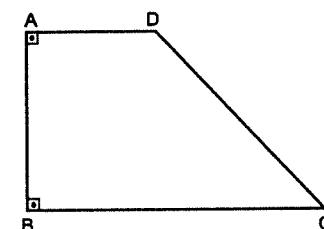
Tanıdık değilse D'den veya A'dan paralel çizeriz.  
Paralelkenar olur.



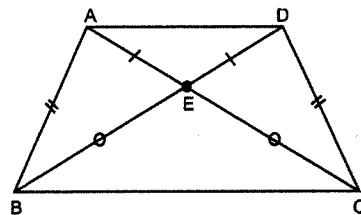
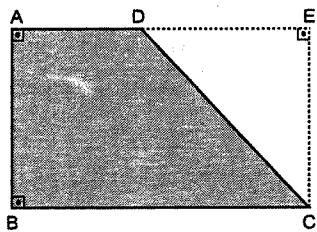
$$\text{Taralı Alan} = \frac{\text{A(ABCD)}}{2}$$



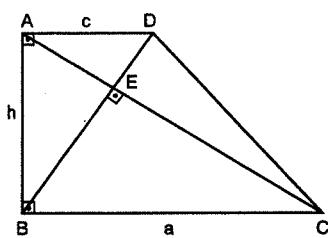
$$A \cdot B = S^2$$



Sade Dik yamuk sorularında şekli dikdörtgene çevirir.

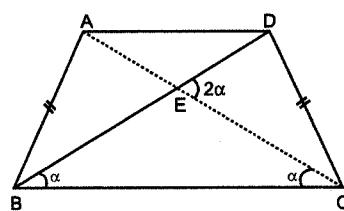


İkizkenar yamukta köşegenler birbirine eşit ve alta ve üstte iki tane ikizkenar üçgen oluşur.

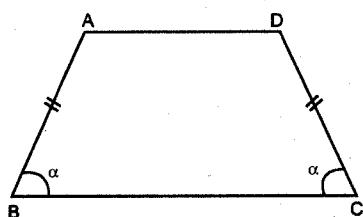


Köşegenleri dik keşisen dik yamuktan

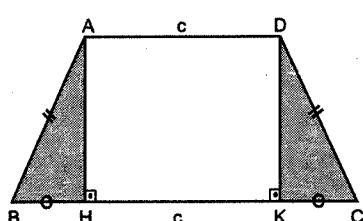
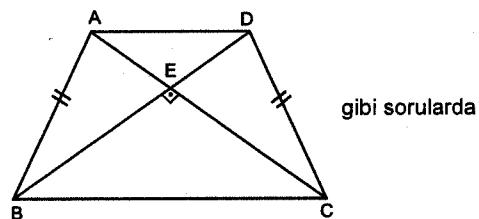
$$h^2 = a \cdot c \quad \text{dir.}$$



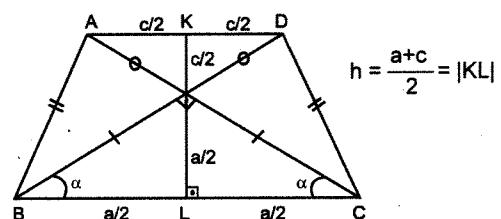
$$\text{Alan(ABCD)} = \frac{|AC| \cdot |BD|}{2} \cdot \sin 2\alpha$$



ABCD ikizkenar yamuktur.  
 $|AB| = |DC|$  ve  $m(\widehat{B}) = m(\widehat{C}) = \alpha$



Tarali üçgenler eşittir.

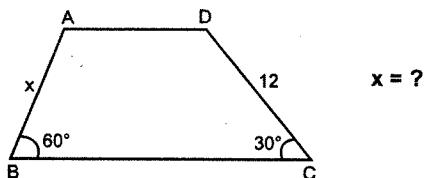


$$\text{Alan(ABCD)} = \frac{(a+c) \cdot h}{2}$$

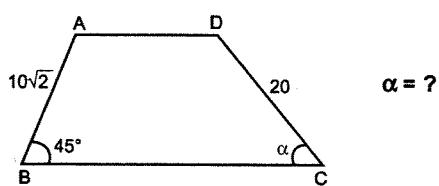
$$= \left( \frac{a+c}{2} \right) \left( \frac{a+c}{2} \right) = h^2$$

Yani ikizkenar yamukta köşegenler dik kestiği zaman yüksekliğin karesi alana eşittir.

1.

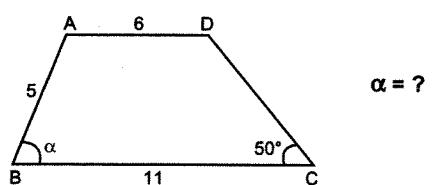
 $x = ?$ Cevap:  $4\sqrt{3}$ 

2.

 $\alpha = ?$ 

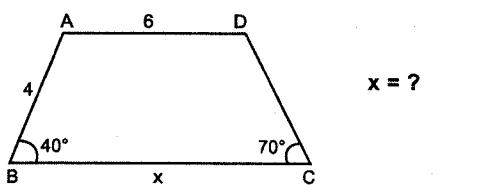
Cevap: 30

3.

 $\alpha = ?$ 

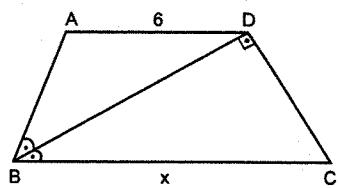
Cevap: 80

4.

 $x = ?$ 

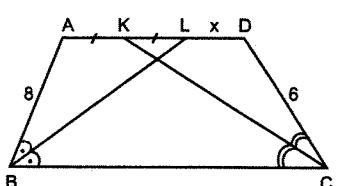
Cevap: 10

5.

 $x = ?$ 

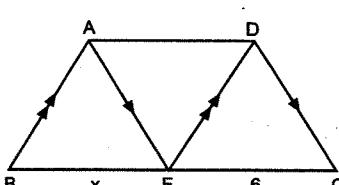
Cevap: 12

6.

 $x = ?$ 

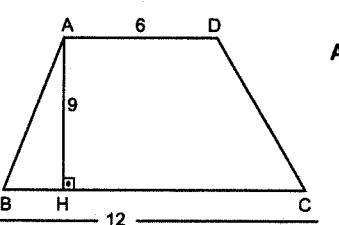
Cevap: 2

7.

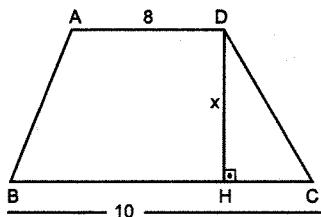
 $x = ?$ 

Cevap: 6

8.

 $A(ABCD) = ?$ 

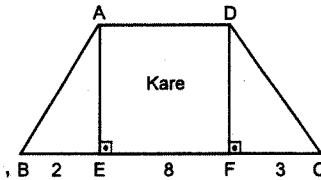
Cevap: 81

**9.**

$$A(ABCD) = 54$$

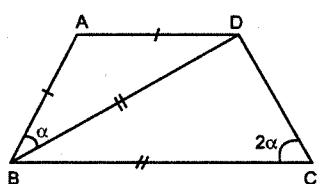
$$x = ?$$

Cevap: 6

**13.**

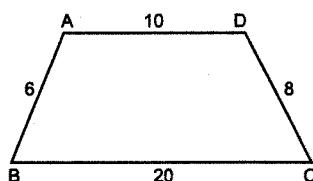
$$A(ABCD) = ?$$

Cevap: 84

**10.**

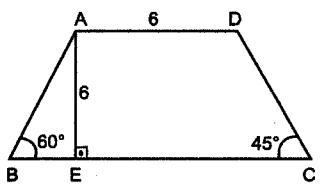
$$\alpha = ?$$

Cevap: 36

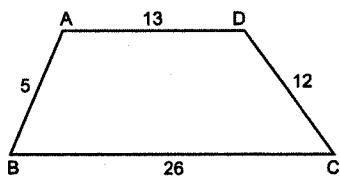
**14.**

$$A(ABCD) = ?$$

Cevap: 72

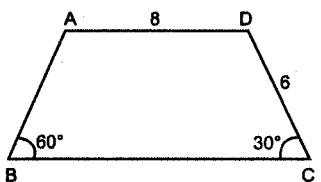
**11.**

$$A(ABCD) = ?$$

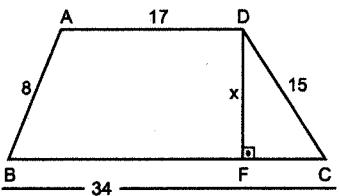
Cevap:  $54 + 6\sqrt{3}$ **15.**

$$A(ABCD) = ?$$

Cevap: 90

**12.**

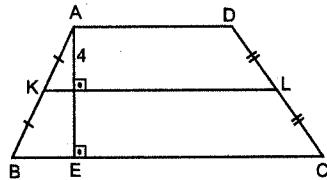
$$A(ABCD) = ?$$

Cevap:  $24 + 6\sqrt{3}$ **16.**

$$x = ?$$

$$\text{Cevap: } \frac{120}{17}$$

17.

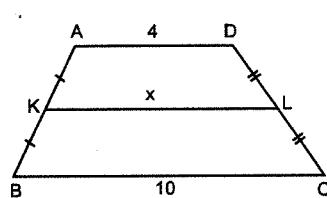


$$|KL| = 12$$

$$A(ABCD) = ?$$

Cevap: 96

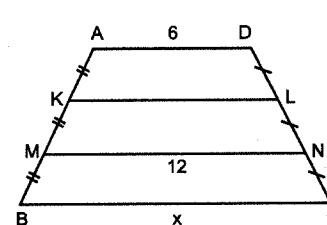
18.



$$x = ?$$

Cevap: 7

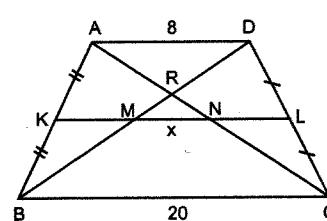
19.



$$x = ?$$

Cevap: 15

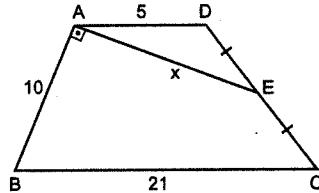
20.



$$x = ?$$

Cevap: 6

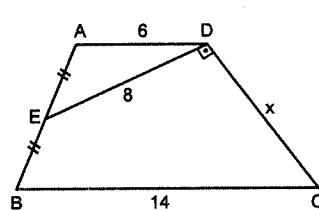
21.



$$x = ?$$

Cevap: 12

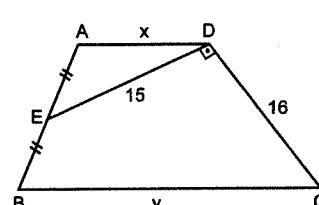
22.



$$x = ?$$

Cevap: 12

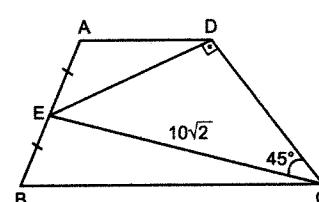
23.



$$y + x = ?$$

Cevap: 34

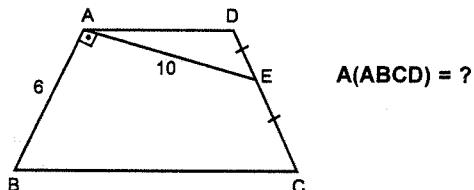
24.



$$A(ABCD) = ?$$

Cevap: 100

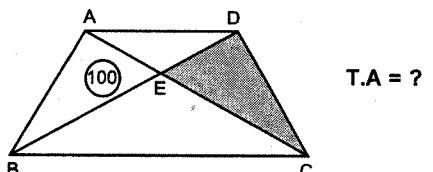
25.



$$A(ABCD) = ?$$

Cevap: 60

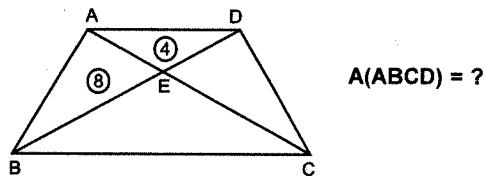
26.



$$T.A = ?$$

Cevap: 100

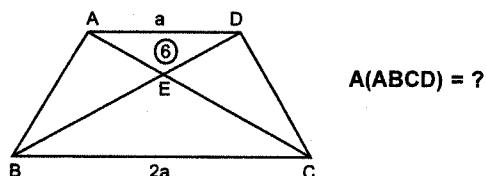
27.



$$A(ABCD) = ?$$

Cevap: 36

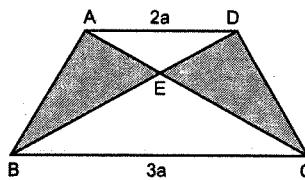
28.



$$A(ABCD) = ?$$

Cevap: 54

29.

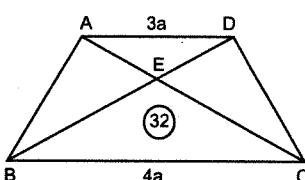


$$A(ABCD) = 100$$

$$T.A = ?$$

Cevap: 48

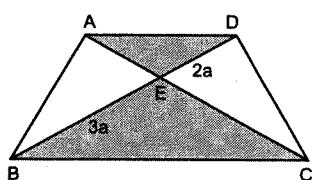
30.



$$A(ABCD) = ?$$

Cevap: 98

31.



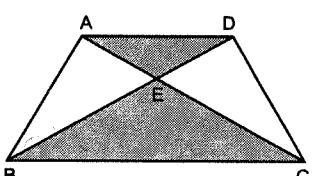
$$3|DE| = 2|EB|$$

$$A(ABCD) = 200$$

$$T.A = ?$$

Cevap: 104

32.



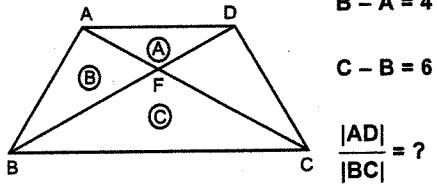
$$T.A = 125$$

$$A(ABCD) = 225$$

$$\frac{|AD|}{|BC|} = ?$$

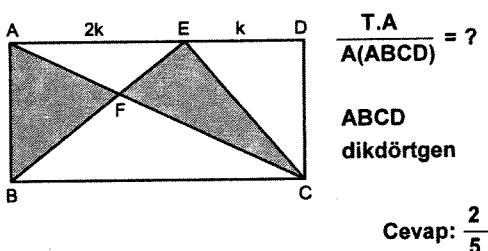
Cevap:  $\frac{1}{2}$

33.



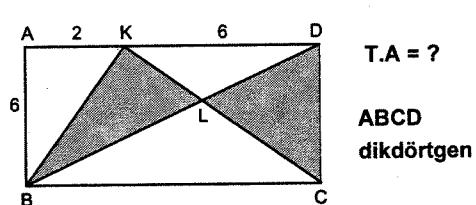
$$\text{Cevap: } \frac{2}{3}$$

34.



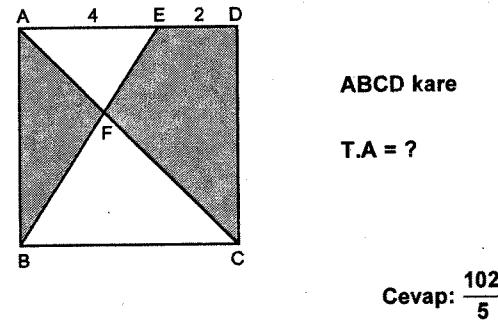
$$\text{Cevap: } \frac{2}{5}$$

35.



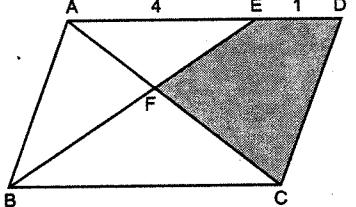
$$\text{Cevap: } \frac{144}{7}$$

36.



$$\text{Cevap: } \frac{102}{5}$$

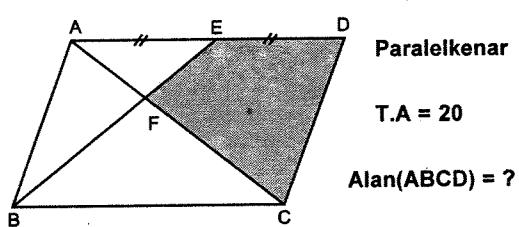
37.



$$\frac{T.A.}{A(ABCD)} = ?$$

$$\text{Cevap: } \frac{29}{90}$$

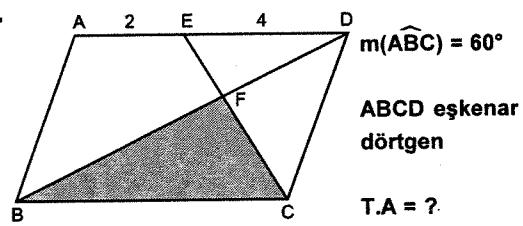
38.



$$\text{Alan}(ABCD) = ?$$

$$\text{Cevap: } 48$$

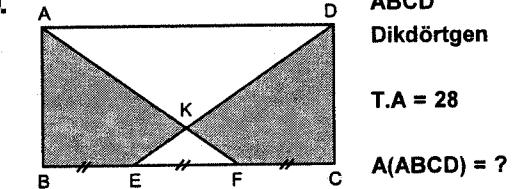
39.



$$T.A. = ?$$

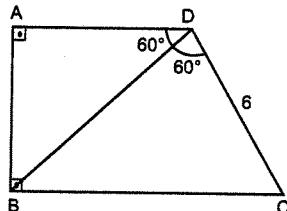
$$\text{Cevap: } \frac{27\sqrt{3}}{5}$$

40.



$$\text{Cevap: } 48$$

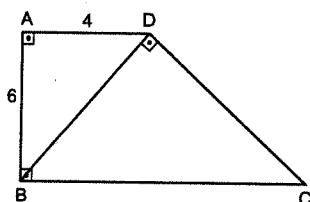
41.



$$A(ABCD) = ?$$

$$\text{Cevap: } \frac{27\sqrt{3}}{2}$$

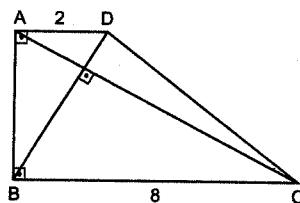
42.



$$A(ABCD) = ?$$

$$\text{Cevap: } 51$$

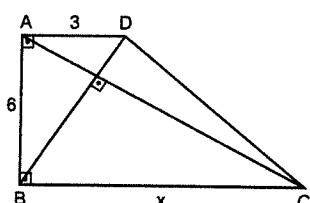
43.



$$A(ABCD) = ?$$

$$\text{Cevap: } 20$$

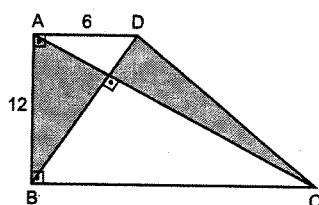
44.



$$x = ?$$

$$\text{Cevap: } 12$$

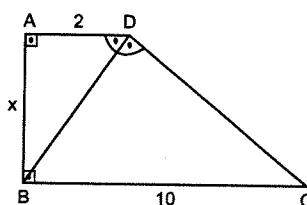
45.



$$T.A = ?$$

$$\text{Cevap: } \frac{288}{5}$$

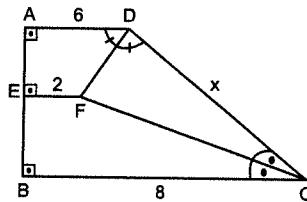
46.



$$x = ?$$

$$\text{Cevap: } 6$$

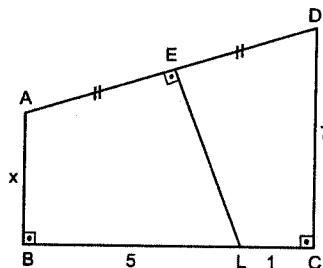
47.



$$x = ?$$

$$\text{Cevap: } 10$$

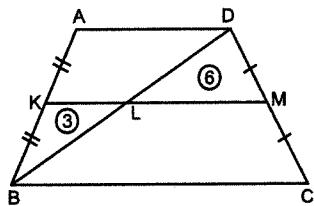
48.



$$x = ?$$

$$\text{Cevap: } 5$$

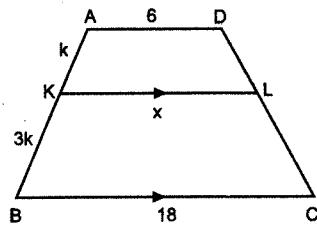
49.



$$A(ABCD) = ?$$

Cevap: 36

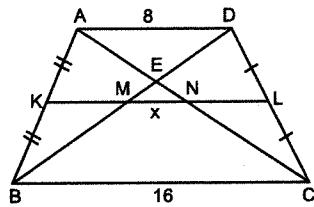
53.



$$x = ?$$

Cevap: 9

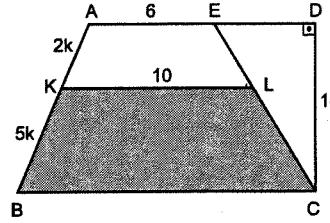
50.



$$x = ?$$

Cevap: 4

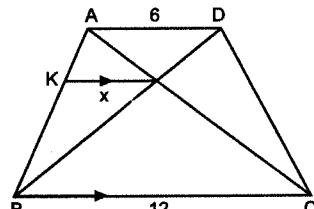
54.



$$T.A = ?$$

Cevap: 150

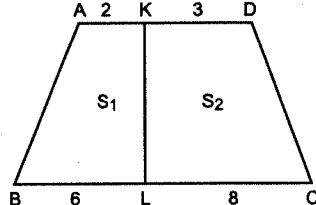
51.



$$x = ?$$

Cevap: 4

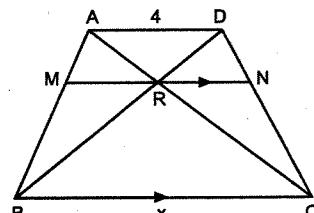
55.



$$\frac{S_1}{S_2} = ?$$

Cevap:  $\frac{8}{11}$ 

52.

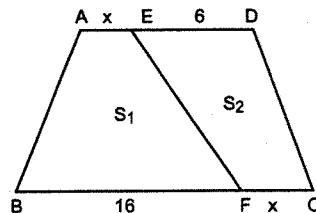


$$|MN| = 6$$

$$x = ?$$

Cevap: 12

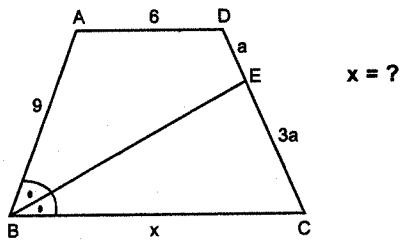
56.



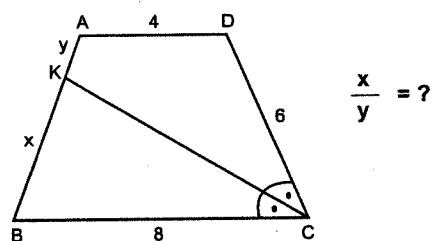
$$\frac{S_1}{S_2} = \frac{5}{3}$$

$$x = ?$$

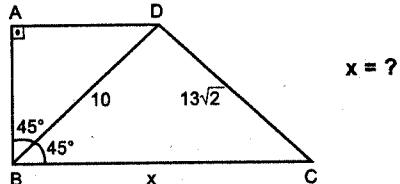
Cevap: 9

**57.**

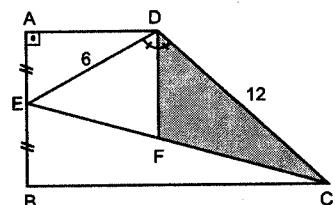
$x = ?$

**Cevap: 9****58.**

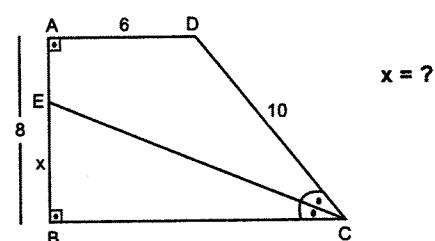
$\frac{x}{y} = ?$

**Cevap: 4****61.**

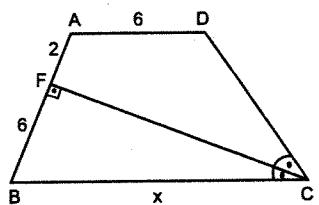
$x = ?$

**Cevap:  $17\sqrt{2}$** **62.**

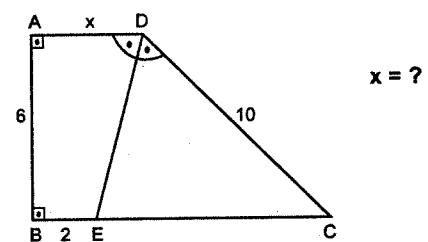
$\frac{T.A}{A(ABCD)} = ?$

**Cevap:  $\frac{1}{3}$** **59.**

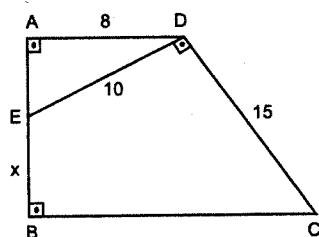
$x = ?$

**Cevap: 6****63.**

$x = ?$

**Cevap: 18****60.**

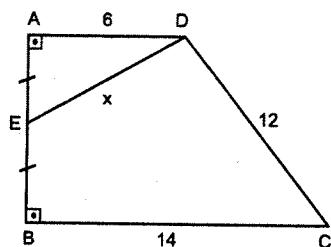
$x = ?$

**Cevap: 4****64.**

$x = ?$

**Cevap: 6**

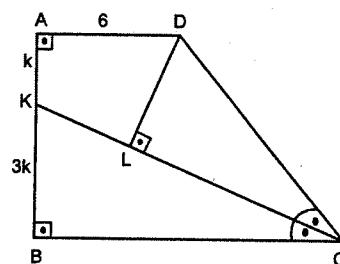
65.



$x = ?$

Cevap:  $2\sqrt{14}$ 

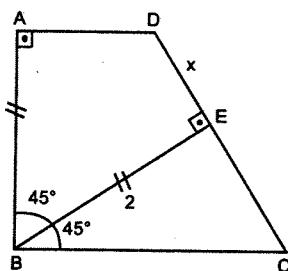
69.



$\frac{|KL|}{|KC|} = ?$

Cevap:  $\frac{1}{3}$ 

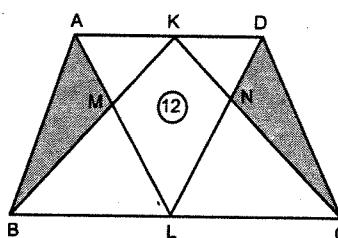
66.



$x = ?$

Cevap:  $2\sqrt{2} - 2$ 

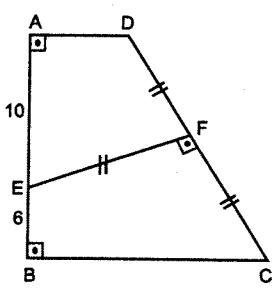
70.



$T.A = ?$

Cevap: 12

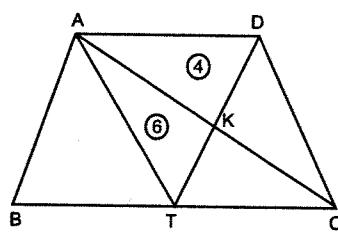
67.



$A(ABCD) = ?$

Cevap: 128

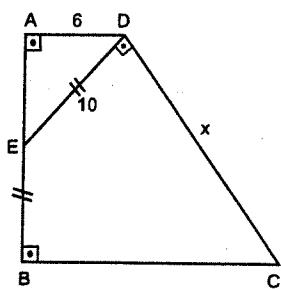
71.

ABTD  
Paralelkenar

$A(ABCD) = ?$

Cevap: 35

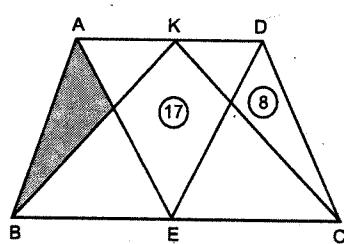
68.



$x = ?$

Cevap: 30

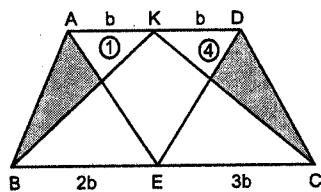
72.



$T.A = ?$

Cevap: 9

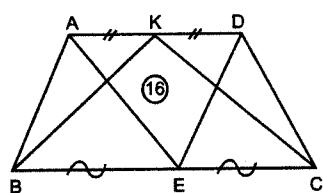
73.



$$T.A = ?$$

Cevap: 14

74.

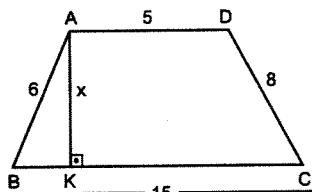


ABED  
paralelkenar

$$A(ABCD) = ?$$

Cevap: 72

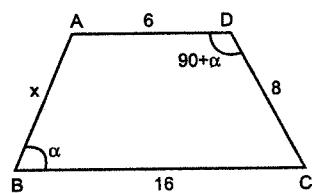
75.



$$x = ?$$

Cevap: 4,8

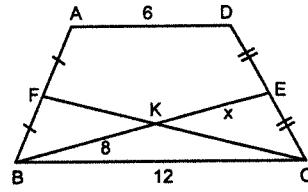
76.



$$x = ?$$

Cevap: 6

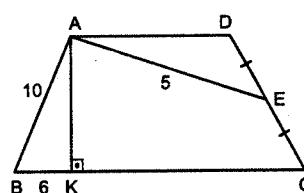
77.



$$x = ?$$

Cevap: 6

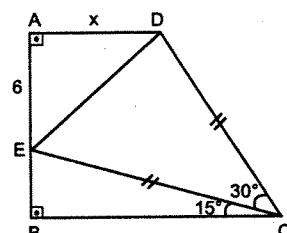
78.



$$A(AKCD) = ?$$

Cevap: 24

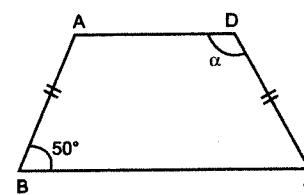
79.



$$x = ?$$

Cevap:  $2\sqrt{3}$ 

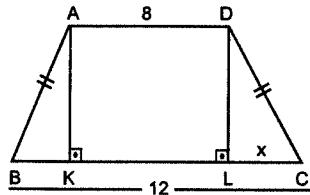
80.



$$\alpha = ?$$

Cevap: 130

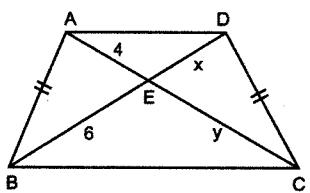
81.



$x = ?$

Cevap: 2

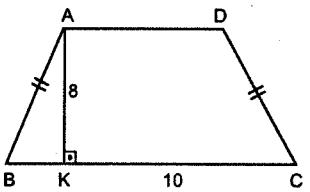
82.



$y - x = ?$

Cevap: 2

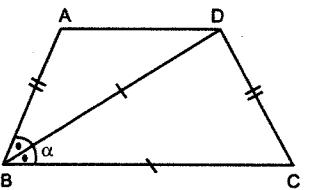
83.



$A(ABCD) = ?$

Cevap: 80

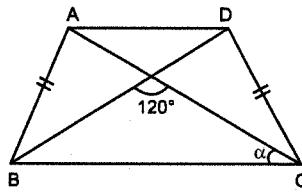
84.



$\alpha = ?$

Cevap: 36

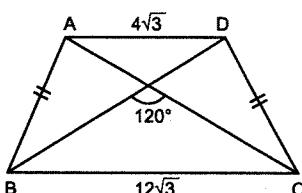
85.



$\alpha = ?$

Cevap: 30

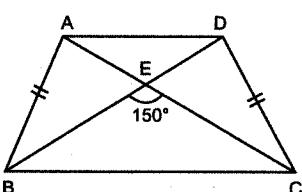
86.



$A(ABCD) = ?$

Cevap:  $64\sqrt{3}$ 

87.

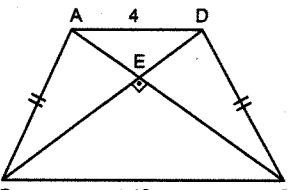


$|BD| = 10 \text{ cm}$

$A(ABCD) = ?$

Cevap: 25

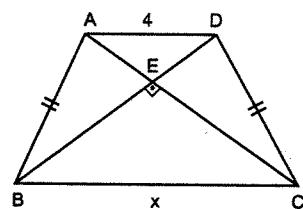
88.



$A(ABCD) = ?$

Cevap: 64

99.

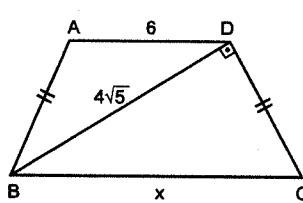


$$A(ABCD) = 100$$

$$x = ?$$

Cevap: 16

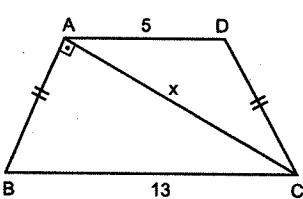
90.



$$x = ?$$

Cevap: 10

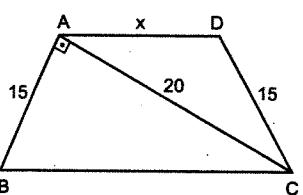
91.



$$x = ?$$

Cevap:  $3\sqrt{13}$ 

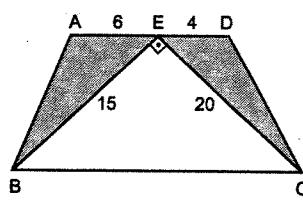
92.



$$x = ?$$

Cevap: 7

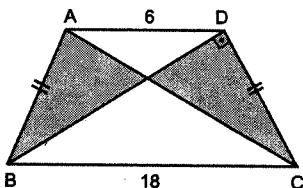
93.



$$T.A = ?$$

Cevap:  $60^\circ$ 

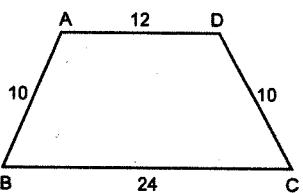
94.



$$T.A = ?$$

Cevap:  $27\sqrt{2}$ 

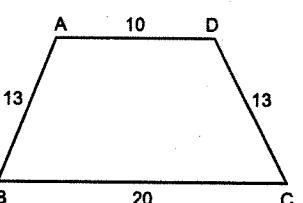
95.



$$\text{Alan}(ABCD) = ?$$

Cevap: 144

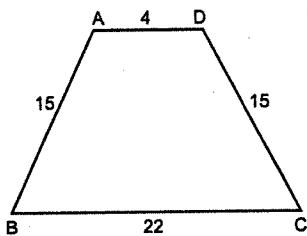
96.



$$A(ABCD) = ?$$

Cevap: 180

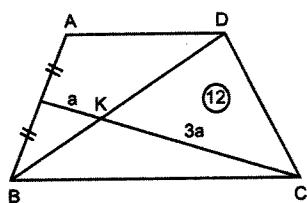
97.



$$A(ABCD) = ?$$

Cevap: 156

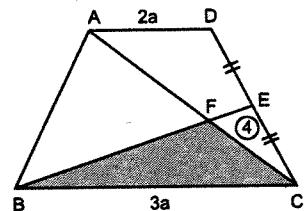
98.



$$A(ABCD) = ?$$

Cevap: 32

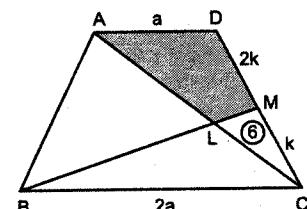
99.



$$T.A = ?$$

Cevap: 12

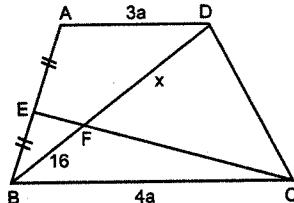
100.



$$T.A = ?$$

Cevap: 57

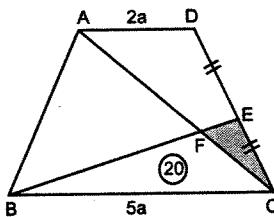
101.



$$x = ?$$

Cevap: 28

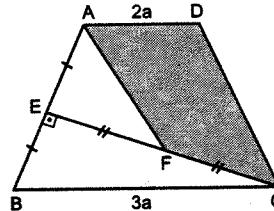
102.



$$T.A = ?$$

Cevap: 4

103.

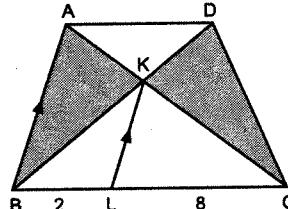


$$T.A = 33$$

$$A(ABCD) = ?$$

Cevap: 60

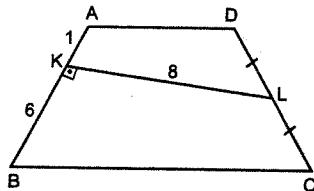
104.



$$T.A = 36$$

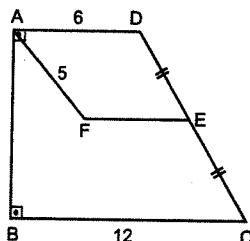
$$A(ABCD) = ?$$

Cevap:  $\frac{225}{2}$

**105.**

$$A(ABCD) = ?$$

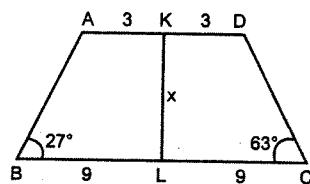
Cevap: 56

**106.**

AFED paralelkenar

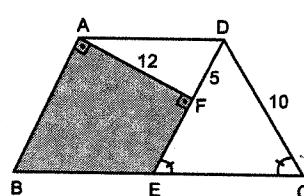
$$A(AFED) = ?$$

Cevap: 24

**109.**

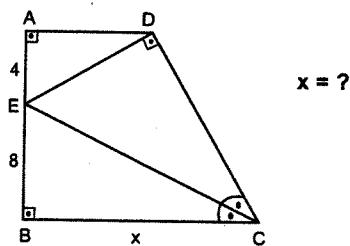
$$x = ?$$

Cevap: 6

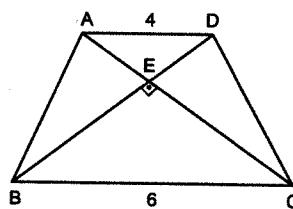
**110.**

$$T.A = ?$$

Cevap: 90

**107.**

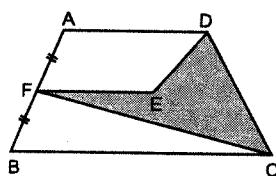
$$x = ?$$

Cevap:  $8\sqrt{3}$ **111.**

$$|AC| = 8$$

$$|BD| = ?$$

Cevap: 6

**108.**

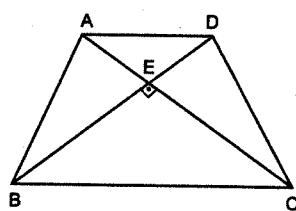
AFED paralelkenar

$$T.A = 12$$

$$A(ABCD) = 40$$

$$A(FED) = ?$$

Cevap: 16

**112.**

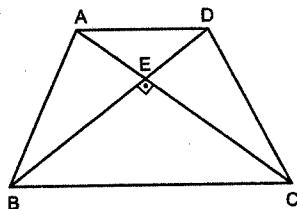
$$|AD| + |BC| = 20$$

$$|AC| = 16$$

$$|BD| = ?$$

Cevap: 12

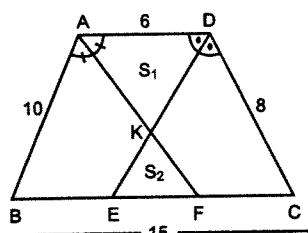
113.



$$\begin{aligned}|BD| &= 8 \\ |AC| &= 15 \\ |AD| + |BC| &=?\end{aligned}$$

Cevap: 17

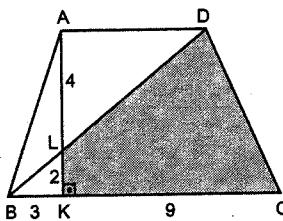
114.



$$\frac{S_1}{S_2} = ?$$

Cevap: 4

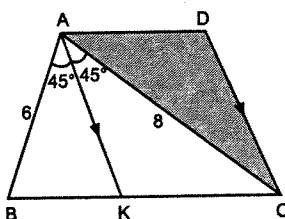
117.



$$T.A = ?$$

Cevap: 33

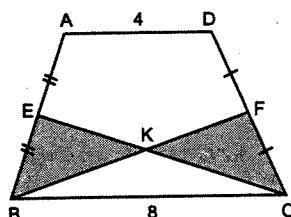
118.



$$T.A = ?$$

Cevap:  $\frac{96}{7}$ 

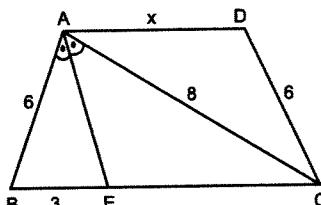
115.



$$\frac{T.A}{A(ABCD)} = ?$$

Cevap:  $\frac{2}{7}$ 

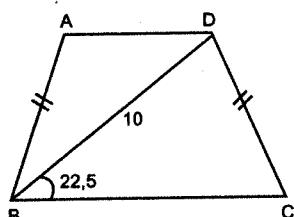
119.



$$x = ?$$

Cevap: 4

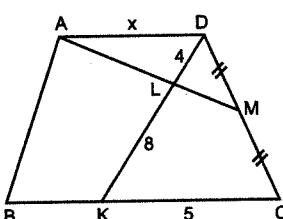
116.



$$A(ABCD) = ?$$

Cevap:  $25\sqrt{2}$ 

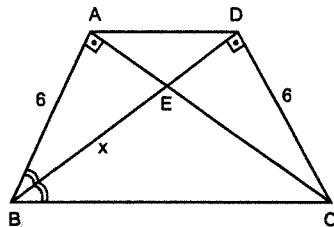
120.



$$x = ?$$

Cevap: 5

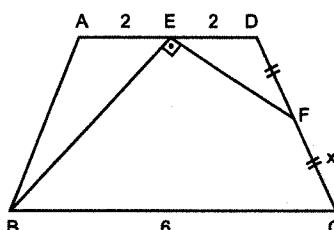
121.



$x = ?$

Cevap:  $4\sqrt{3}$ 

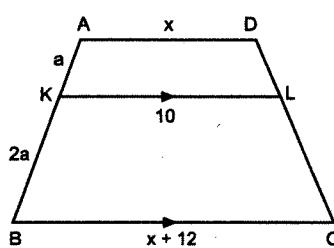
122.



$x = ?$

Cevap: 2

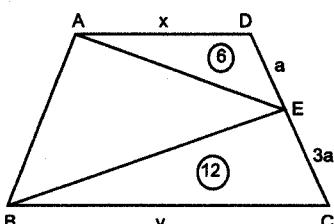
123.



$x = ?$

Cevap: 6

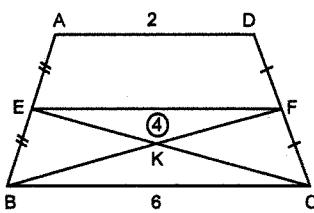
124.



$\frac{x}{y} = ?$

Cevap:  $\frac{3}{2}$ 

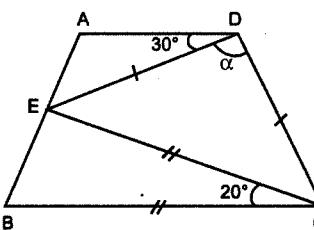
125.



$A(ABCD) = ?$

Cevap: 40

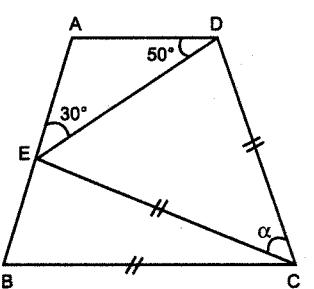
126.



$\alpha = ?$

Cevap: 80

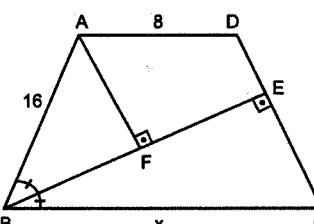
127.



$\alpha = ?$

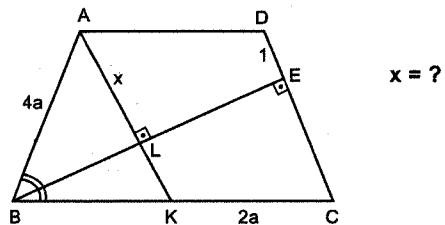
Cevap: 40

128.



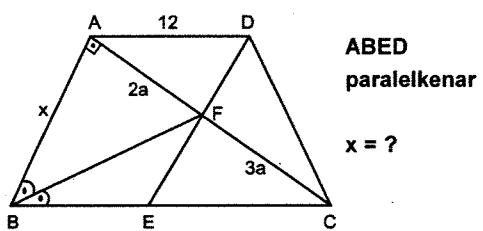
$x = ?$

Cevap: 24

**129.**

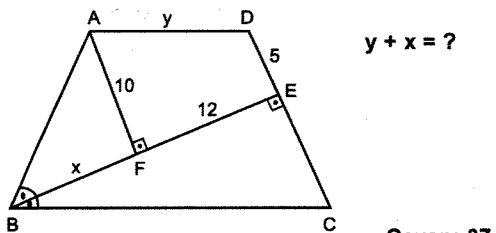
$x = ?$

Cevap: 2

**130.**ABED  
paralelkenar

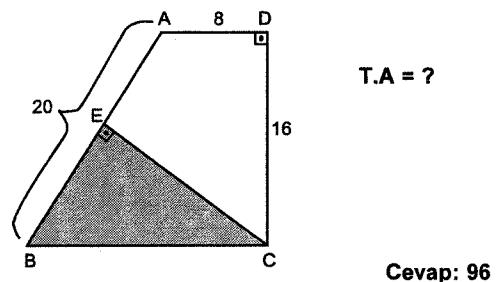
$x = ?$

Cevap: 20

**131.**

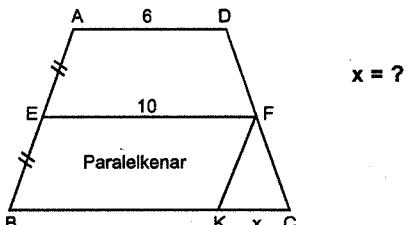
$y + x = ?$

Cevap: 37

**132.**

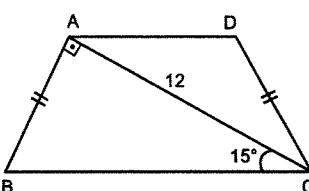
$T.A = ?$

Cevap: 96

**133.**

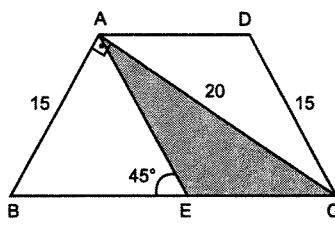
$x = ?$

Cevap: 4

**134.**

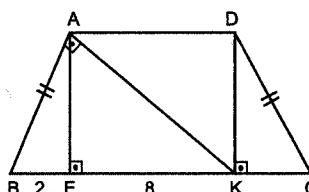
$A(ABCD) = ?$

Cevap: 36

**135.**

$T.A = ?$

Cevap: 24

**136.**

$A(ABCD) = ?$

Cevap: 40

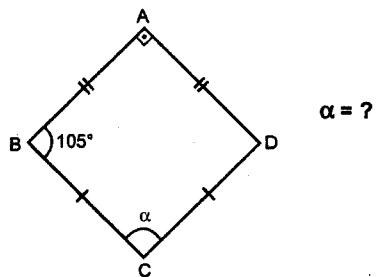
## DELTOİD

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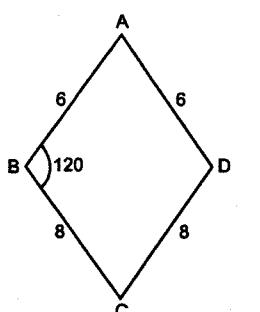
**1.**



$$\alpha = ?$$

Cevap: 60

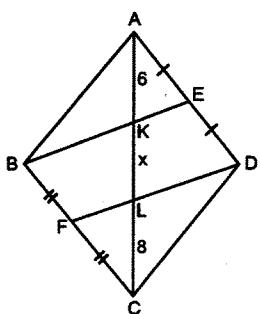
**2.**



$$A(ABCD) = ?$$

Cevap:  $24\sqrt{3}$

**3.**



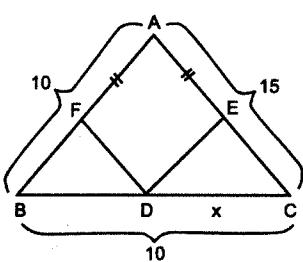
Deltoid

$$|AB| = |AD|$$

$$x = ?$$

Cevap: 7

**4.**

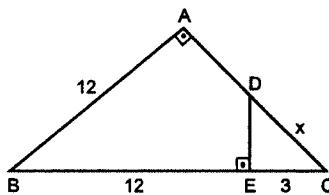


AFDE  
Deltoid

$$x = ?$$

Cevap: 6

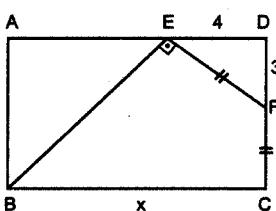
**5.**



$$x = ?$$

Cevap: 5

**6.**

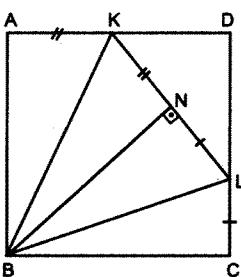


Dikdörtgen

$$x = ?$$

Cevap: 10

**7.**

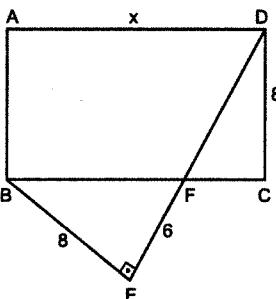


Kare

$$m(\widehat{KBL}) = ?$$

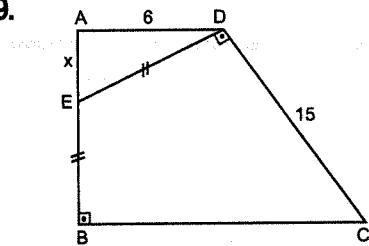
Cevap: 45

**8.**



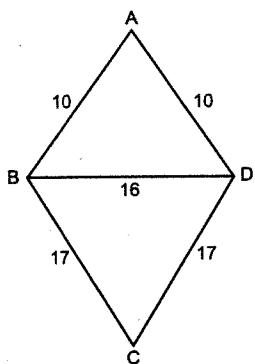
$$x = ?$$

Cevap: 16

**9.**

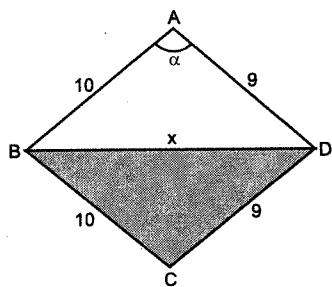
$$x = ?$$

$$\text{Cevap: } \frac{9}{2}$$

**10.**

$$A(ABCD) = ?$$

$$\text{Cevap: } 168$$

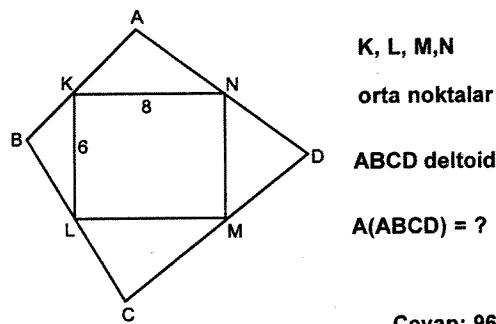
**11.**

$$\alpha > 90$$

$$T.A = 36$$

$$x = ?$$

$$\text{Cevap: } 17$$

**12.**

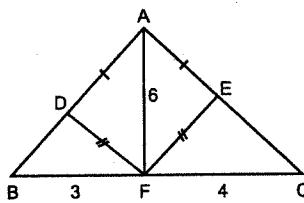
K, L, M, N

orta noktalar

ABCD deltoid

$$A(ABCD) = ?$$

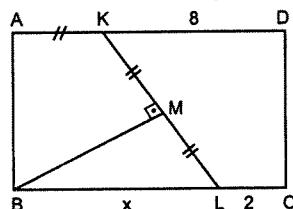
$$\text{Cevap: } 96$$

**13.**

ADFE deltoid

$$\widehat{C(ABC)} = ?$$

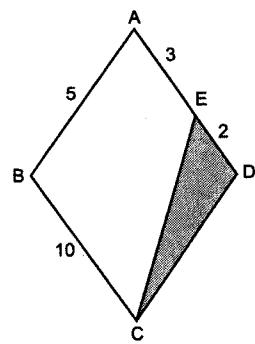
$$\text{Cevap: } 21$$

**14.**

Dikdörtgen

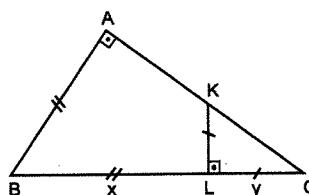
$$x = ?$$

$$\text{Cevap: } 12$$

**15.**

$$\frac{T.A}{A(ABCD)} = ?$$

$$\text{Cevap: } \frac{1}{5}$$

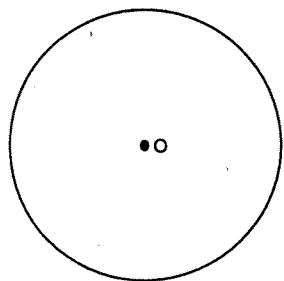
**16.**

$$\frac{x}{y} = ?$$

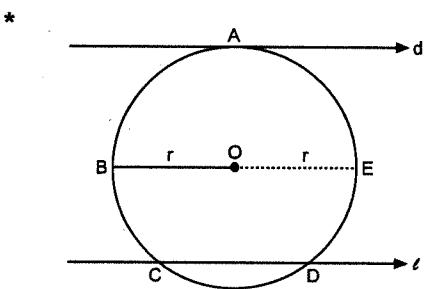
$$\text{Cevap: } \sqrt{2} + 1$$

## ÇEMBERDE AÇI

- \* Düzlemede sabit bir noktaya eşit uzaklıktaki noktalar kümesine çember denir.



Çember tam açıdır. Yani  $360^\circ$  dir.



O : Merkez

d : Teğet doğrusu

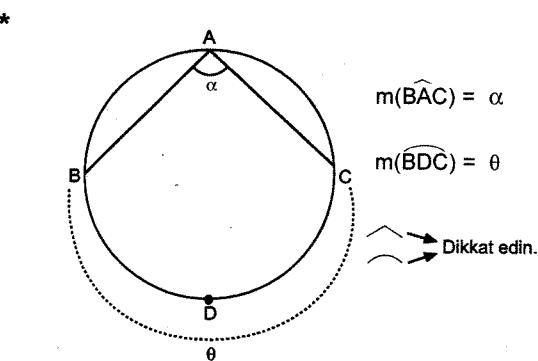
A : Teğetenin değme noktası

e : kesen

[CD] : kiriş

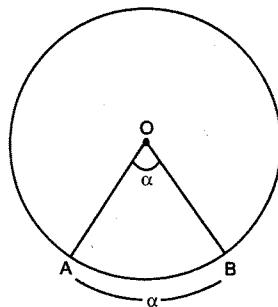
$|OB| = r$

$|EB| = 2r$  (çap)



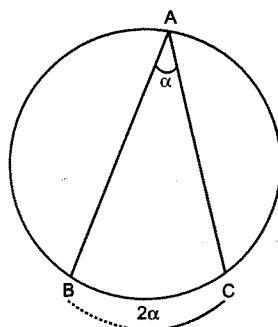
Özellikler: Merkez Açı: Gördüğü yaya eşittir.

1)



$$m(\widehat{AB}) = \alpha$$

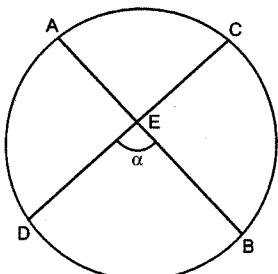
2) Çevre Açı: Gördüğü yayın yarısına eşittir.



$$m(\widehat{BC}) = 2\alpha$$

3) İç açı: ( $\alpha$ )

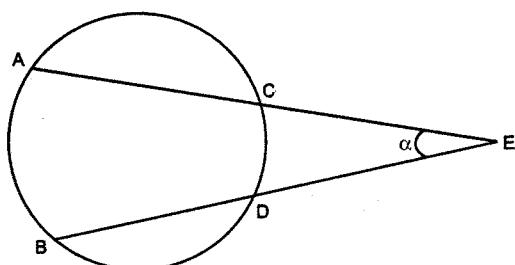
Gördüğü yaylar toplamının yarısına eşittir.



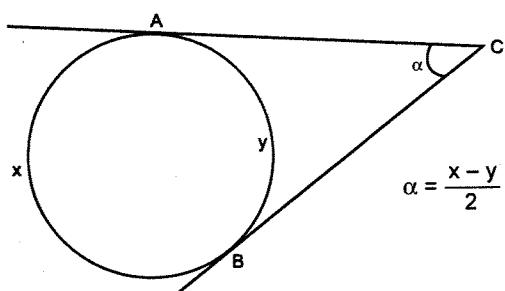
$$\alpha = \frac{m(\widehat{AC}) + m(\widehat{BD})}{2}$$

4) Dış açı: ( $\alpha$ )

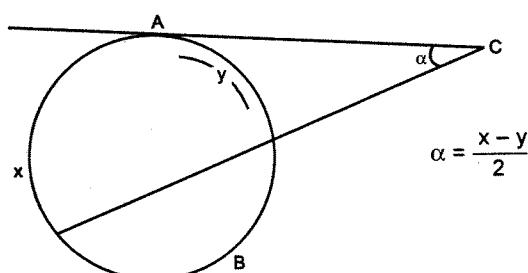
Gördüğü yaylar farkının yarısına eşittir.



$$\frac{m(\widehat{AB}) - m(\widehat{DC})}{2} = \alpha$$



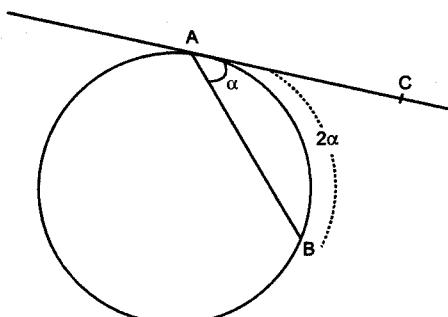
$$\alpha = \frac{x - y}{2}$$



$$\alpha = \frac{x - y}{2}$$

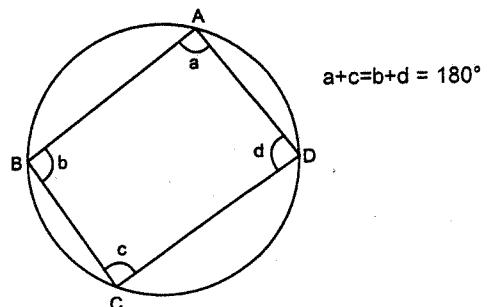
5) Teğet Kiriş Açısı: ( $\alpha$ )

Gördüğü yayın yarısına eşittir.

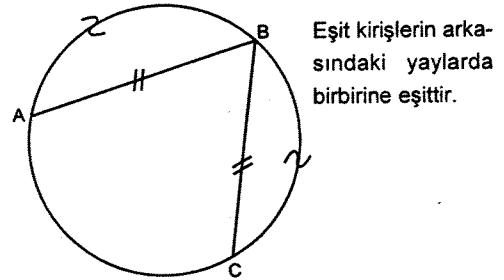


## 6) Kirişler Dörtgeni

Karşılıklı açıların toplamı  $180^\circ$  dir.

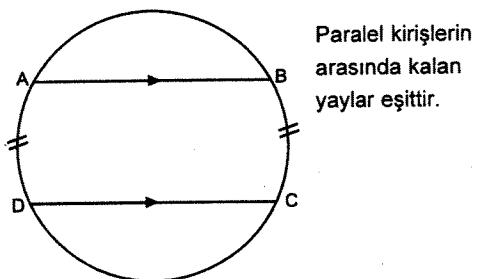


## 7)



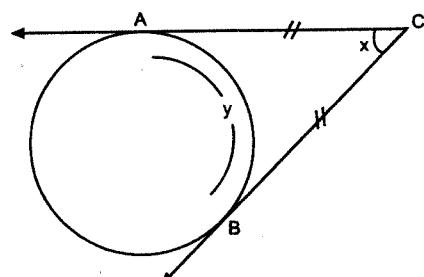
$$|AB| = |BC| \Rightarrow m(\widehat{AB}) = m(\widehat{BC})$$

## 8)



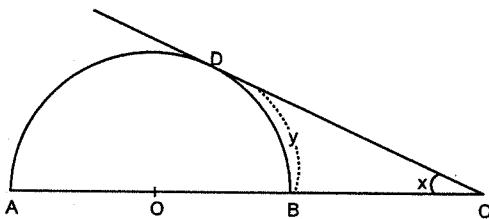
Paralel kirişlerin arasında kalan yaylar eşittir.

## 9)



$$[CA \text{ ve } CB \text{ teğet ise}] \\ x + y = 180^\circ \text{ ve } |AC| = |BC|$$

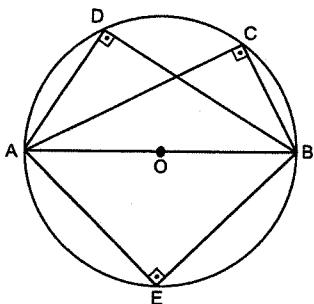
10)



$[CA]$ , merkezden geçiyor ve  $[CD]$  teğet ise

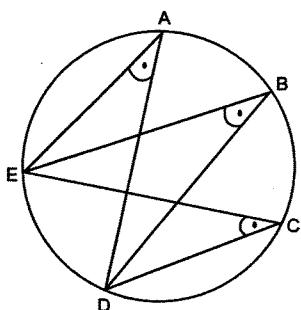
$$x + y = 90^\circ$$

\*



Çapı gören çevre açı  $90^\circ$  dir.

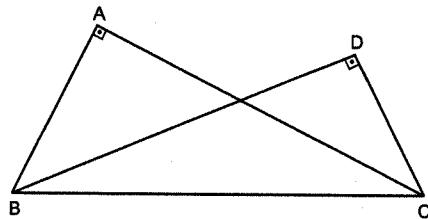
\*



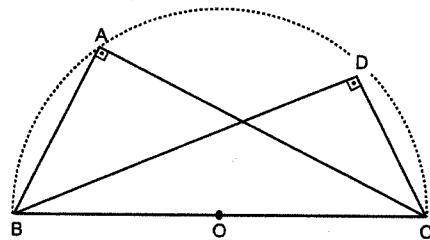
Aynı yayı gören çevre açıları birbirine eşittir.

- Karşılıklı açıları toplamı  $180^\circ$  olan tüm dörtgenlerin etrafından bir çember geçer.
- $90^\circ$  ler aynı hipotenüsü görüyorlarsa bu  $90^\circ$  lerin etrafından bir çember geçer.

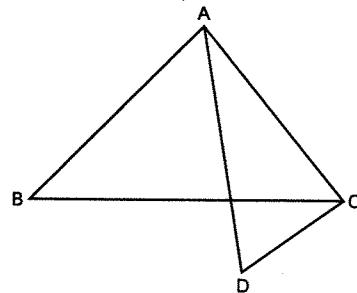
Şekil böyle verilirse



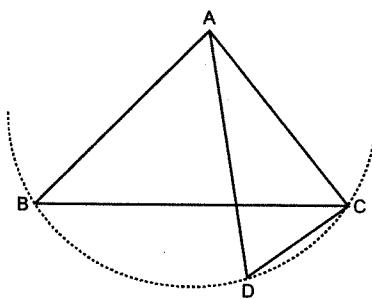
Öğrencinin yapması gerekiği



\*

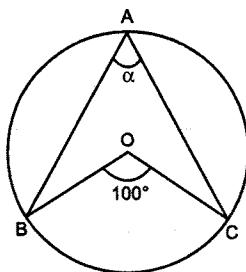


$|AB| = |AD| = |AC|$  verilirse



A merkezli  $|AB|$ ,  $|AD|$  ve  $|AC|$  yarıçaplı bir çember oluşturur.

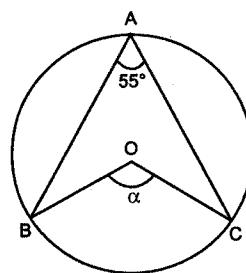
1.



$$\alpha = ?$$

Cevap: 50

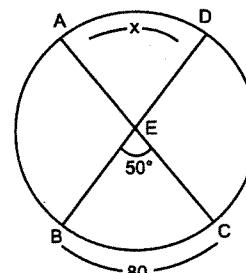
2.



$$\alpha = ?$$

Cevap: 110

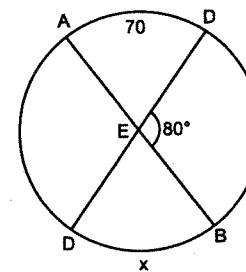
3.



$$x = ?$$

Cevap: 20

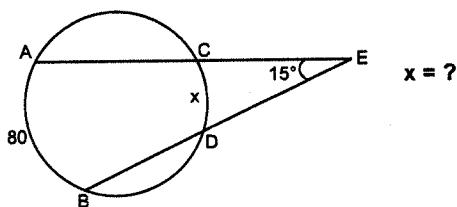
4.



$$x = ?$$

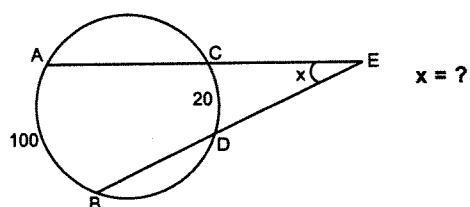
Cevap: 130

5.



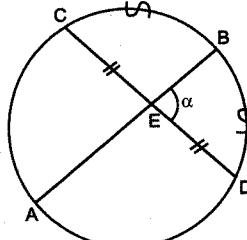
Cevap: 50

6.



Cevap: 40

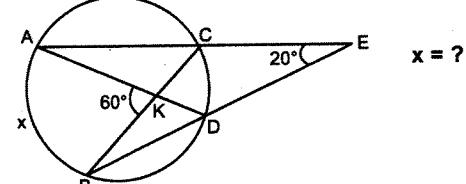
7.



$$\alpha = ?$$

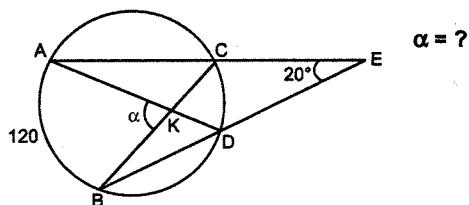
Cevap: 90

8.



Cevap: 80

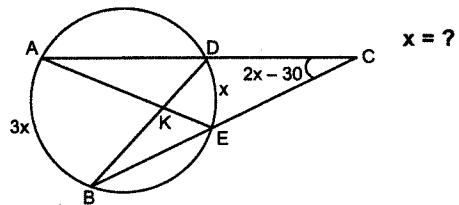
9.



$\alpha = ?$

Cevap: 100

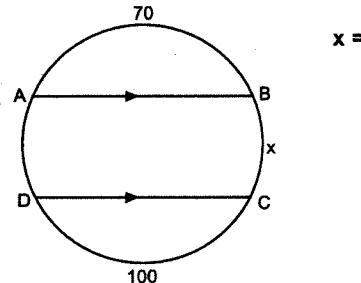
10.



$x = ?$

Cevap: 30

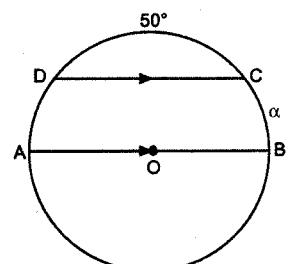
11.



$x = ?$

Cevap: 95

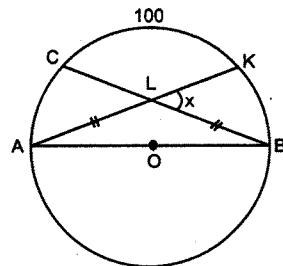
12.



$\alpha = ?$

Cevap: 65

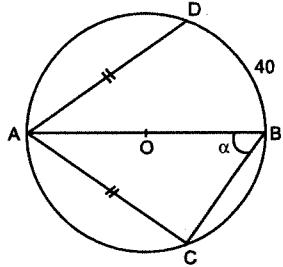
13.



$x = ?$

Cevap: 40

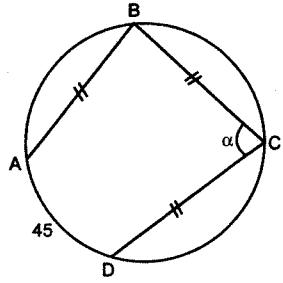
14.



$\alpha = ?$

Cevap: 70

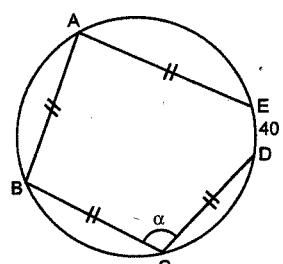
15.



$\alpha = ?$

Cevap: 75

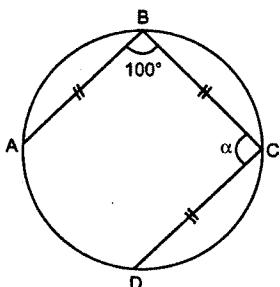
16.



$\alpha = ?$

Cevap: 100

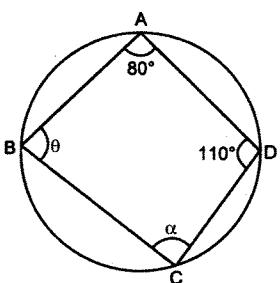
17.



$\alpha = ?$

Cevap: 100

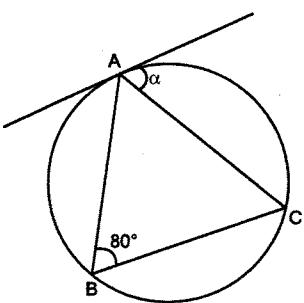
18.



$\alpha - \theta = ?$

Cevap: 30

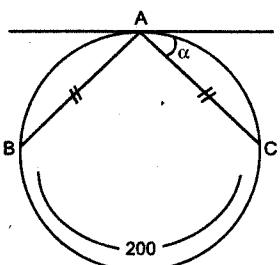
19.



$\alpha = ?$

Cevap: 80

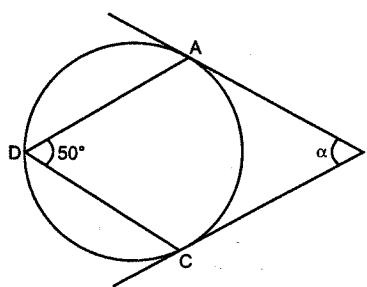
20.



$\alpha = ?$

Cevap: 40

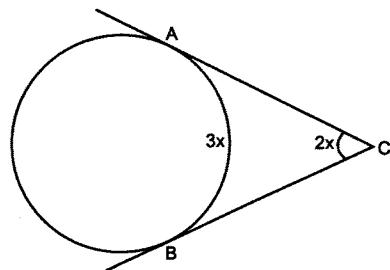
21.



$\alpha = ?$

Cevap: 80

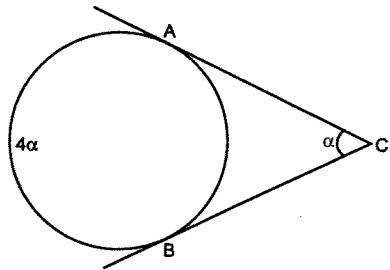
22.



$x = ?$

Cevap: 36

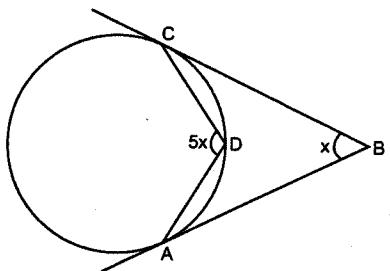
23.



$\alpha = ?$

Cevap: 60

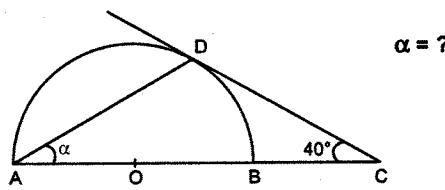
24.



$x = ?$

Cevap: 20

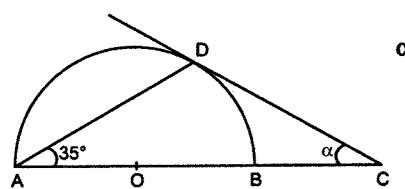
25.



$\alpha = ?$

Cevap: 25

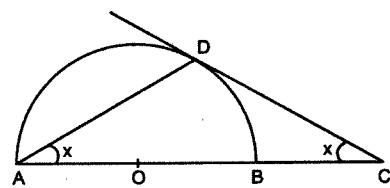
26.



$\alpha = ?$

Cevap: 20

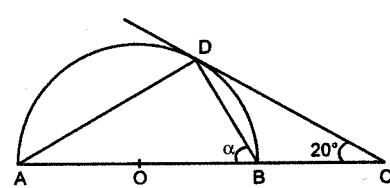
27.



$x = ?$

Cevap: 30

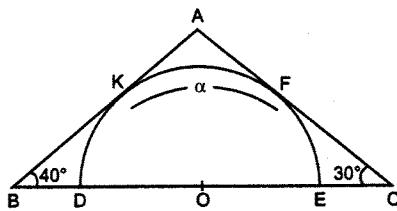
28.



$\alpha = ?$

Cevap: 55

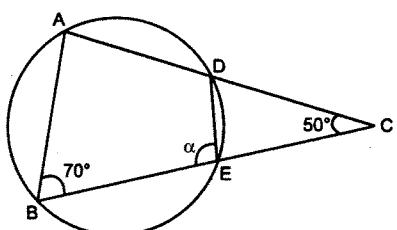
29.



$\alpha = ?$

Cevap: 70

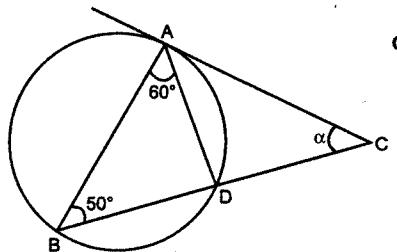
30.



$\alpha = ?$

Cevap: 120

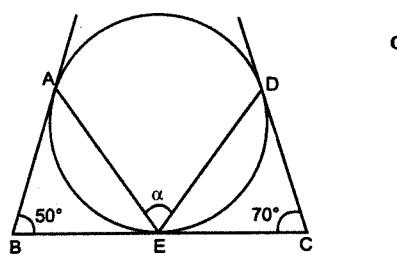
31.



$\alpha = ?$

Cevap: 20

32.



$\alpha = ?$

Cevap: 60

33.

$\alpha = ?$

Cevap: 50

34.

$\alpha = ?$

Cevap: 60

35.

Kirişler  
dörtgeni

$\alpha - \theta = ?$

Cevap: 5

36.

$\alpha = ?$

Cevap: 35

37.

$|AD| = |AB| = |AC|$

$\alpha = ?$

Cevap: 40

38.

$\alpha = ?$

Cevap: 25

39.

ABC eşkenar üçgen

$\alpha = ?$

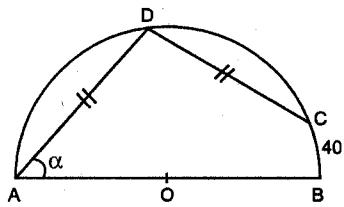
Cevap: 30

40.

$\alpha = ?$

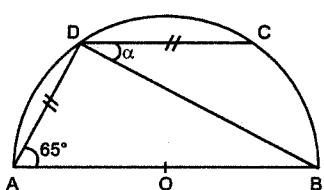
Cevap: 30

41.

 $\alpha = ?$ 

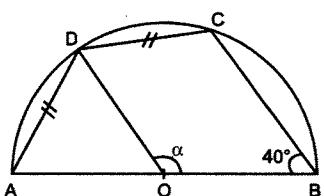
Cevap: 55

42.

 $\alpha = ?$ 

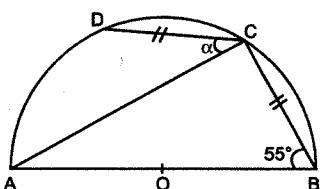
Cevap: 40

43.

 $\alpha = ?$ 

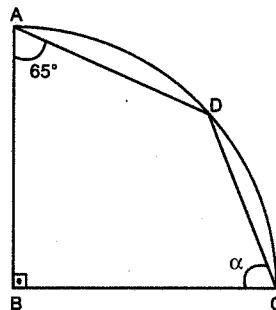
Cevap: 140

44.

 $\alpha = ?$ 

Cevap: 20

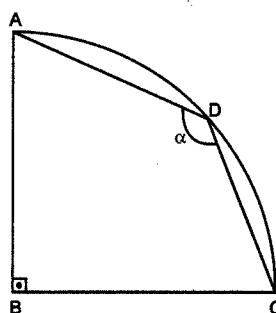
45.

 $\alpha = ?$ 

çeyrek çember

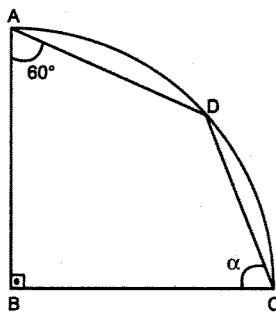
Cevap: 70

46.

 $\alpha = ?$ 

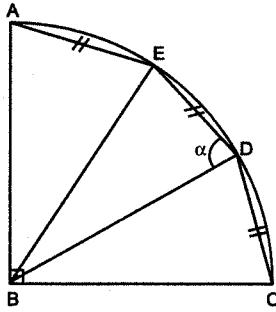
Cevap: 135

47.

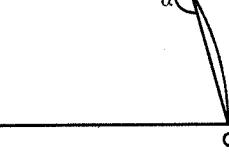
 $\alpha = ?$ 

Cevap: 75

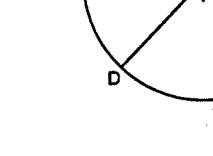
48.

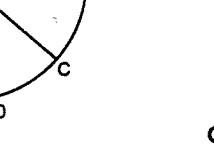
 $\alpha = ?$ 

Cevap: 75

- 49.**   $\alpha = ?$   
Cevap:  $145^\circ$

**50.**   $x = ?$   
Cevap:  $60$

**51.**   $\alpha = ?$   
Cevap:  $18$

**52.**   $\alpha = ?$   
Cevap:  $24$

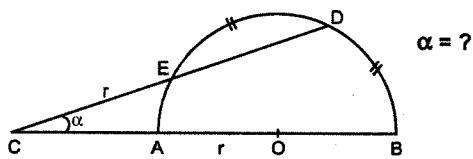
**53.**   $\alpha = ?$   
Cevap:  $120$

**54.**   $\alpha = ?$   
Cevap:  $60$

**55.**   $\alpha = ?$   
Cevap:  $135$

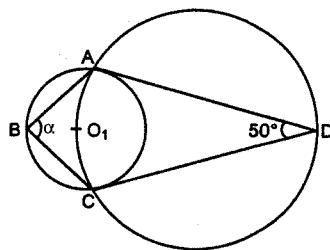
**56.**   
ABCDE...  
düzgün dokuzgen  
 $\alpha = ?$   
Cevap:  $80$

57.



$$\text{Cevap: } \frac{180}{7}$$

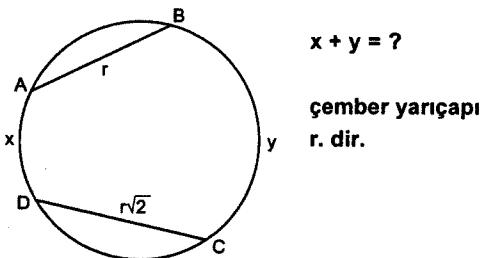
61.



$$\alpha = ?$$

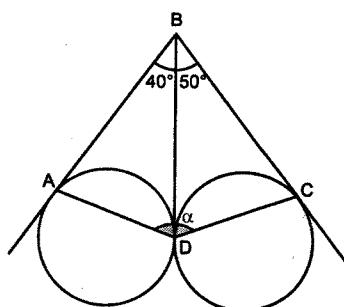
$$\text{Cevap: } 65$$

58.



$$\text{Cevap: } 210$$

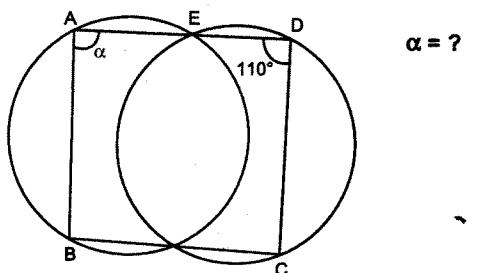
62.



$$\alpha = ?$$

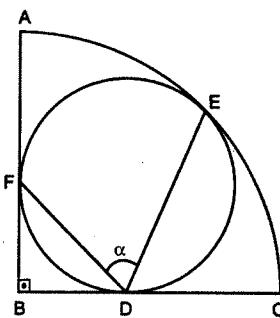
$$\text{Cevap: } 135$$

59.



$$\text{Cevap: } 70$$

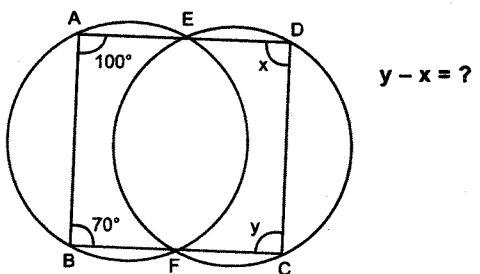
63.



$$\alpha = ?$$

$$\text{Cevap: } 67,5$$

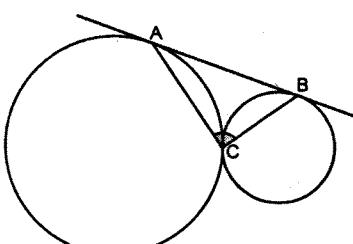
60.



$$y - x = ?$$

$$\text{Cevap: } 30$$

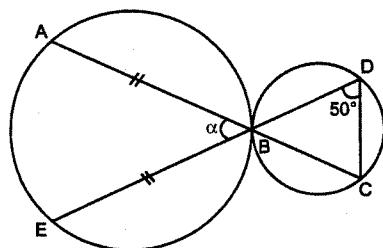
64.



$$m(\widehat{ACB}) = ?$$

$$\text{Cevap: } 90$$

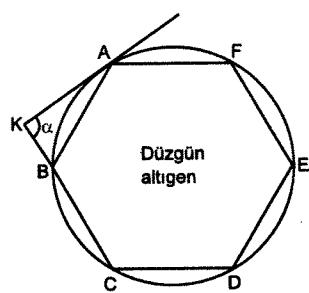
65.



$\alpha = ?$

Cevap: 80

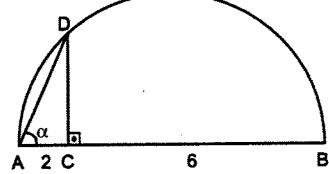
66.



$\alpha = ?$

Cevap: 90

67.

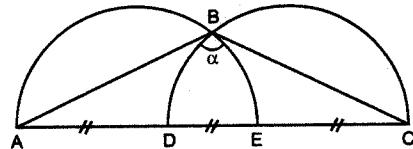


[AB] çap

$\alpha = ?$

Cevap: 60

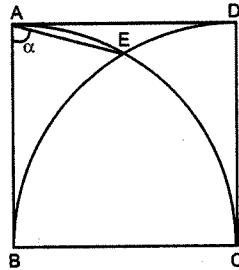
68.



$\alpha = ?$

Cevap: 120

69.

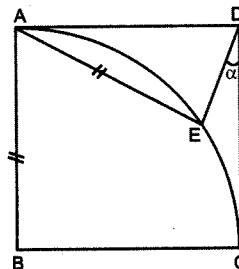


Kare

$\alpha = ?$

Cevap: 75

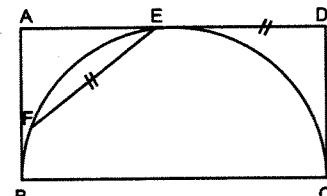
70.



$\alpha = ?$

Cevap: 15

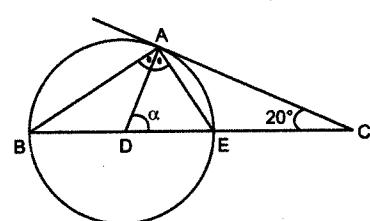
71.



$m(\widehat{FB}) = ?$

Cevap: 30

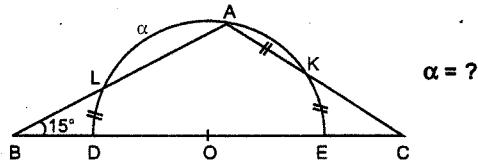
72.



$\alpha = ?$

Cevap: 80

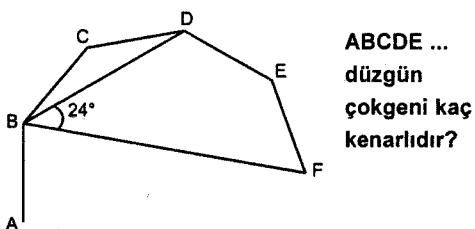
73.



$\alpha = ?$

Cevap: 90

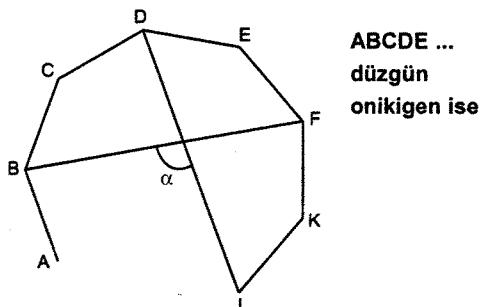
74.



ABCDE ...  
düzgün  
çokgeni kaç  
kenarlıdır?

Cevap: 15

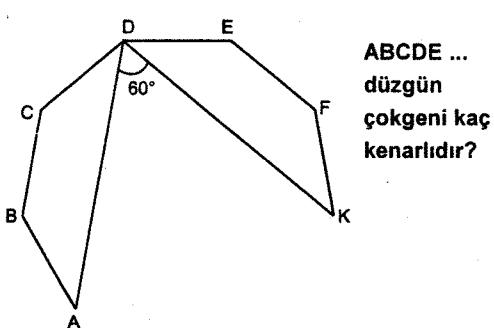
75.



ABCDE ...  
düzgün  
onikigen ise

Cevap: 120

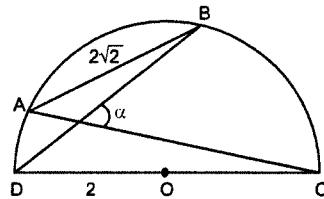
76.



ABCDE ...  
düzgün  
çokgeni kaç  
kenarlıdır?

Cevap: 9

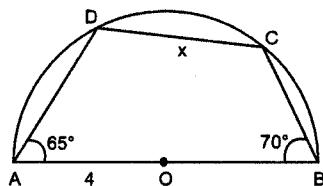
77.



$\alpha = ?$

Cevap: 45

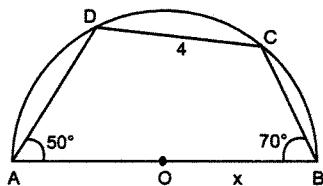
78.



$x = ?$

Cevap:  $4\sqrt{2}$ 

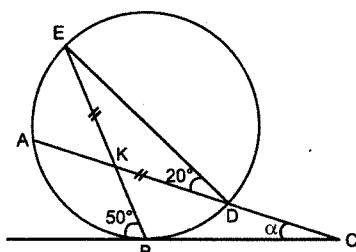
79.



$x = ?$

Cevap: 4

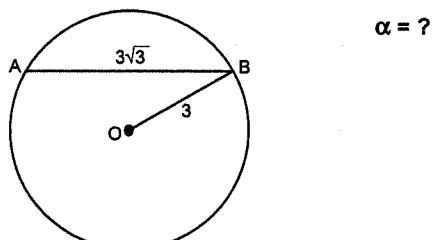
80.



$\alpha = ?$

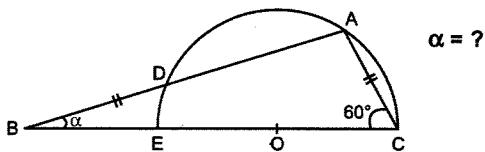
Cevap: 10

81.

 $\alpha = ?$ 

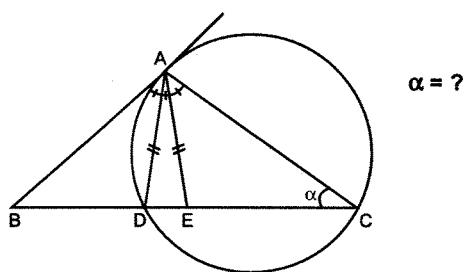
Cevap: 120

82.

 $\alpha = ?$ 

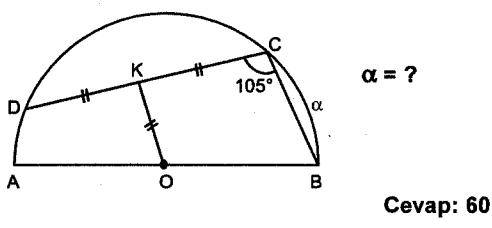
Cevap: 20

83.

 $\alpha = ?$ 

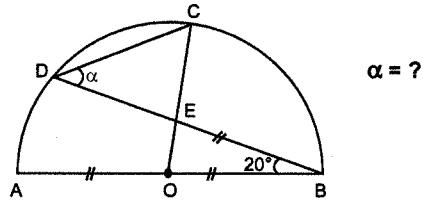
Cevap: 36

84.

 $\alpha = ?$ 

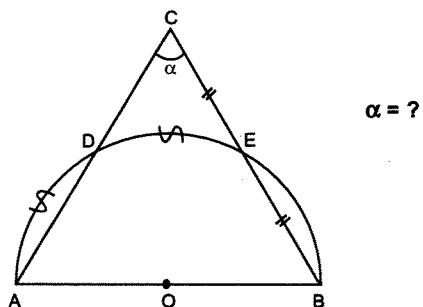
Cevap: 60

85.

 $\alpha = ?$ 

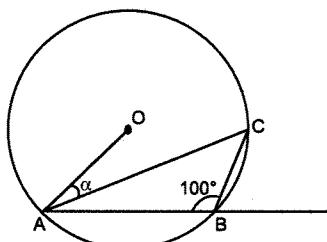
Cevap: 40

86.

 $\alpha = ?$ 

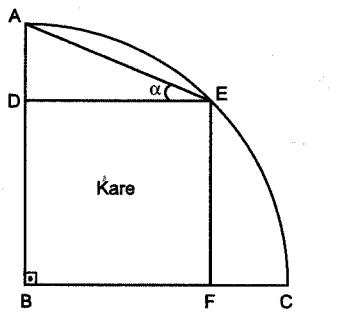
Cevap: 60

87.

 $\alpha = ?$ 

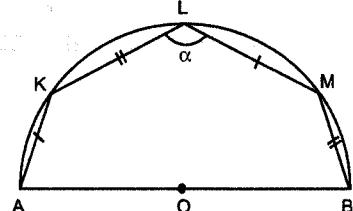
Cevap: 10

88.

 $\alpha = ?$ 

Cevap: 22,5

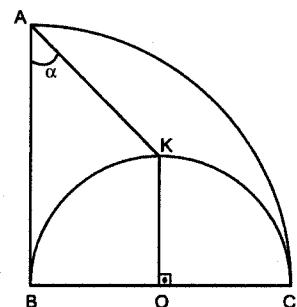
90.



$\alpha = ?$

Cevap: 135

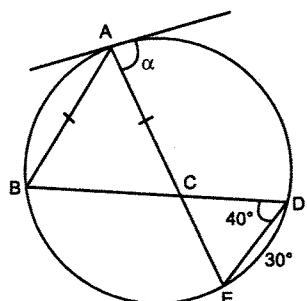
90.



$\alpha = ?$

Cevap: 45

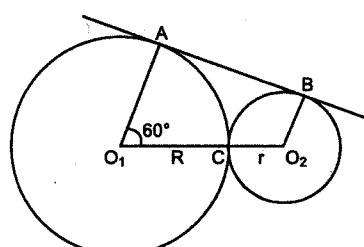
91.



$\alpha = ?$

Cevap: 85

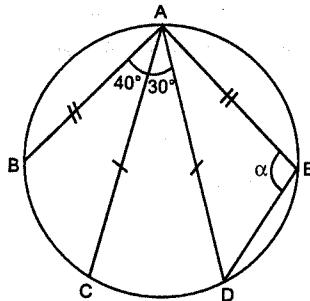
92.



$\frac{R}{r} = ?$

Cevap: 3

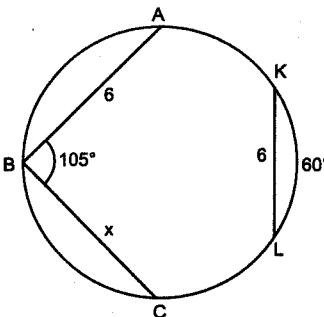
93.



$\alpha = ?$

Cevap: 105

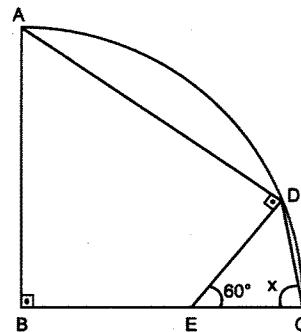
94.



$x = ?$

Cevap:  $6\sqrt{2}$ 

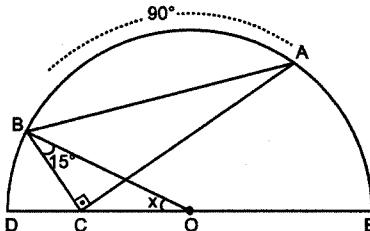
95.



$x = ?$

Cevap: 75

96.



$x = ?$

Cevap: 30

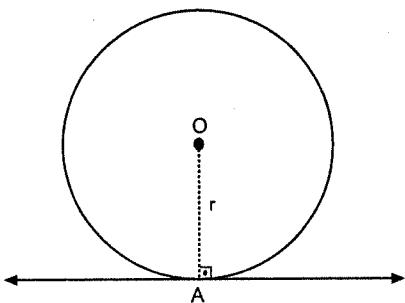
## ÇEMBERDE UZUNLUK

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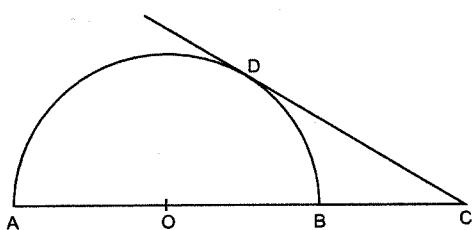
**1.**



Merkezden teğeten değme noktasına çizilen yarıçap teğete dikdir.

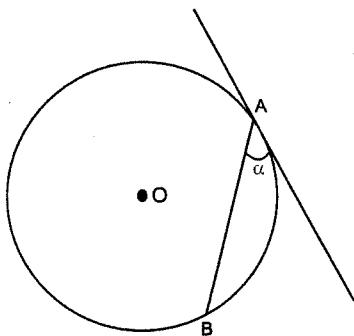
Çemberde uzunluk sorularının çoğu, merkezden teğeten değme noktasına dik indirin ve yarıçap olduğunu şekilde gösterir.

**Örnek:**

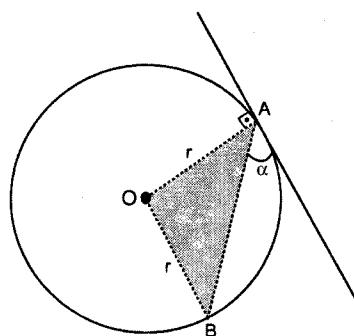


**Şekilde verilen**

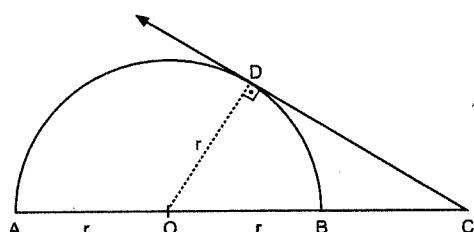
**Örnek:**



**$\alpha$  tanıdık bir açı ise**

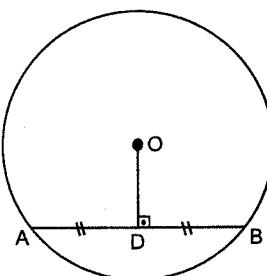


**Öğrencinin yapacağı**



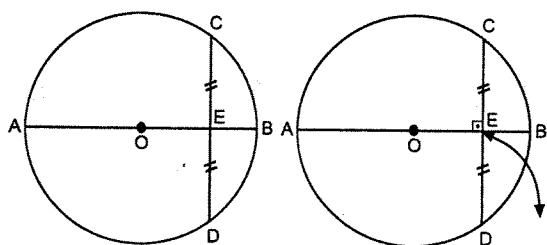
**Öğrencinin yapacağı**

**2**



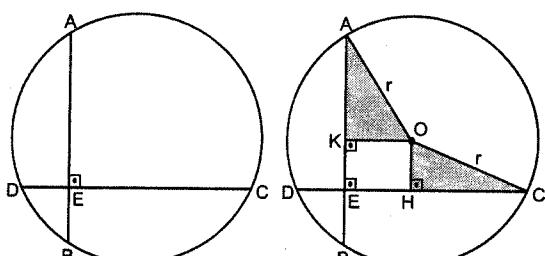
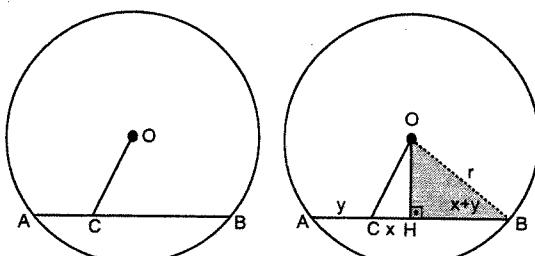
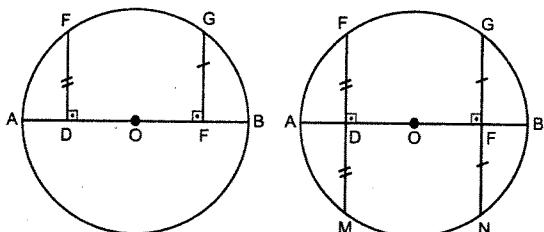
Merkezden kirişen indirilen dik, kirişin ikiye ayılır.

**Örnek:**



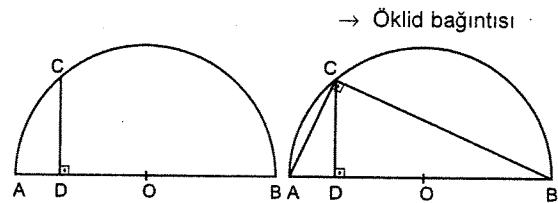
Şekilde verilen

Öğrencinin yapacağı



$$|AK| = |KB| \\ |DH| = |HC|$$

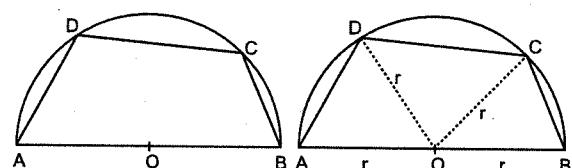
3. Çapı gören çevre açı  $90^\circ$  dir.



Şekilde verilen

Öğrencinin yapacağı

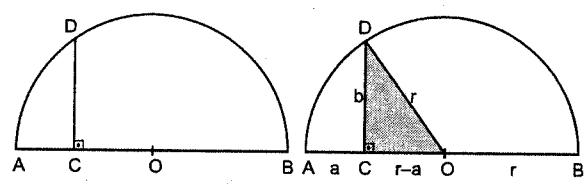
4. Merkezden uygun noktalara yarıçap çekeriz.



(İkizkenar üçgenler çıkıyor.)

Şekilde verilen

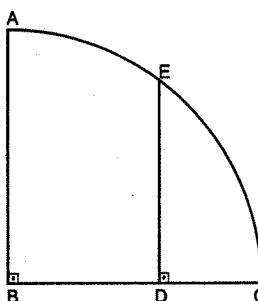
Öğrencinin yapacağı



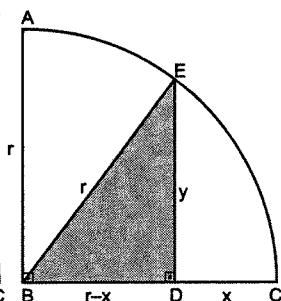
(Pisagor bağıntısı)

Şekilde verilen

Öğrencinin yapacağı

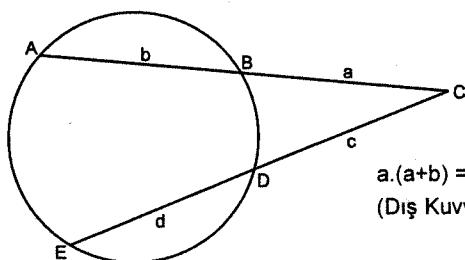


(Pisagor bağıntısı)



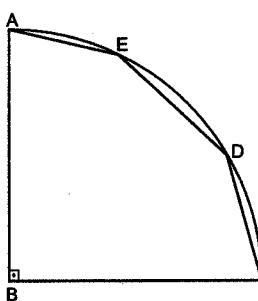
Öğrencinin yapacağı

Şekilde verilen

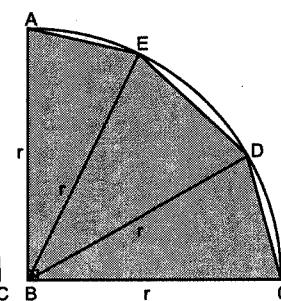


$$a \cdot (a+b) = c \cdot (c+d)$$

(Dış Kuvvet)

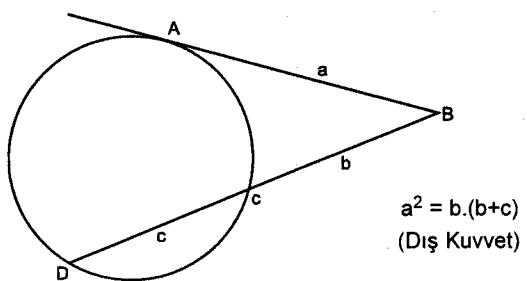


(İkizkenar üçgenler)



Öğrencinin yapacağı

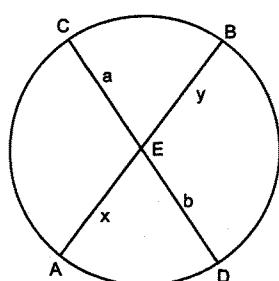
Şekilde verilen



$$a^2 = b \cdot (b+c)$$

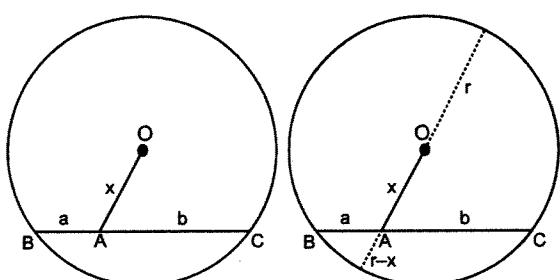
(Dış Kuvvet)

### 5. İç Kuvvet ve Dış Kuvvet yaparız.



$$x \cdot y = a \cdot b$$

İç Kuvvet

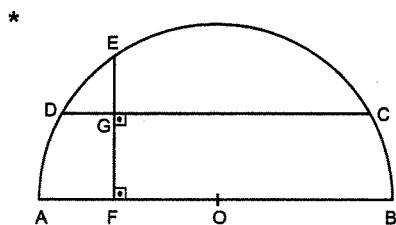


$$(r-x) \cdot (r+x) = a \cdot b$$

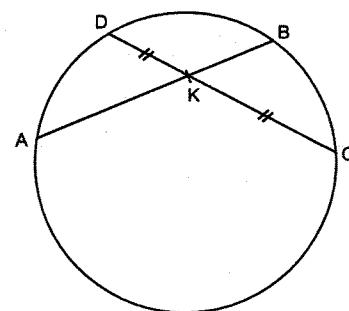
İç Kuvvet

Şekilde verilen

Öğrencinin yapacağı

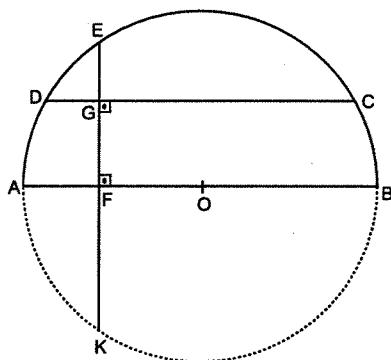


Şekilde verilen



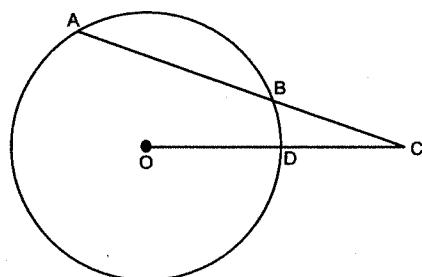
$|DC|$  dir. ve  $|DK| = |KC|$  dir.  
 $|DK| \cdot |KC| = |AK| \cdot |KB|$  (İç Kuvvet)

Öğrencinin yapacağı

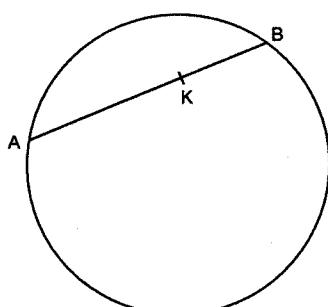


$|EG| \cdot |GK| = |DG| \cdot |GC|$   
 İç Kuvvet

Öğrencinin yapacağı

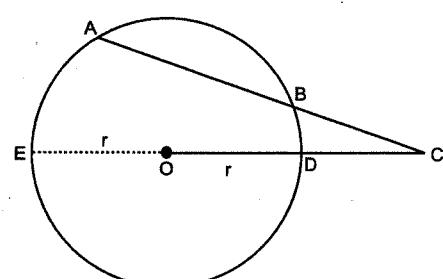


Şekilde verilen



K noktasından geçen en kısa kiriş

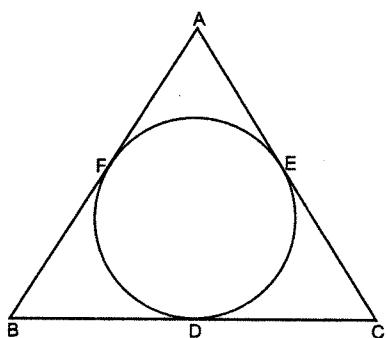
Şekilde verilen



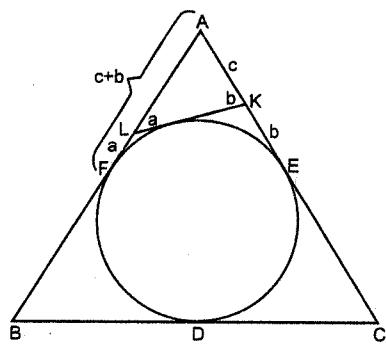
(Şimdi dış kuvvet yapabiliriz.)

Öğrencinin yapacağı

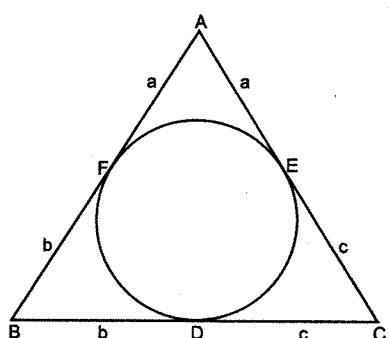
6. Çembere dışardan çizilen teğetler var ise teğet uzunlukları birbirine eşittir.



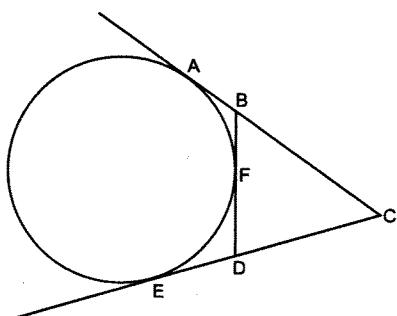
Şekilde verilen



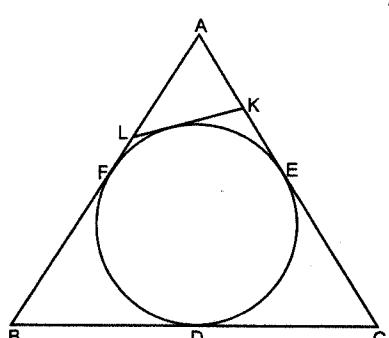
Öğrencinin yapacağı



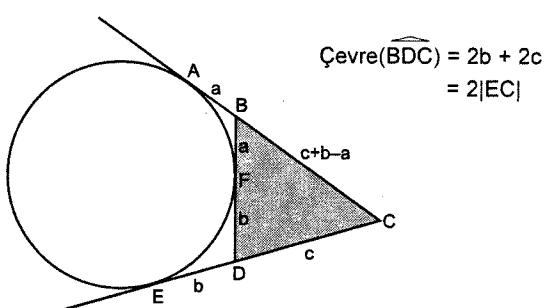
Öğrencinin yapacağı



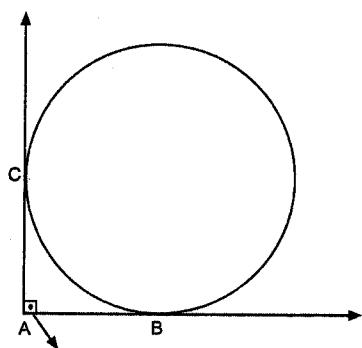
Şekilde verilen



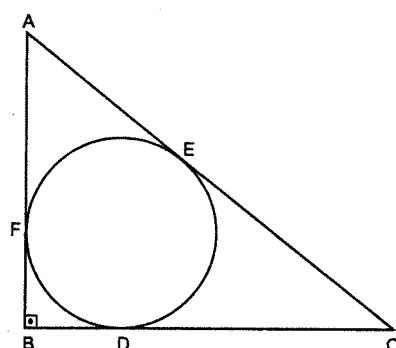
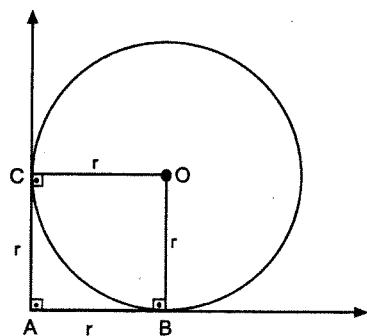
Şekilde verilen



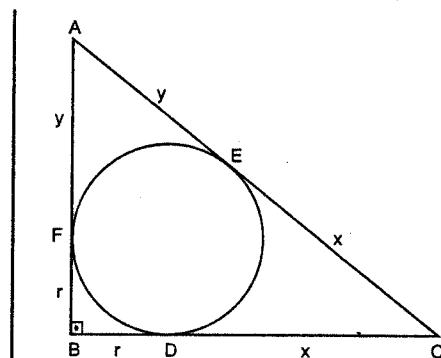
Öğrencinin yapacağı



Açı  $90^\circ$  olduğu zaman  $|AB|$  ve  $|AC|$  yarıçap eşittir.

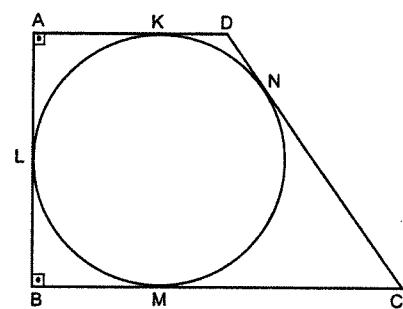


Şekilde verilen

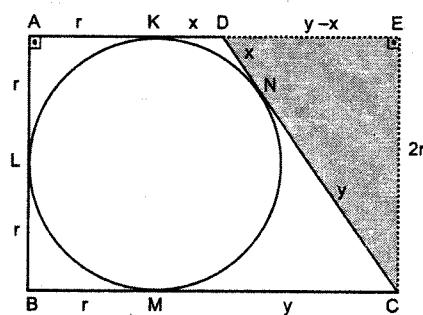


Dikkat

Öğrencinin yapacağı

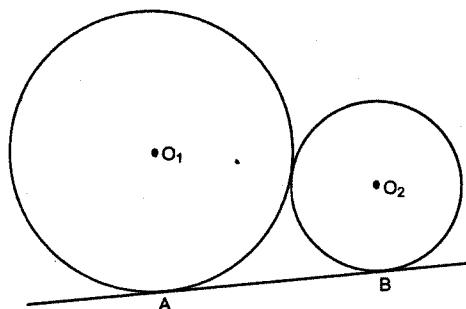


Şekilde verilen

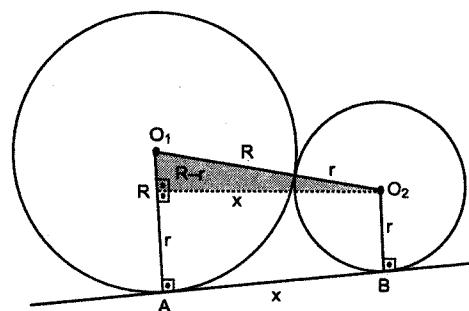


Öğrencinin yapacağı

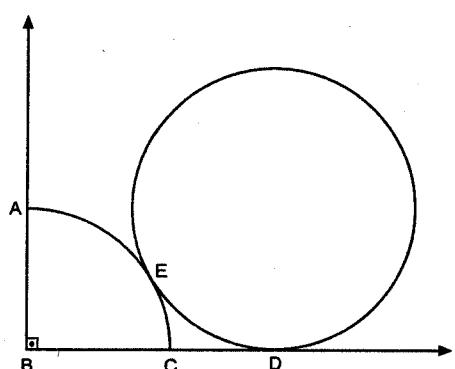
7. İki çember birbirine dıştan teğet ise çemberin merkezleri doğrusal olarak birleştirilir. Sonra merkezden teğete yarıçap çizilir. Ya dik üçgen ya da dik yamuk şekli çıkar. Bu şekiller yardımcı ile soru çözülebilir.



Şekilde verilen

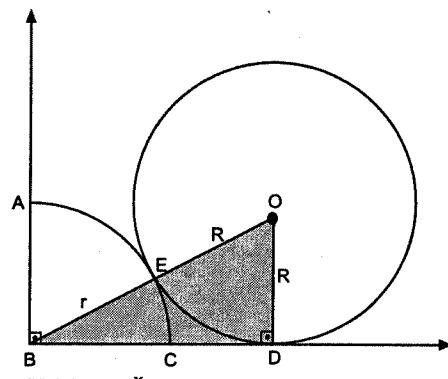


Öğrencinin yapacağı



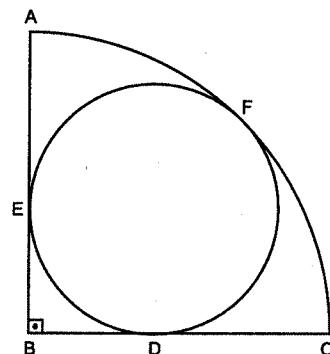
Şekilde verilen

Gibi

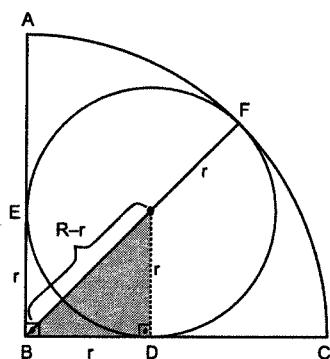


Öğrencinin yapacağı

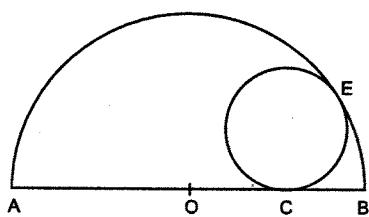
8. İki çember birbirine içten teğet ise çemberlerin merkezleri değme noktasına kadar doğrusal birleştirilir. Sonra içteki çemberden teğete dik indirilir. Sonra üçgen veya çikan şekil yardımcı ile soru çözülebilir.



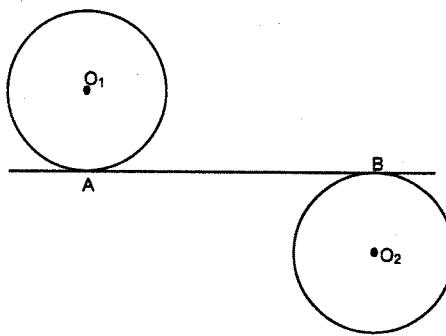
Şekilde verilen



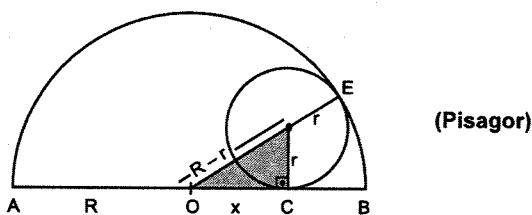
Öğrencinin yapacağı



Şekilde verilen



Şekilde verilen

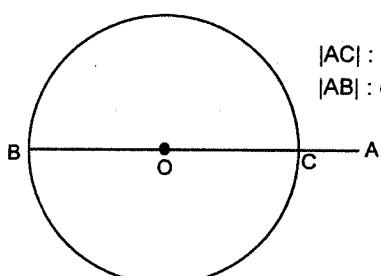


(Pisagor)

Öğrencinin yapacağı

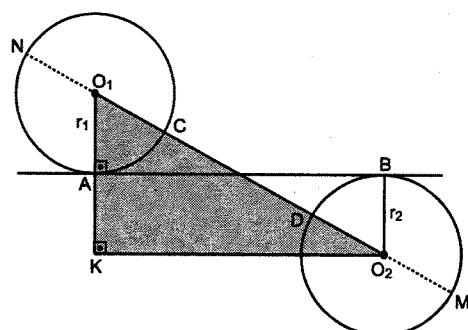
9. En kısa ve en uzun uzaklık şöyle bulunur. Bir sonda herhangi bir noktanın çembere en yakın ve en büyük uzaklık soruluyorsa bu noktadan çemberin merkezinden geçecek şekilde bir çizgi çizeriz.

➤ Bu noktanın çemberin başlangıç yerine olan uzaklığını en kısa, çemberin bitim yerine olan uzaklığını ise en büyük uzaklığı olur.



$|AC|$  : en kısa uzaklık

$|AB|$  : en büyük uzaklık

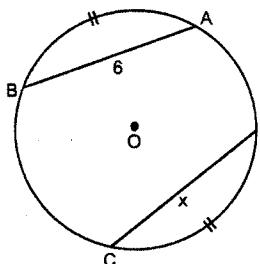


Öğrencinin yapacağı

$|CD|$  : en kısa uzaklık (çemberler arası)

$(MN)$  : çemberler arası en büyük uzaklık

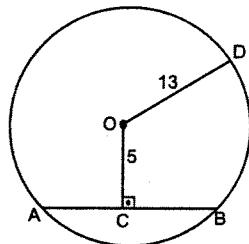
1.



$x = ?$

Cevap: 6

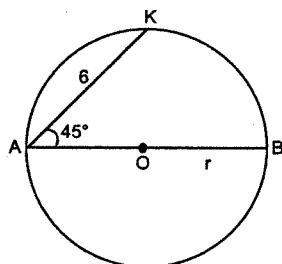
2.



$|AB| = ?$

Cevap: 24

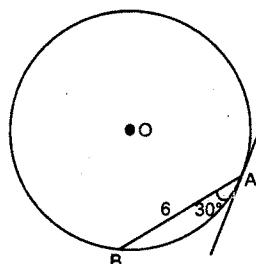
3.



$r = ?$

Cevap:  $3\sqrt{2}$ 

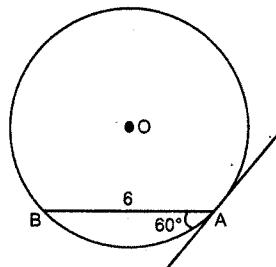
4.



$r = ?$

Cevap: 6

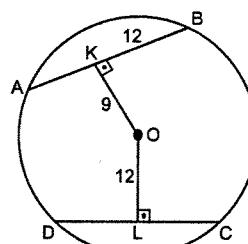
5.



$r = ?$

Cevap:  $2\sqrt{3}$ 

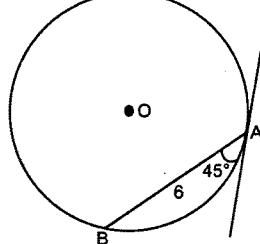
6.



$|DC| = ?$

Cevap: 18

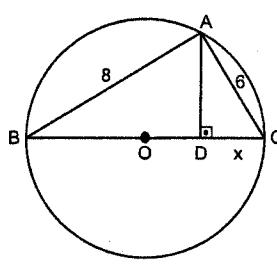
7.



$r = ?$

Cevap:  $3\sqrt{2}$ 

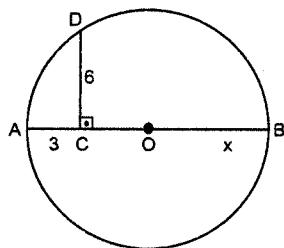
8.



$x = ?$

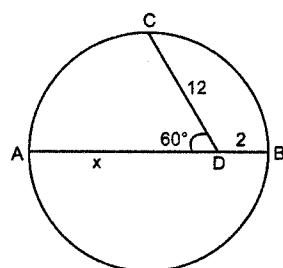
Cevap: 3,6

9.



$$x = ?$$

13.

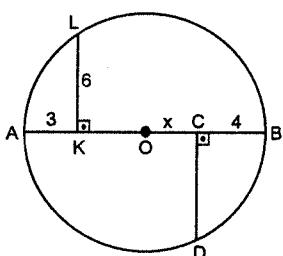


[AB] çap

$$x = ?$$

$$\text{Cevap: } \frac{39}{2}$$

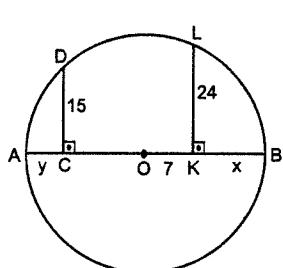
10.



$$x = ?$$

$$\text{Cevap: } \frac{7}{2}$$

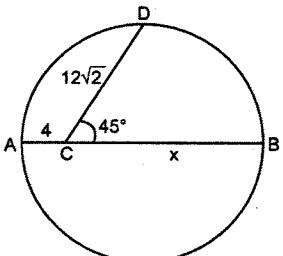
14.



$$x - y = ?$$

$$\text{Cevap: } 13$$

11.

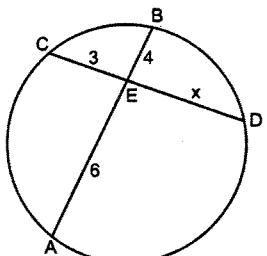


[AB] çap

$$x = ?$$

$$\text{Cevap: } 21$$

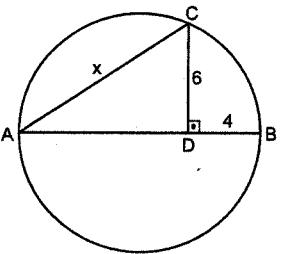
15.



$$x = ?$$

$$\text{Cevap: } 8$$

12.

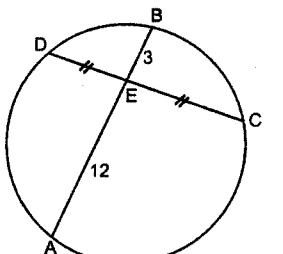


[AB] çap

$$x = ?$$

$$\text{Cevap: } 3\sqrt{13}$$

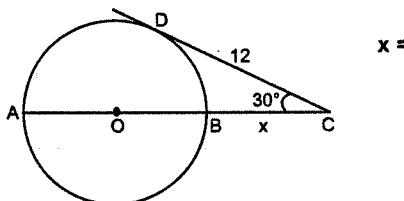
16.



$$|DC| = ?$$

$$\text{Cevap: } 12$$

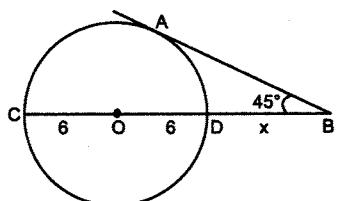
17.



$x = ?$

Cevap:  $4\sqrt{3}$ 

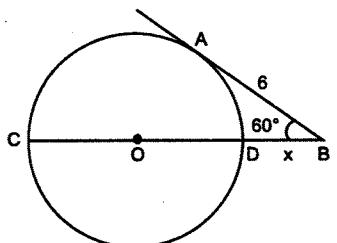
18.



$x = ?$

Cevap:  $6\sqrt{2} - 6$ 

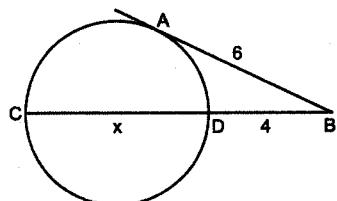
19.



$x = ?$

Cevap:  $12 - 6\sqrt{3}$ 

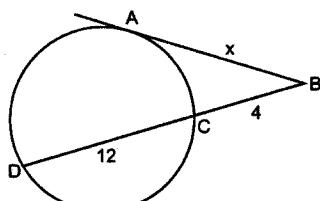
20.



$x = ?$

Cevap: 5

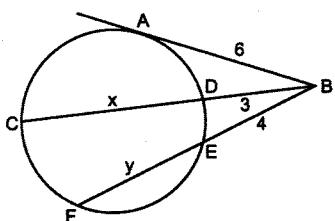
21.



$x = ?$

Cevap: 8

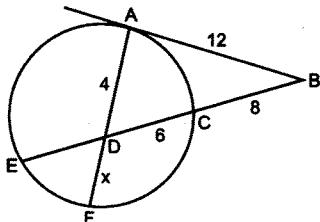
22.



$x - y = ?$

Cevap: 4

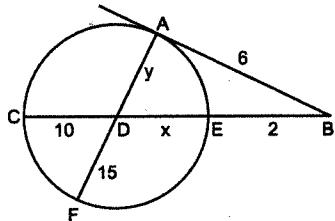
23.



$x = ?$

Cevap: 6

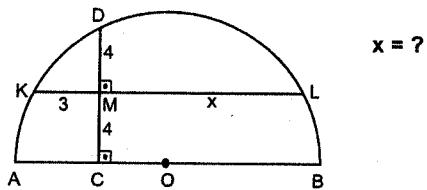
24.



$y + x = ?$

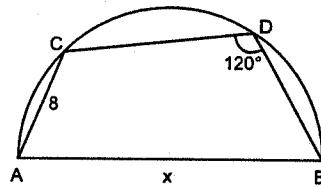
Cevap: 10

25.



$x = ?$

29.



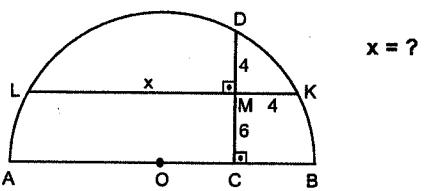
$|AB| \text{ çap}$

$|AB| = ?$

Cevap: 16

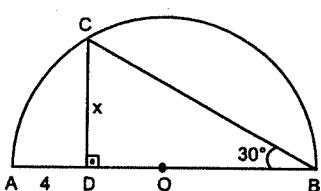
Cevap: 16

26.



$x = ?$

30.

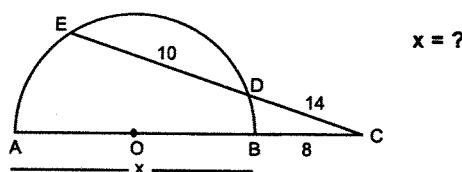


$x = ?$

Cevap:  $4\sqrt{3}$ 

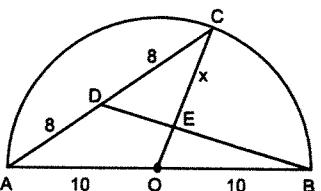
Cevap: 16

27.



$x = ?$

31.

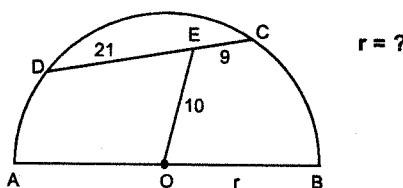


$x = ?$

Cevap:  $\frac{20}{3}$ 

Cevap: 34

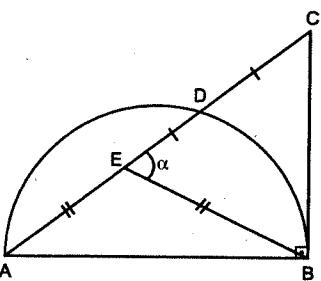
28.



$r = ?$

Cevap: 17

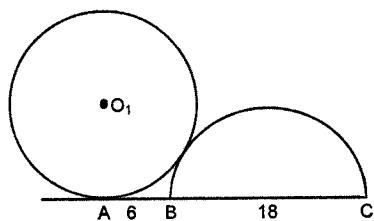
32.



$\alpha = ?$

Cevap: 60

33.

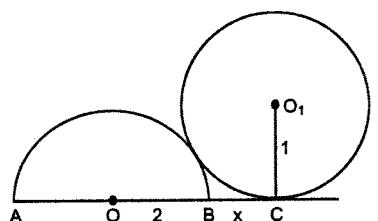


[BC] çap

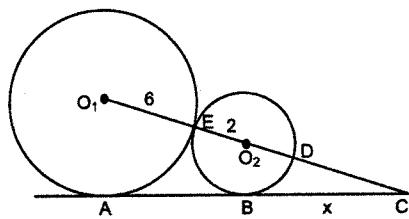
 $r_1 = ?$ 

Cevap: 8

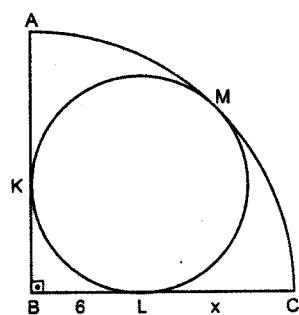
34.

 $x = ?$ Cevap:  $2\sqrt{2} - 2$ 

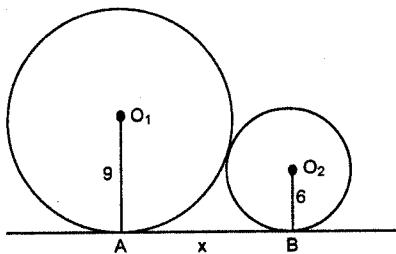
35.

 $x = ?$ Cevap:  $2\sqrt{3}$ 

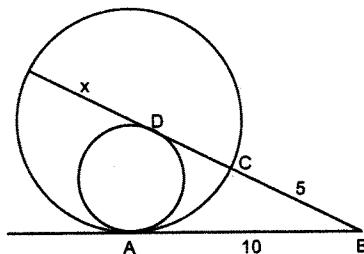
36.

 $x = ?$ Cevap:  $6\sqrt{2}$ 

37.

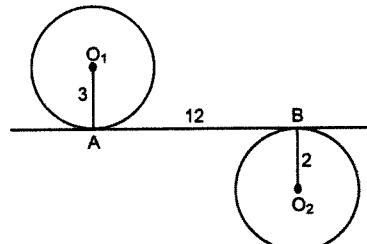
 $x = ?$ Cevap:  $6\sqrt{6}$ 

38.

 $x = ?$ 

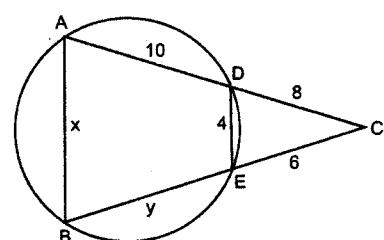
Cevap: 10

39.

 $|O_1O_2| = ?$ 

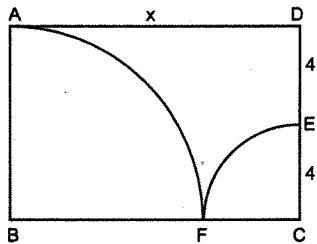
Cevap: 13

40.

 $x + y = ?$ 

Cevap: 30

41.

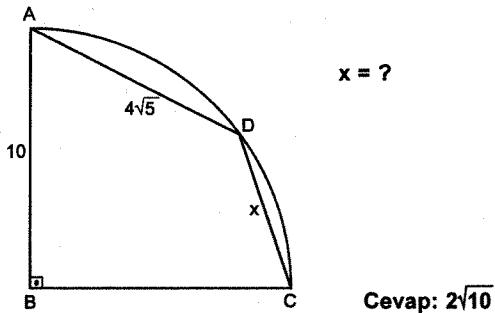


Dikdörtgen

$x = ?$

Cevap: 12

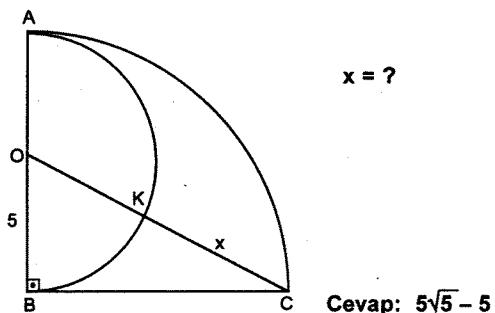
42.



$x = ?$

Cevap:  $2\sqrt{10}$ 

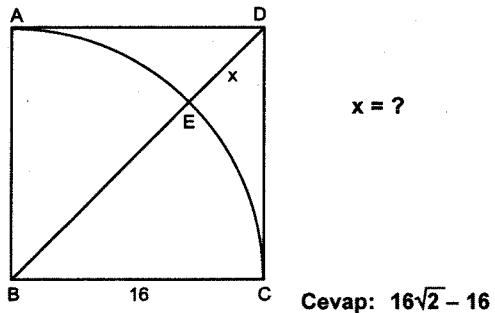
43.



$x = ?$

Cevap:  $5\sqrt{5} - 5$ 

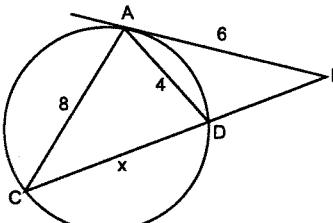
44.



$x = ?$

Cevap:  $16\sqrt{2} - 16$ 

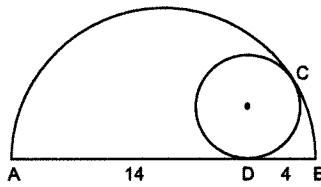
45.



$x = ?$

Cevap: 9

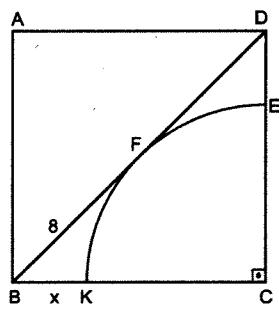
46.



$r = ?$

Cevap:  $\frac{28}{9}$ 

47.

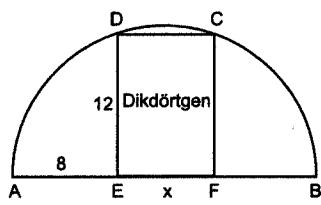


Kare;

$x = ?$

Cevap:  $8\sqrt{2} - 8$ 

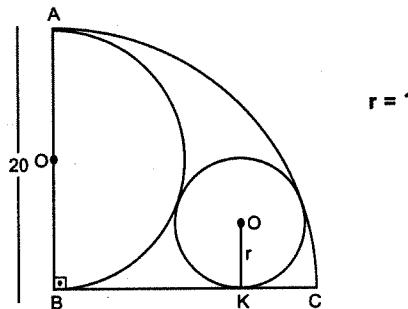
48.



$x = ?$

Cevap: 10

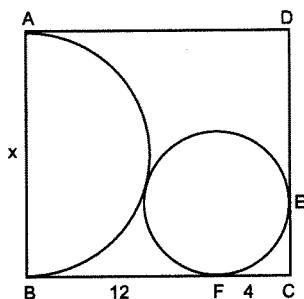
49.



$r = ?$

Cevap: 5

50.

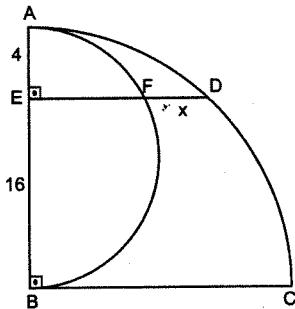


Dikdörtgen

$x = ?$

Cevap: 18

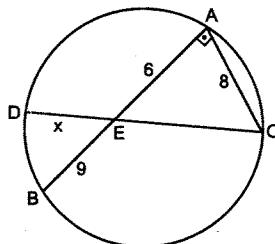
53.



$x = ?$

Cevap: 4

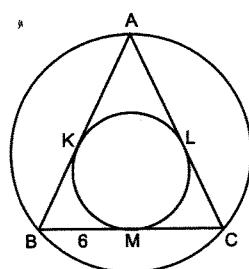
54.



$x = ?$

Cevap: 5,4

51.

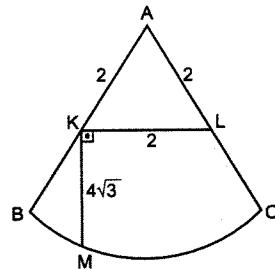


ABC eşkenar üçgen

$R - r = ?$

Cevap:  $2\sqrt{3}$ 

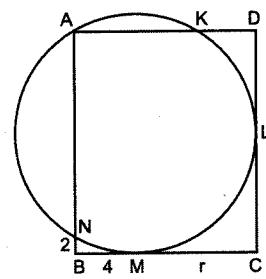
55.

A merkezli çember yarıçapı  
 $r = ?$ 

$r = ?$

Cevap:  $2\sqrt{19}$ 

52.

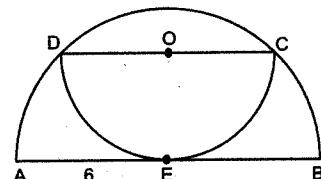


Dikdörtgen

$r = ?$

Cevap: 5

56.

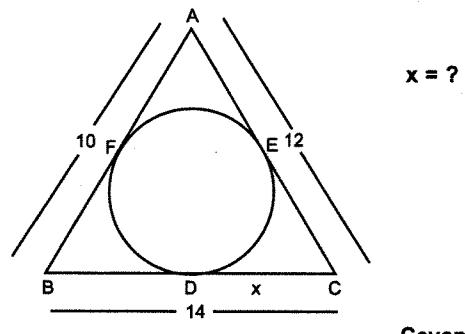


[AB] çap

$|DC| = ?$

Cevap:  $6\sqrt{2}$

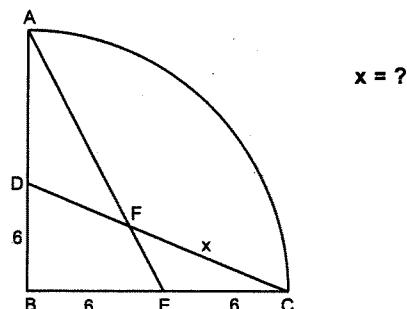
57.



$x = ?$

Cevap: 8

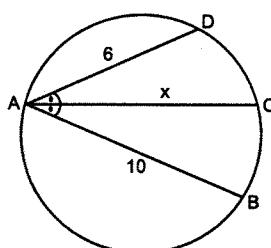
61.



$x = ?$

Cevap:  $4\sqrt{5}$ 

58.

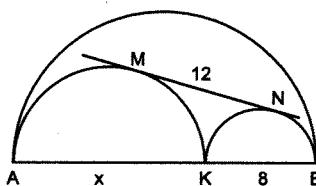


[AB] çap

$x = ?$

Cevap:  $4\sqrt{5}$ 

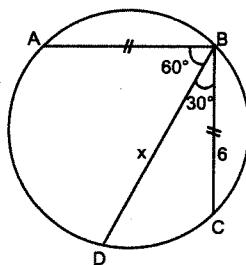
62.



$x = ?$

Cevap: 18

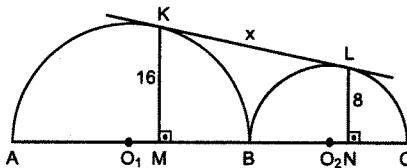
59.



$x = ?$

Cevap:  $3\sqrt{3} + 3$ 

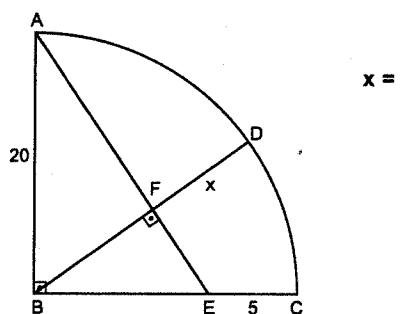
63.



$x = ?$

Cevap: 24

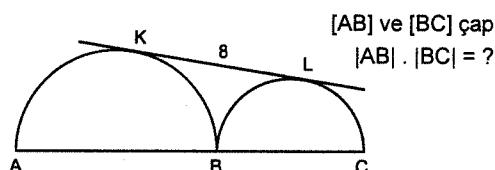
60.



$x = ?$

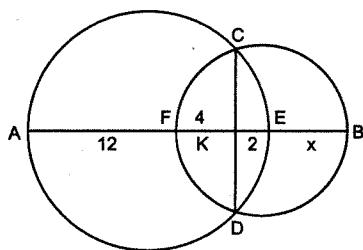
Cevap: 8

64.

[AB] ve [BC] çap  
 $|AB| \cdot |BC| = ?$ 

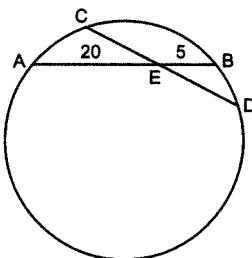
Cevap: 64

65.



$x = ?$

69.

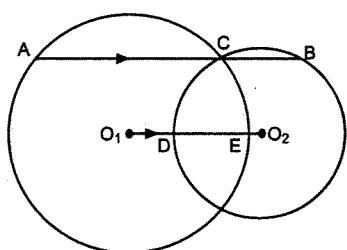


E noktasından geçen en kısa kiriş [CD] ise

$|CD| = ?$

Cevap: 20

66.

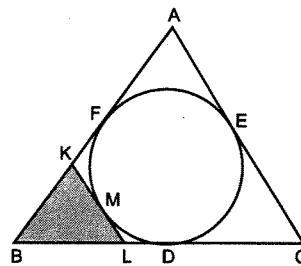


$|AB| = 16$

$|O_1O_2| = ?$

Cevap: 8

70.



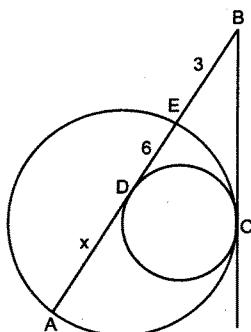
ABC eşkenar

$\hat{C}(ABC) = 30$

$\hat{C}(BKL) = ?$

Cevap: 10

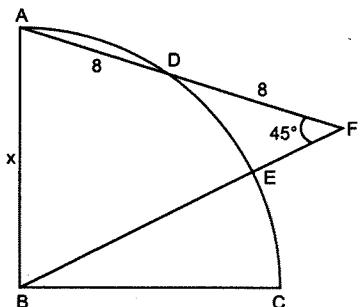
67.



$x = ?$

Cevap: 18

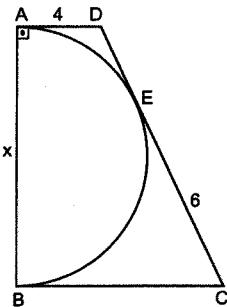
71.



$x = ?$

Cevap:  $4\sqrt{10}$ 

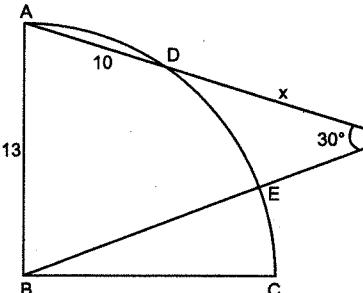
68.



$x = ?$

Cevap:  $4\sqrt{6}$ 

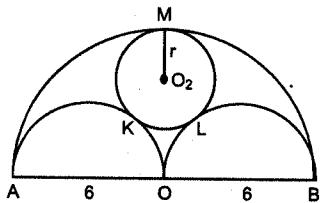
72.



$x = ?$

Cevap:  $12\sqrt{3} - 5$

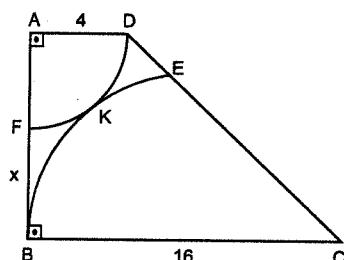
73.



$r = ?$

Cevap: 2

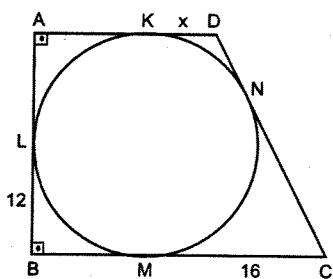
74.



$x = ?$

Cevap: 8

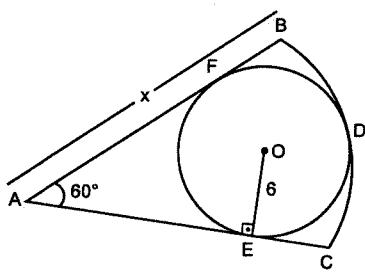
75.



$x = ?$

Cevap: 9

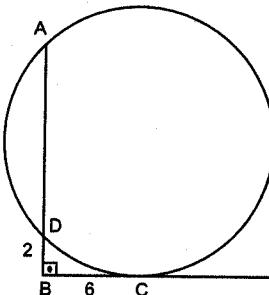
76.



$x = ?$

Cevap: 18

77.

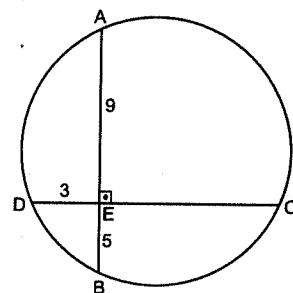


Çemberin yarıçapı

$r = ?$

Cevap: 10

78.

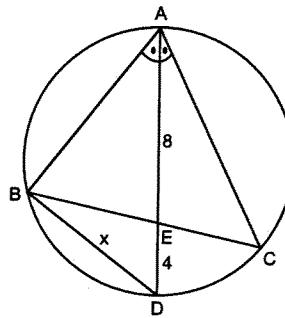


Çemberin yarıçapı

$r = ?$

Cevap:  $\sqrt{85}$ 

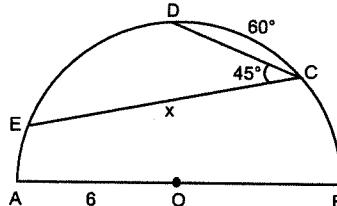
79.



$x = ?$

Cevap:  $4\sqrt{3}$ 

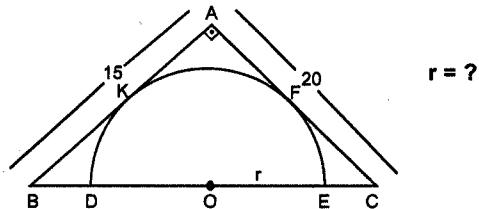
80.



$x = ?$

Cevap:  $3\sqrt{2} + 3\sqrt{6}$

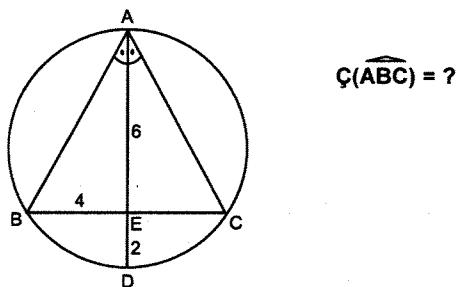
81.



$r = ?$

$\text{Cevap: } \frac{60}{7}$

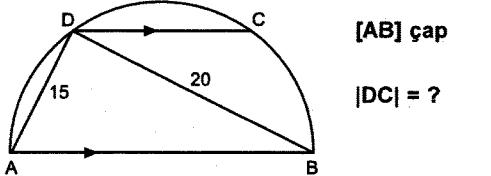
82.



$\hat{\angle}(\widehat{ABC}) = ?$

$\text{Cevap: } 21$

83.

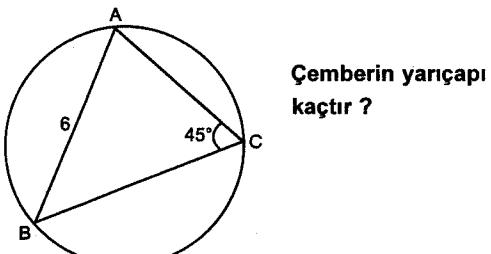


$[AB] \text{ çap}$

$|DC| = ?$

$\text{Cevap: } 7$

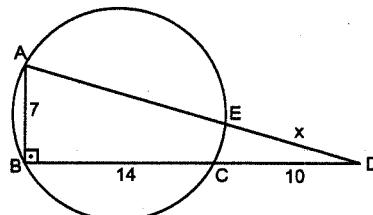
84.



Çemberin yarıçapı  
kaçtır?

$\text{Cevap: } 3\sqrt{2}$

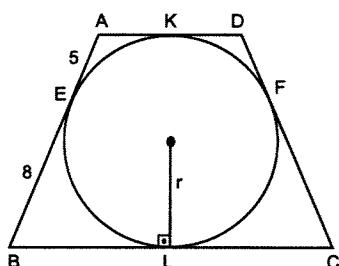
85.



$x = ?$

$\text{Cevap: } \frac{48}{5}$

86.

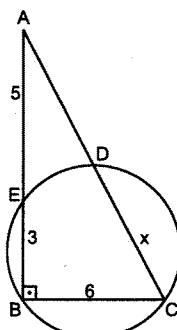


İkizkenar  
yamuk

$r = ?$

$\text{Cevap: } 2\sqrt{10}$

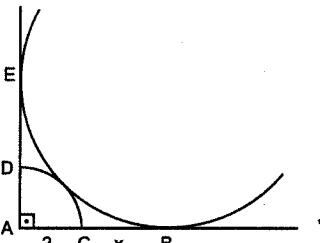
87.



$x = ?$

$\text{Cevap: } 6$

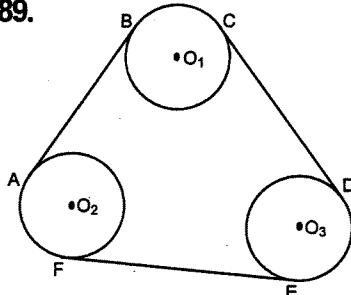
88.



$x = ?$

$\text{Cevap: } 2\sqrt{2}$

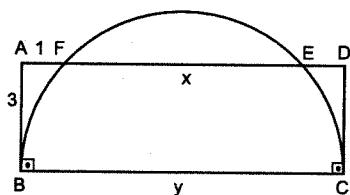
91.



Eşçemberler  
 $r = 3$   
 $\widehat{C(O_1O_2O_3)} = 12\pi$   
 ipin çevresi

Cevap:  $18\pi$ 

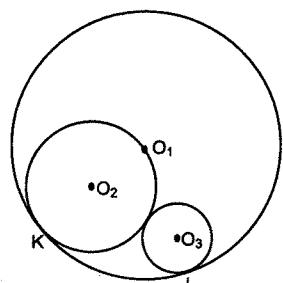
90.



ABCD  
 dikdörtgen  
 $y - x = ?$

Cevap: 2

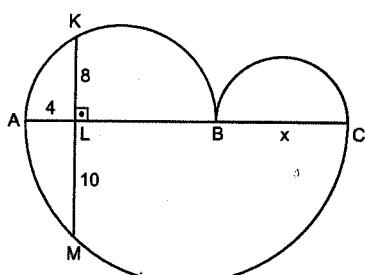
91.



$r_1 = 10$   
 $r_3 = 4$   
 $\widehat{C(O_1O_2O_3)} = ?$

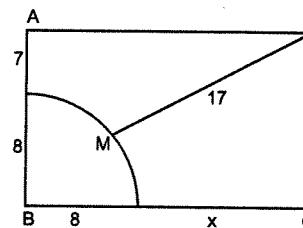
Cevap: 20

92.

 $x = ?$ 

Cevap: 9

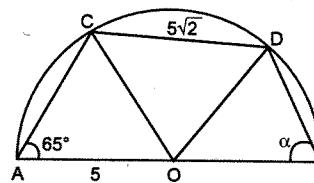
93.



D noktasının  
 çembere en  
 yakın uzaklığı  
 M ise  
 $|DM| = 17$   
 $x = ?$

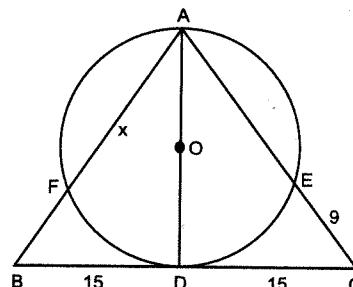
Cevap: 12

94.

 $\alpha = ?$ 

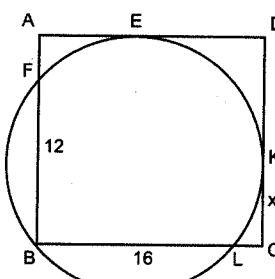
Cevap: 70

95.

 $x = ?$ 

Cevap: 16

96.

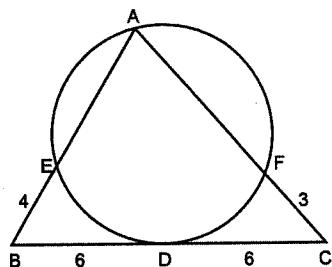


ABCD dikdörtgen

 $x = ?$ 

Cevap: 6

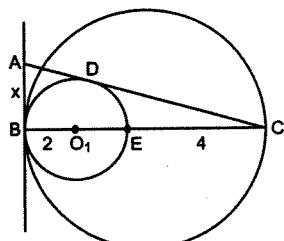
97.



$$\hat{c}(ABC) = ?$$

Cevap: 33

98.

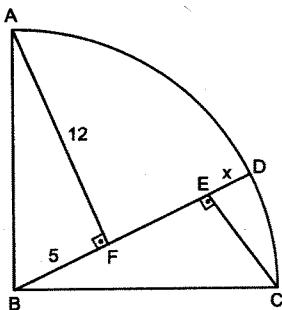


$$|BC| \text{ çap}$$

$$x = ?$$

Cevap:  $2\sqrt{2}$ 

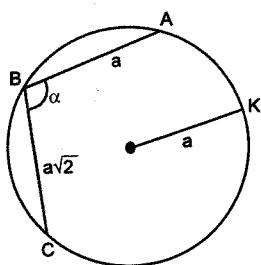
99.



$$x = ?$$

Cevap: 1

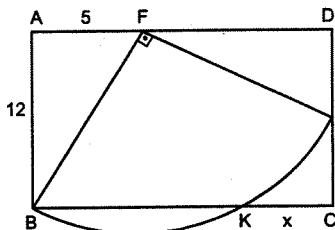
100.



$$\alpha = ?$$

Cevap: 105

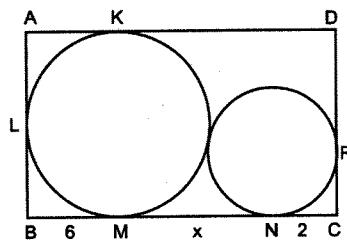
101.



$$x = ?$$

Cevap: 7

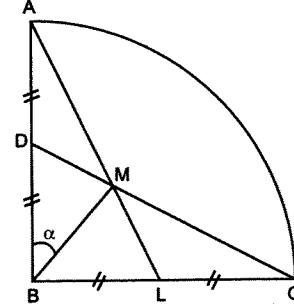
102.



$$x = ?$$

Cevap:  $4\sqrt{3}$ 

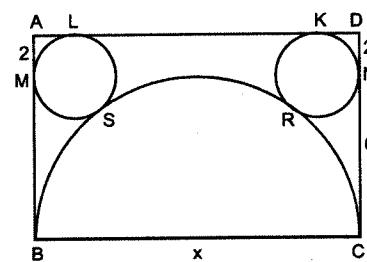
103.



$$\alpha = ?$$

Cevap: 45

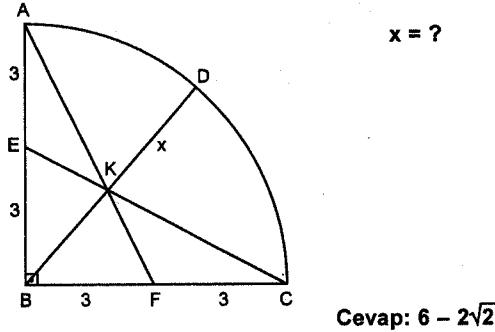
104.



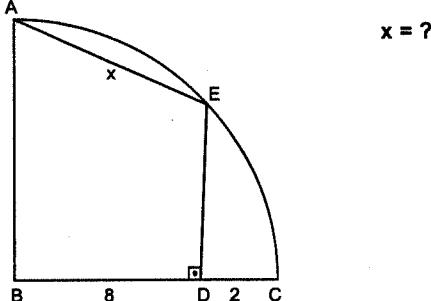
$$x = ?$$

Cevap: 9

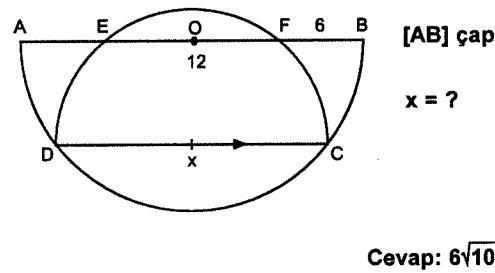
105.



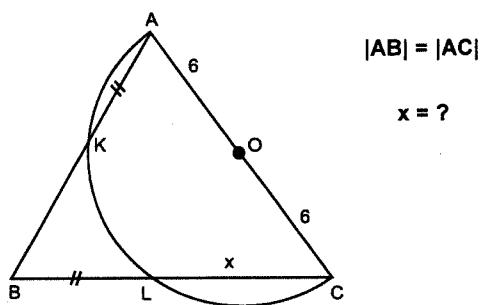
109.



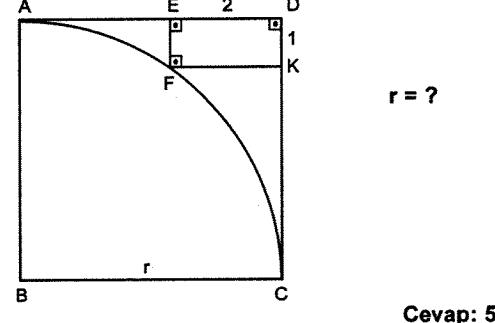
106.



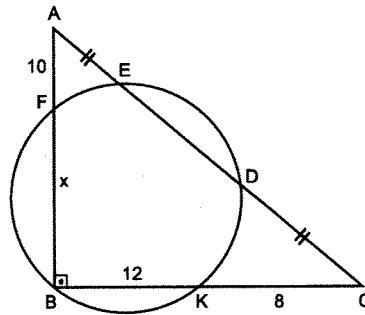
110.



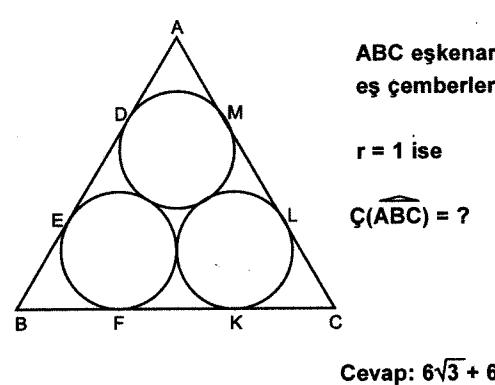
107.



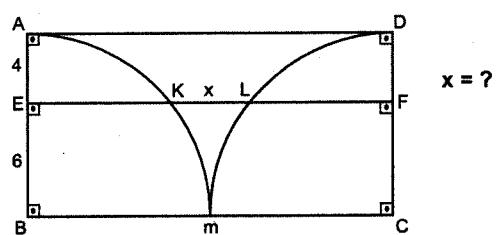
111.



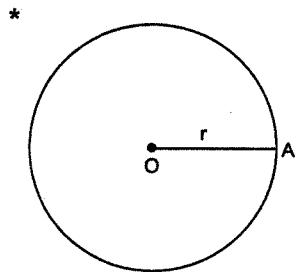
108.



112.

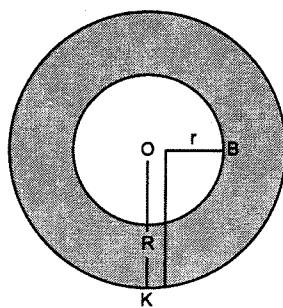


## DAİREDE ALAN

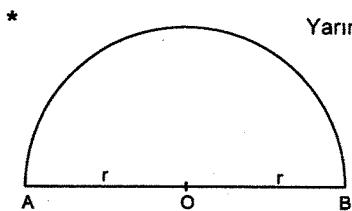


Dairenin Alanı:  $\pi r^2$

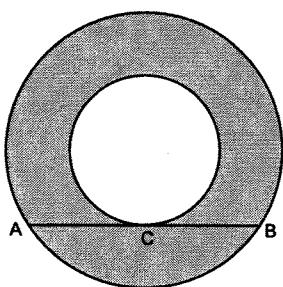
Çemberin çevresi:  $2\pi r$



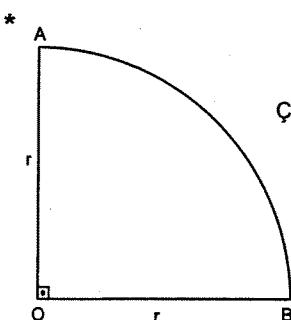
T.A =  $\pi(R^2 - r^2)$



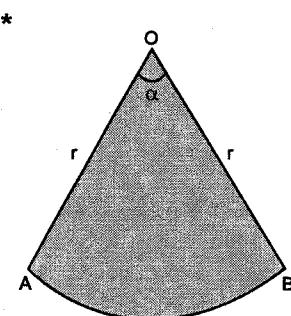
Yarım Dairenin Alanı:  $\frac{\pi r^2}{2}$



T.A =  $\left(\frac{|AB|}{2}\right)^2 \pi$



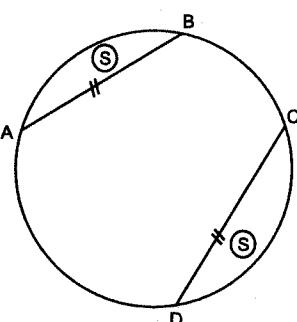
Çeyrek Dairenin Alanı  $\frac{\pi r^2}{4}$



Taralı Alan =  $\frac{\alpha}{360} \pi r^2$

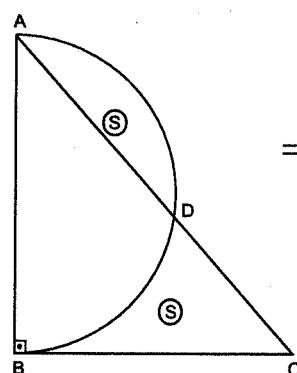
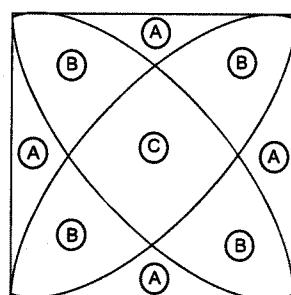
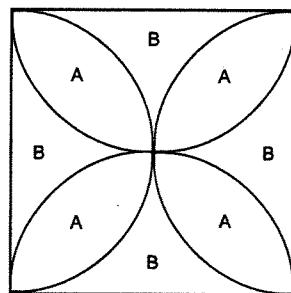
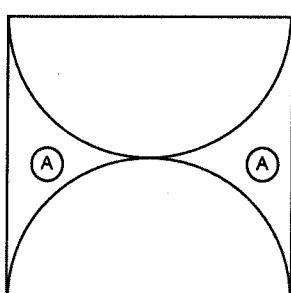
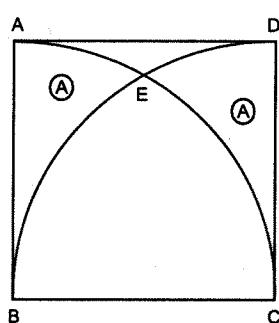
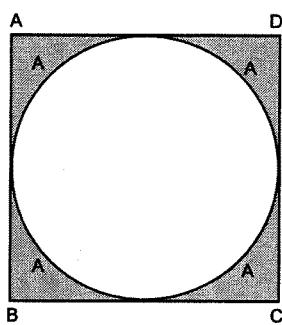
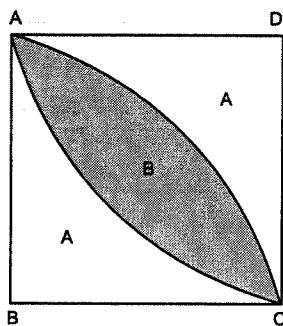
$|\widehat{AB}| = \frac{\alpha}{360} \cdot 2\pi r$

$$T.A = \frac{|\widehat{AB}| \cdot r}{2}$$

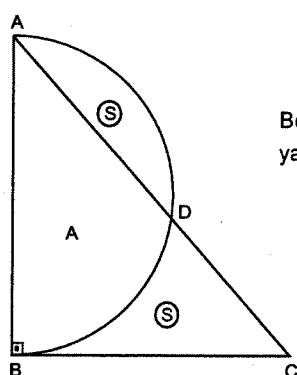


$|AB| = |DC| \Rightarrow$  Arkadaki Daire parçaları eşittir.

- Dairede alanda simetri şekiller çizilmişse eşit alanlara S, A, B gibi bulunduğuları yerleri harflendirin.



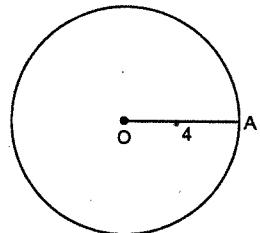
⇒ Alanlar eşit ise



Boş bulduğumuz yere A yazarak soruyu çözebiliriz.

$$\text{Yarım Dairenin Alanı} = A(\widehat{ABC})$$

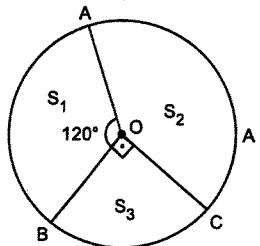
1.



Çevre = ?  
Alan = ?

Çevre  $8\pi$   
Alan  $16\pi$

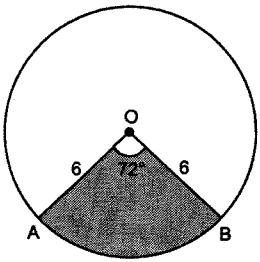
2.



$$\frac{S_1 + S_2}{S_3} = ?$$

Cevap: 3

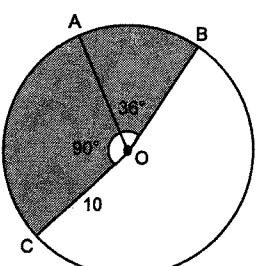
3.



T.A = ?

Cevap:  $\frac{36\pi}{5}$

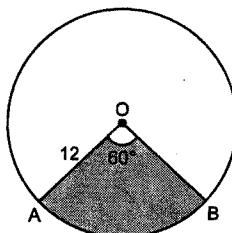
4.



T.A = ?

Cevap:  $35\pi$

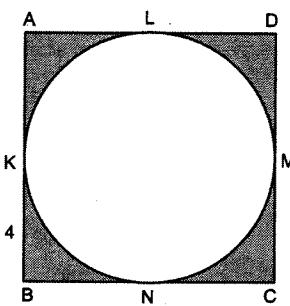
5.



T.A = ?

Cevap:  $24\pi$

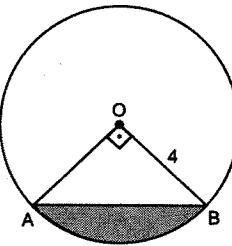
6.



T.A = ?

Cevap:  $64 - 16\pi$

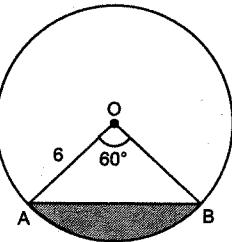
7.



T.A = ?

Cevap:  $4\pi - 8$

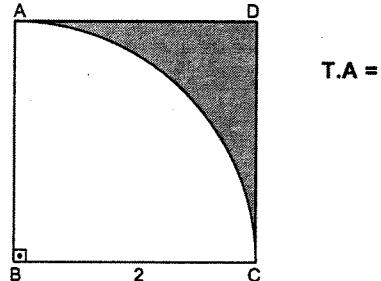
8.



T.A = ?

Cevap:  $6\pi - 9\sqrt{3}$

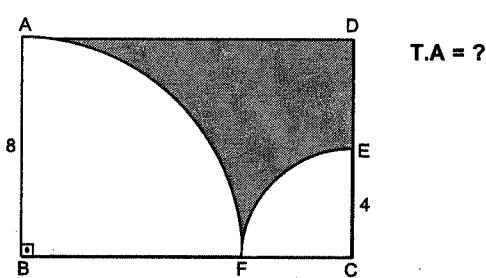
9.



$$\text{T.A} = ?$$

Cevap:  $4 - \pi$

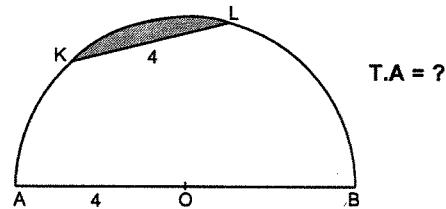
10.



$$\text{T.A} = ?$$

Cevap:  $96 - 20\pi$

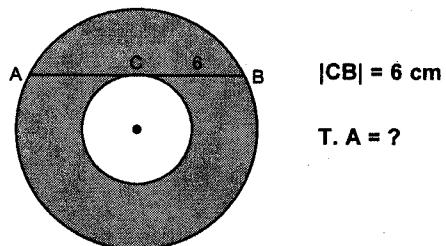
13.



$$\text{T.A} = ?$$

$$\text{Cevap: } \frac{8\pi}{3} - 4\sqrt{3}$$

14.

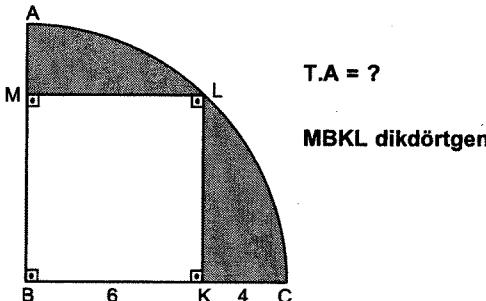


$$|\text{CB}| = 6 \text{ cm}$$

$$\text{T.A} = ?$$

$$\text{Cevap: } 36\pi$$

11.

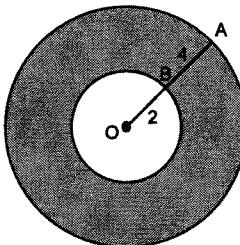


$$\text{T.A} = ?$$

MBKL dikdörtgen

Cevap:  $25\pi - 48$

15.

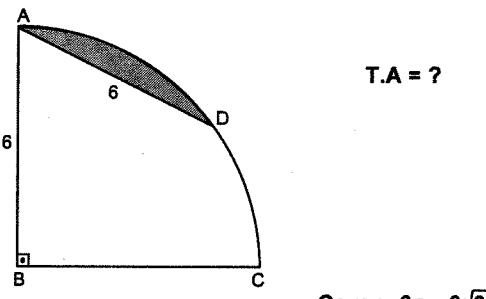


$$\text{T.A} = ?$$

$$|\text{AB}| = 4 \text{ cm}$$

$$\text{Cevap: } 32\pi$$

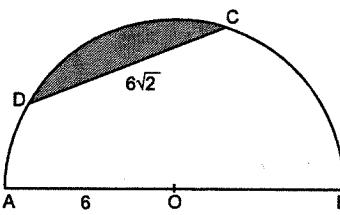
12.



$$\text{T.A} = ?$$

Cevap:  $6\pi - 9\sqrt{3}$

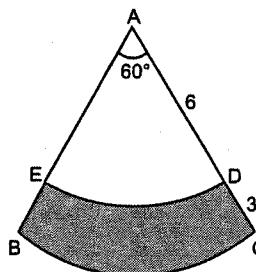
16.



$$6\sqrt{2}$$

$$\text{Cevap: } 9\pi - 18$$

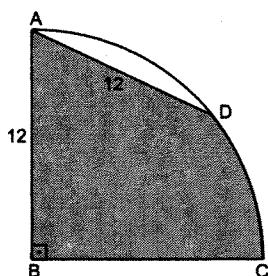
17.



T.A = ?

$$\text{Cevap: } \frac{15\pi}{2}$$

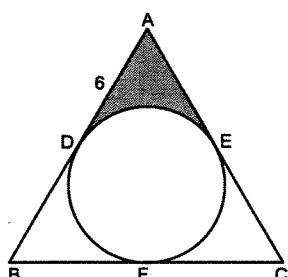
18.



T.A = ?

$$\text{Cevap: } 12\pi + 36\sqrt{3}$$

19.

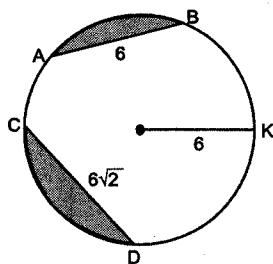


ABC eşkenar

T.A = ?

$$\text{Cevap: } 12\sqrt{3} - 4\pi$$

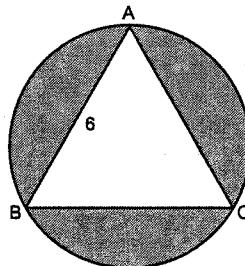
20.



T.A = ?

$$\text{Cevap: } 15\pi - 18 - 9\sqrt{3}$$

21.

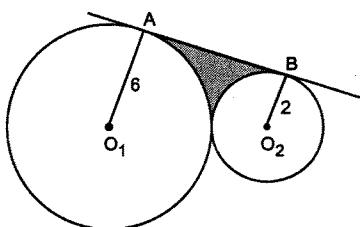


ABC eşkenar

T.A = ?

$$\text{Cevap: } 12\pi - 9\sqrt{3}$$

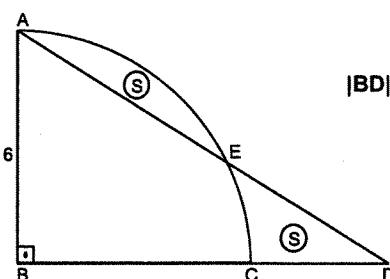
22.



T.A = ?

$$\text{Cevap: } 16\sqrt{3} - \frac{22\pi}{3}$$

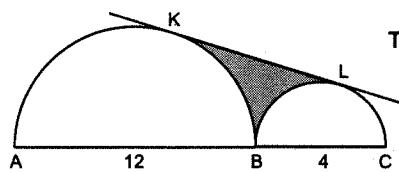
23.



|BD| = ?

$$\text{Cevap: } 3\pi$$

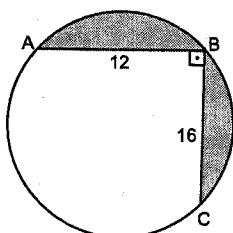
24.



T.A = ?

$$\text{Cevap: } 16\sqrt{3} - \frac{22\pi}{3}$$

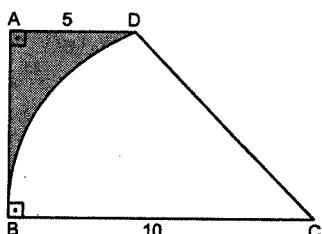
25.



T.A = ?

Cevap:  $50\pi - 96$ 

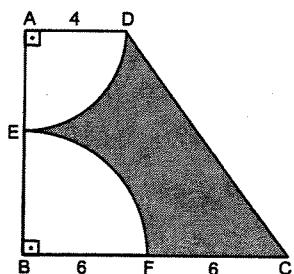
26.

C merkezli  
çember yayı

T.A = ?

Cevap:  $\frac{75\sqrt{3}}{2} - \frac{50\pi}{3}$ 

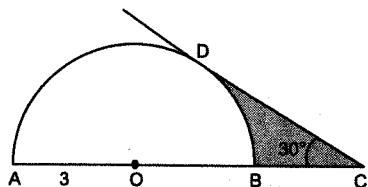
27.



T.A = ?

Cevap:  $80 - 13\pi$ 

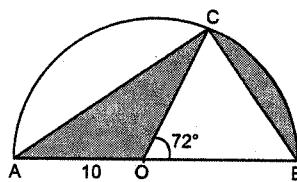
28.



T.A = ?

Cevap:  $\frac{9\sqrt{3}}{2} - \frac{3\pi}{2}$ 

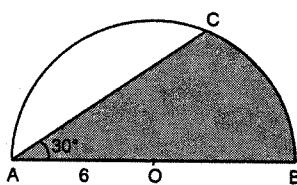
29.



T.A = ?

Cevap:  $20\pi$ 

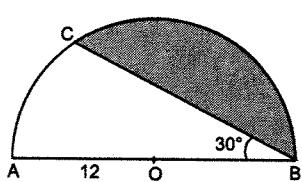
30.



T.A = ?

Cevap:  $6\pi + 9\sqrt{3}$ 

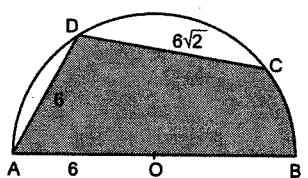
31.



T.A = ?

Cevap:  $48\pi - 36\sqrt{3}$ 

32.



T.A = ?

Cevap:  $3\pi + 18 + 9\sqrt{3}$

33.



T.A = ?

Cevap:  $36 - 9\pi$ 

34.



T.A = ?

Cevap:  $24\pi - 18\sqrt{3}$ 

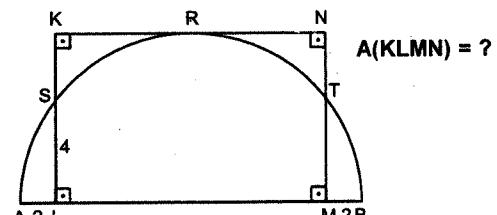
35.



T.A = ?

Cevap:  $9\sqrt{3} - 3\pi$ 

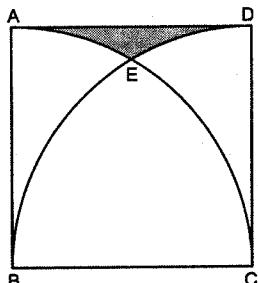
36.



A(KLMN) = ?

Cevap: 30

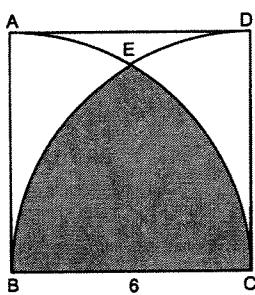
37.



T.A = ?

Cevap:  $36 - 6\pi - 9\sqrt{3}$ 

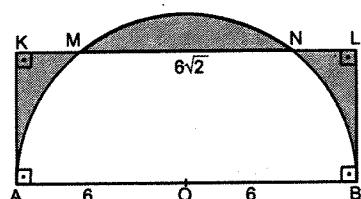
38.



T.A = ?

Cevap:  $12\pi - 9\sqrt{3}$ 

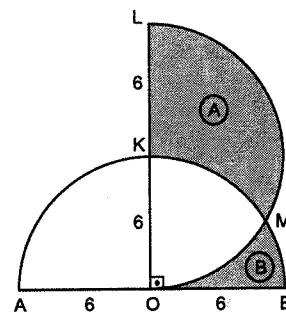
39.



T.A = ?

Cevap:  $36\sqrt{2} - 36$ 

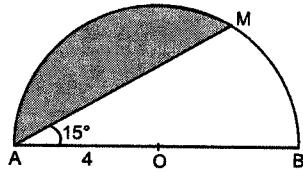
40.



A - B = ?

Cevap:  $9\pi$

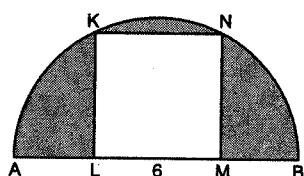
41.



T.A = ?

$$\text{Cevap: } \frac{20\pi}{3} - 4$$

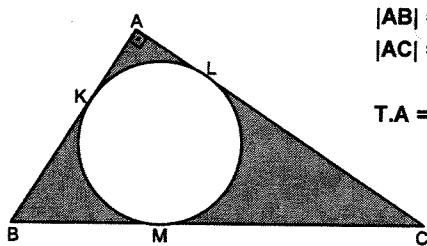
42.



KLMN Kare

$$\text{Cevap: } \frac{45\pi}{2} - 36$$

43.

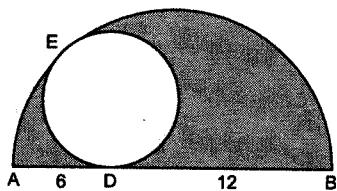


$$|AB| = 5 \\ |AC| = 12$$

T.A = ?

$$\text{Cevap: } 30 - 4\pi$$

44.

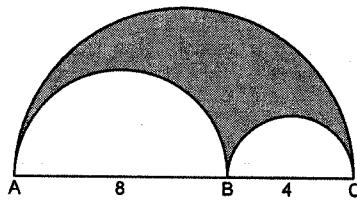


[AB] çap

T.A = ?

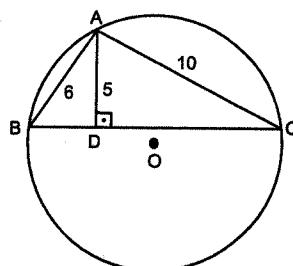
$$\text{Cevap: } \frac{49\pi}{2}$$

45.

T.A = ?  
[AB] ve [BC] çap

$$\text{Cevap: } 8\pi$$

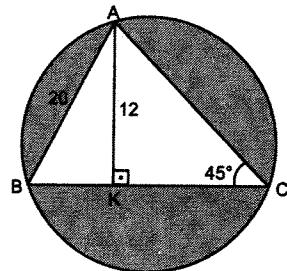
46.



Dairenin alanı ?

$$\text{Cevap: } 36\pi$$

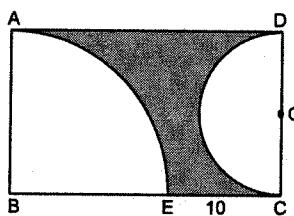
47.



T.A = ?

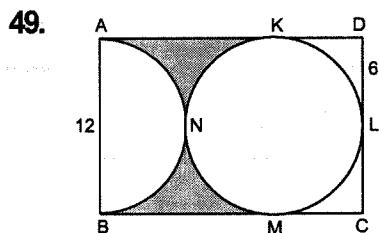
$$\text{Cevap: } 200\pi - 168$$

48.

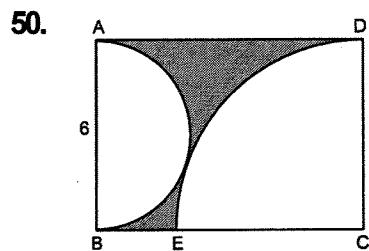
Daireler arası  
en kısa uzunluk  
4 cm ise

T.A = ?

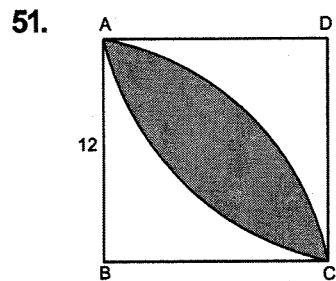
$$\text{Cevap: } 336 - \frac{147\pi}{2}$$

ABCD  
dikdörtgen

T.A = ?

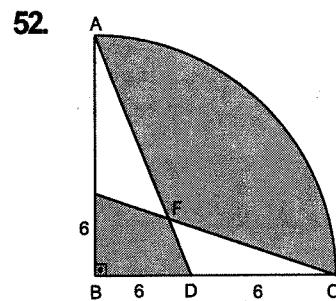
Cevap:  $144 - 36\pi$ 

T.A = ?

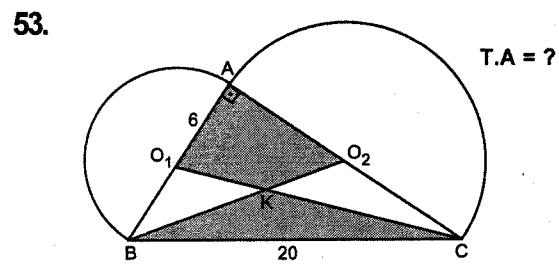
ABCD  
dikdörtgenCevap:  $36\sqrt{2} - \frac{27\pi}{2}$ 

T.A = ?

ABCD kare

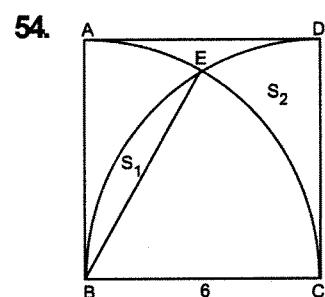
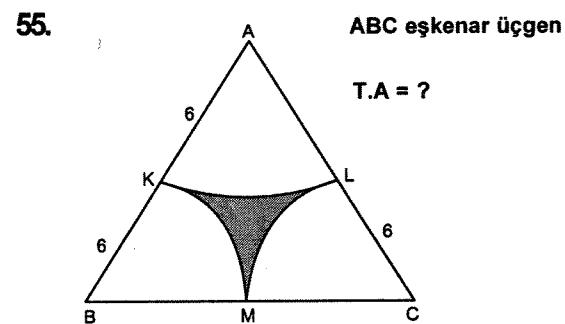
Cevap:  $72\pi - 144$ 

T.A = ?

Cevap:  $36\pi - 24$ 

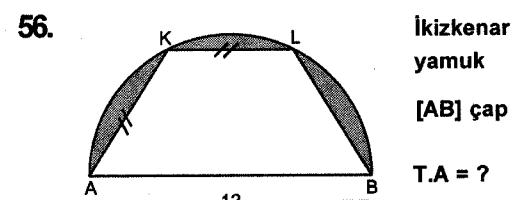
T.A = ?

Cevap: 64

 $S_2 - S_1 = ?$ Cevap:  $18\sqrt{3} - 9\pi$ 

ABC eşkenar üçgen

T.A = ?

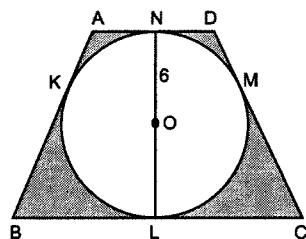
Cevap:  $36\sqrt{3} - 18\pi$ İkizkenar  
yamuk

[AB] çap

T.A = ?

Cevap:  $18\pi - 27\sqrt{3}$

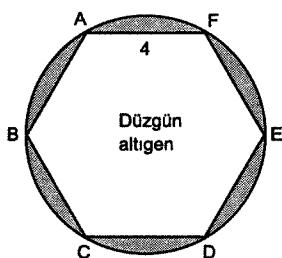
57.



İkizkenar  
yamuk  
Ortaban = 20 cm  
ise  
 $T.A = ?$

Cevap:  $240 - 36\pi$

58.

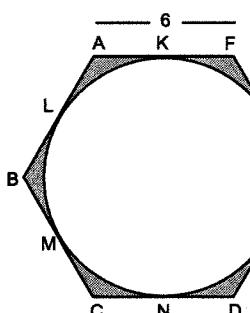


$T.A = ?$

Dügün  
altigen

Cevap:  $16\pi - 24\sqrt{3}$

59.

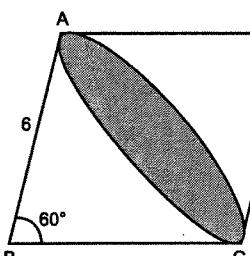


Dügün altigen

$T.A = ?$

Cevap:  $54\sqrt{3} - 27\pi$

60.

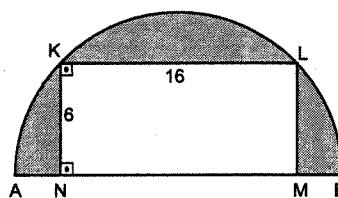


Paralelkenar

$T.A = ?$

Cevap:  $12\pi - 18\sqrt{3}$

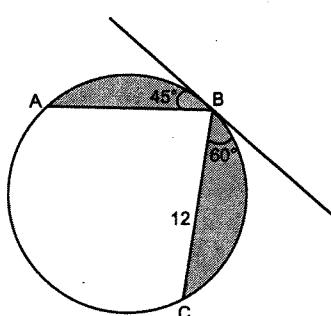
61.



$T.A = ?$

Cevap:  $50\pi - 96$

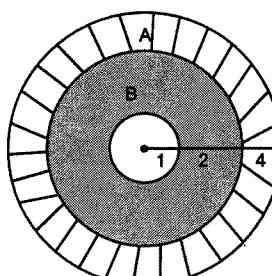
62.



$T.A = ?$

Cevap:  $28\pi - 24 - 12\sqrt{3}$

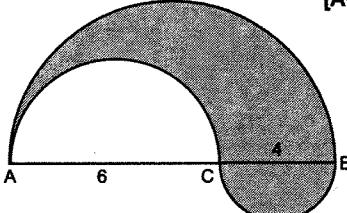
63.



$A - B = ?$

Cevap:  $32\pi$

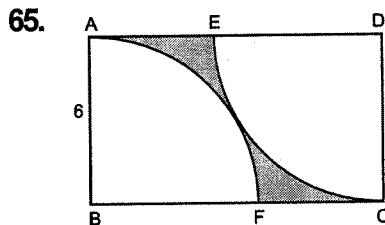
64.



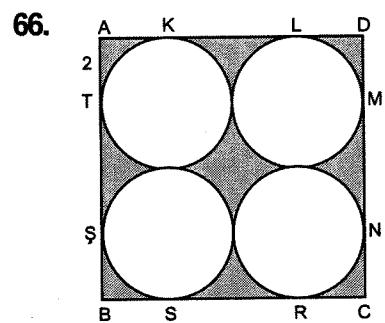
[AC] ve [BC] çap

$T.A = ?$

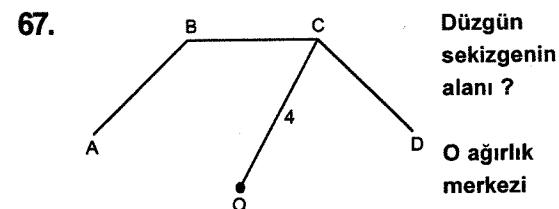
Cevap:  $10\pi$



T.A. = ?

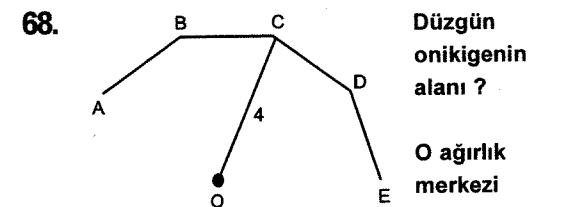
Cevap:  $36\sqrt{3} - 18\pi$ Eş daireler  
ABCD kare

T.A. = ?

Cevap:  $64 - 16\pi$ 

Düzenin sekizgenin alanı ?

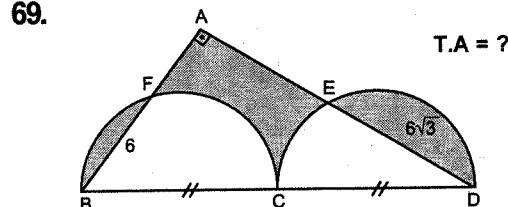
O ağırlık merkezi

Cevap:  $32\sqrt{2}$ 

Düzenin onikigenin alanı ?

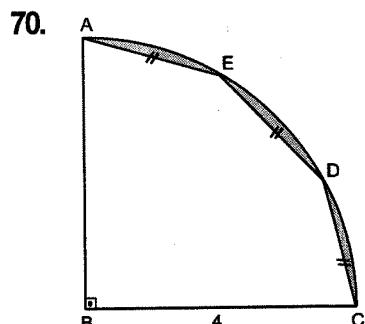
O ağırlık merkezi

Cevap: 48



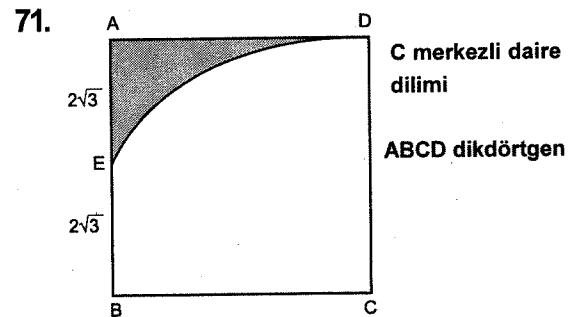
T.A. = ?

T.A. = ?

Cevap:  $36\sqrt{3}$ 

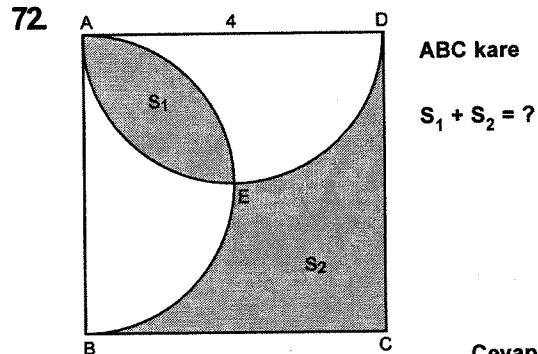
T.A. = ?

T.A. = ?

Cevap:  $4\pi - 12$ 

C merkezli daire dilimi

ABCD dikdörtgen

Cevap:  $18\sqrt{3} - 8\pi$ 

ABC kare

 $S_1 + S_2 = ?$ 

Cevap: 8

# TRİGONOMETRİ

## BÖLÜM - I

### Açı ölçü çeşitleri:

Derece , Radyan , Grad  
(D) (R) (G)

### Esas Ölçünün Bulunuşu:

- Pozitif yönlü açıların esas ölçülerinin bulunuşu açı derece cinsinden verilmişse  $360^\circ$  nin katları, Radyan cinsinden verilmişse  $2\pi$  nin katları atılarak bulunur.
- Negatif yönlü açıların esas ölçülerinin bulunuşu açı pozitifmiş gibi esas ölçü bulunur ve bulunan değer, derece cinsinden ise  $360^\circ$  den radyan cinsinden ise  $2\pi$  den çıkarılarak bulunur.

**Örnek:**  $3270^\circ$  nin esas ölçüsü?

$$\begin{array}{r} 3270 \\ \underline{-} 360 \\ = 30 \end{array}$$

esas ölçüsü  $30^\circ$  dir.

**Örnek:**  $-3270^\circ$  nin esas ölçüsü?

$$\begin{array}{r} 3270 \\ \underline{-} 360 \\ = 3240 \\ \underline{-} 360 \\ = 30 \end{array}$$

$360 - 30$  esas ölçüsü  $330^\circ$  dir.

**Örnek:**  $64 \frac{\pi}{7}$  nin esas ölçüsü?

paydanın 2 katı alınır. Paya bölünür.

$$\begin{array}{r} 64 \quad | \quad 14 \\ \underline{-} 56 \quad | \quad 4 \\ = 8 \end{array} \quad \text{esas ölçüsü } \frac{8\pi}{7}$$

$$4.2\pi + \left(\frac{8\pi}{7}\right) = \frac{64\pi}{7}$$

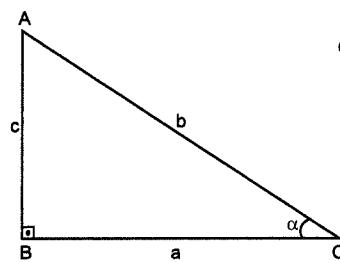
**Örnek:**  $\frac{113\pi}{5}$  nin esas ölçüsü?

paydanın 2 katı alınır. Paya bölünür.

$$\begin{array}{r} 113 \quad | \quad 10 \\ \underline{-} 110 \quad | \quad 11 \\ = 3 \end{array} \quad \text{esas ölçüsü } \frac{3\pi}{5}$$

$$\frac{113\pi}{5} = 11.2\pi + \left(\frac{3\pi}{5}\right)$$

### Dik Üçgende Trigonometri Bağıntıları:



$\alpha$  açısı için;  
Karşı dik kenar  $\rightarrow c$   
Komşu dik kenar  $\rightarrow a$   
Hipotenüs  $\rightarrow b$

$$\text{Sinüs} \rightarrow \frac{\text{Karşı dik kenar}}{\text{Hipotenüs}} = \frac{c}{b}$$

$$\text{Cosinüs} \rightarrow \frac{\text{Komşu dik kenar}}{\text{Hipotenüs}} = \frac{a}{b}$$

$$\text{Tanjant} \rightarrow \frac{\text{Karşı dik kenar}}{\text{Komşu dik kenar}} = \frac{c}{a}$$

$$\left( \frac{\sin \alpha}{\cos \alpha} \right)$$

$$\text{Cotanjant} \rightarrow \frac{\text{Komşu dik kenar}}{\text{Karşı dik kenar}} = \frac{a}{c}$$

$$\left( \frac{\cos \alpha}{\sin \alpha} \right)$$

$$\text{Secant} \rightarrow \frac{1}{\cos x} \quad \text{Cosecx} = \frac{1}{\sin x}$$

➤ Birbirini  $90^\circ$  ye tamamlayan açıların sinüsü, cosinusune cosinüsü sinüsüne, tanjanti cotanjantına, cotanjantı, tanjantına eşittir.

$$\sin x = \cos(90-x)$$

$$\cos x = \sin(90-x)$$

$$\cot x = \tan(90-x)$$

$$\tan x = \cot(90-x)$$

$$\text{Örnek: } \sin 30^\circ = \cos 60^\circ$$

$$\cos 70^\circ = \sin 20^\circ$$

$$\tan 40^\circ = \cot 50^\circ$$

$$\cot 25^\circ = \tan 65^\circ$$

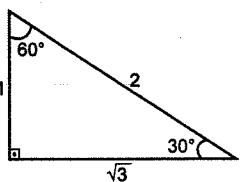
**Örnek:**  $x + y = 90^\circ \Rightarrow \tan x = \cot y$

$$\text{Örnek: } 7x = \frac{\pi}{2}$$

$$\sin 4x = \cos 3x$$

$$\tan 2x = \cot 5x \text{ gibi.}$$

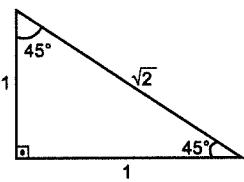
**Dik Üçgende Bazı Özel Açıların Trigonometrik Değerleri:**



$$\sin 30^\circ = \frac{1}{2} = \cos 60^\circ$$

$$\tan 30^\circ = \frac{1}{\sqrt{3}} = \cot 60^\circ$$

$$\tan 60^\circ = \sqrt{3} = \cot 30^\circ$$



$$\sin 60^\circ = \frac{\sqrt{3}}{2} = \cos 30^\circ$$

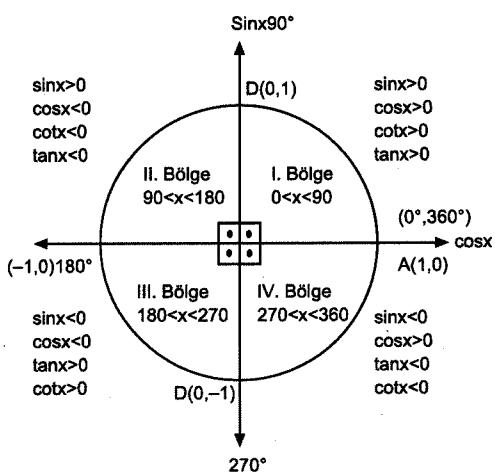
$$\tan 45^\circ = 1 = \cot 45^\circ$$

$$\cos 45^\circ = \sin 45^\circ = \frac{\sqrt{2}}{2}$$

**BİRİM ÇEMBER**

Merkezi orjin, yarıçapı 1 br olan çembere birim çember denir.

$$x^2 + y^2 = 1$$



$$\sin 0 = 0$$

$$\cos 0 = 1$$

$$\tan 0 = 0$$

$$\cot 0 = +\infty$$

$$\sin 180^\circ = 0$$

$$\cos 180^\circ = -1$$

$$\tan 180^\circ = 0$$

$$\cot 180^\circ = -\infty$$

$$\sin 90^\circ = 1$$

$$\cos 90^\circ = 0$$

$$\tan 90^\circ = +\infty$$

$$\cot 90^\circ = 0$$

$$\sin 270^\circ = -1$$

$$\cos 270^\circ = 0$$

$$\tan 270^\circ = -\infty$$

$$\cot 270^\circ = 0$$

**Çok önemli:** Sinüs, cosinüs, tanjant ve Cot'ın içindeki açılar  $90^\circ$  den büyük ise bu açıların değeri dar açı açısından hesap edilmelidir.

Öncelikle parantez içindeki ifade birim çemberde kaçınıcı bölgeye denk geldiği bulunur. Bu bölgede işaretini ne ise yazılır. Sonra  $\alpha$ nın solundaki (yanındaki) ifade  $90^\circ$ ının tek katları ise  $\sin \rightarrow \cos$ 'a dönüşür.

$\cos \rightarrow \sin$ 'e    $\tan \rightarrow \cot$ 'a    $\cot \rightarrow \tan$ 'a

trigonometrik değerlerinin bilinmesi ile sonuç bulunur.

►  $90^\circ$  nin çift katlarında dönüşüm olmaz.

$$\sin(90^\circ + x) = +\cos x$$

2. bölge

$$\sin(180^\circ + x) = -\sin x$$

3. bölge

$$\sin\left(\frac{\pi}{2} - x\right) = \cos x$$

1. bölge

$$\sin\left(\frac{\pi}{2} + x\right) = +\cos x$$

2. bölge

$$\sin(\pi - x) = +\sin x$$

2. bölge

$$\sin(\pi + x) = -\sin x$$

3. bölge

$$\sin(3\frac{\pi}{2} - x) = -\cos x$$

3. bölge

$$\sin(3\frac{\pi}{2} + x) = -\cos x$$

4. bölge

$$\sin(3\pi - x) = +\sin x$$

2. bölge

$$\sin(2\pi - x) = -\sin x$$

4. bölge

$$\sin(2\pi + x) = +\sin x$$

1. bölge

$$\tan\left(\frac{\pi}{2} - x\right) = \cot x$$

1. bölge

$$\tan\left(\frac{\pi}{2} + x\right) = -\cot x$$

2. bölge

$$\tan(\pi - x) = -\tan x$$

2. bölge

$$\tan(\pi + x) = +\tan x$$

3. bölge

$$\tan\left(\frac{3\pi}{2} - x\right) = +\cot x$$

3. bölge

$$\tan\left(\frac{3\pi}{2} + x\right) = -\cot x$$

4. bölge

$$\tan(2\pi - x) = -\tan x$$

4. bölge

$$\tan(2\pi + x) = \tan x$$

1. bölge

**Örnek:**

$$\sin\left(\frac{\pi}{2} - x\right) + \cos\left(\frac{3\pi}{2} - x\right) + \tan(2\pi - x) + \cot\left(\frac{3\pi}{2} - x\right) = ?$$

**Cevap:**  $\cos x - \sin x$

**Örnek:**

$$\frac{\sin(90+x) + \cos(270+x) + \sin(270-x)}{\sin(2\pi-x) - \cos\left(\frac{\pi}{2} + x\right) - \sin(90-x)} = ?$$

**Cevap:**  $-\tan x$

**Örnek:**

$$\tan(\pi+x) - \cot(\pi-x) + \tan\left(\frac{3\pi}{2} + x\right) - \cot(2\pi-x) = ?$$

**Cevap:**  $\tan x + \cot x$

**Örnek:**

$$\frac{\tan(2\pi-x)}{\cot(\pi+x) - \tan\left(\frac{3\pi}{2} - x\right) - \cot\left(\frac{3\pi}{2} - x\right)} = ?$$

**Cevap:** 1

**Örnek:**

$$\sin x - \cos(90-x) + \cot(90+x) + \cot(90-x) - \tan(270-x) = ?$$

**Cevap:**  $-\cot x$

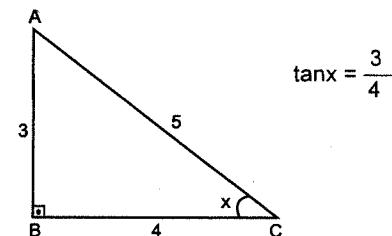
### TRİGONOMETRİK DEĞERLERDEN BİRİNİN VERİLMESİ DURUMUNDA DİĞERİNİN BULUNMASI

**Örnek:**  $0 < x < \frac{\pi}{2}$

$$\sin x = \frac{3}{5} \Rightarrow \tan x = ?$$

**Çözüm:**

Önce bir üçgen çizilir.

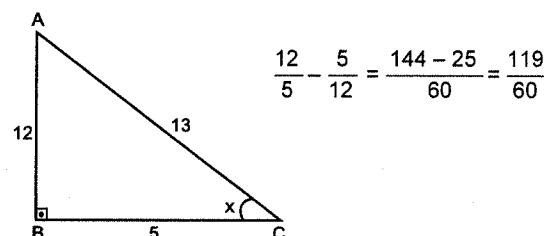


**Örnek:**  $0 < x < \frac{\pi}{2}$

$$\cos x = \frac{5}{13} \Rightarrow \tan x - \cot x = ?$$

**Çözüm:**

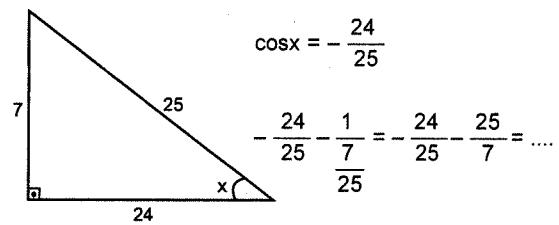
Önce bir üçgen çizilir.



**Örnek:**  $90 < x < 180$

$$\sin x = \frac{7}{25} \Rightarrow \cos x - \frac{1}{\sin x} = ?$$

**Çözüm:**

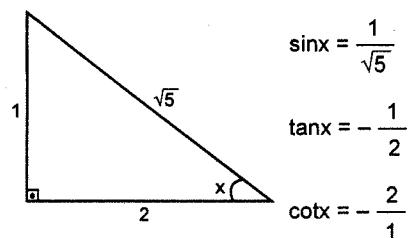


$90 < x < 180$  2. bölge

**Örnek:**  $90^\circ < x < 180^\circ$

$$\cos x = \frac{-2}{\sqrt{5}} \Rightarrow \frac{\sin x - \tan x}{\cot x} = ?$$

**Çözüm:**



$$\frac{\frac{1}{\sqrt{5}} - \left(-\frac{1}{2}\right)}{-2} = \frac{\frac{1}{\sqrt{5}} + \frac{1}{2}}{-2}$$

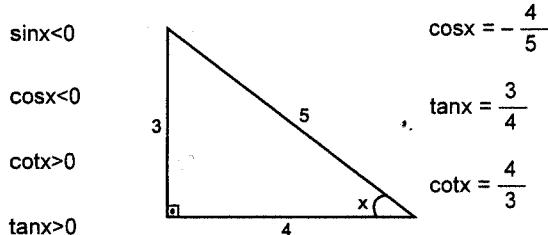
$90^\circ < x < 180^\circ \rightarrow 2.$  bölge

**Örnek:**  $\pi < x < \frac{3\pi}{2}$   $\sin x = \frac{-3}{5} \Rightarrow$

$$\frac{\cos^2 x - \sin x \cdot \cos x}{\cot x - \tan x} = ?$$

**Çözüm:**

$\pi < x < \frac{3\pi}{2}$  3. bölge



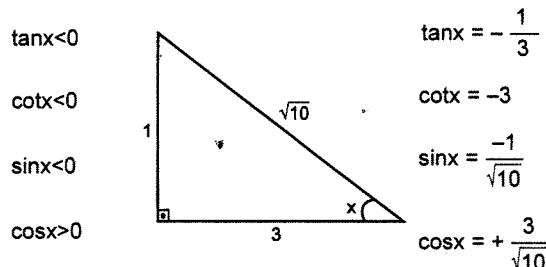
$$\begin{aligned} \left(\frac{-4}{5}\right)^2 - \left(-\frac{3}{5}\right) \cdot \left(-\frac{4}{5}\right) &= \frac{16}{25} - \frac{12}{25} = \frac{4}{25} \cdot \frac{12}{7} = \frac{48}{175} \\ \frac{4}{3} - \frac{3}{4} &= \dots \end{aligned}$$

(4) (3)

**Örnek:**  $\frac{3\pi}{2} < x < 2\pi$

$$\cot x = -3 \Rightarrow \frac{\tan x - \cot x}{\sin x - \cos x} = ?$$

**Örnek:**  $\frac{3\pi}{2} < x < 2\pi$  4. bölge

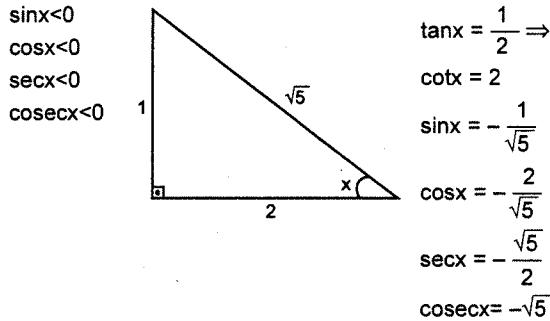


$$\frac{-\frac{1}{3} + (3)}{-\frac{1}{\sqrt{10}} - \frac{3}{\sqrt{10}}} = \frac{\frac{8}{3}}{-\frac{4}{\sqrt{10}}} = \frac{\frac{2}{3} \cdot \frac{\sqrt{10}}{4}}{-\frac{4}{\sqrt{10}}} = \frac{-2\sqrt{10}}{3}$$

**Örnek:**  $\pi < x < \frac{3\pi}{2}$

$$\tan x = \frac{1}{2} \Rightarrow \frac{\cot x}{\sin x + \cos x} - \sec x + \cos ec x = ?$$

**Çözüm:**  $\pi < x < \frac{3\pi}{2}$  3. bölge



$$\begin{aligned} \frac{2}{-\frac{1}{\sqrt{5}} - \frac{2}{\sqrt{5}}} - \left(\frac{2}{\sqrt{5}}\right) + \left(\frac{1}{\sqrt{5}}\right) &= \dots \end{aligned}$$

1.

$\sin x + \cos x = ?$

Cevap:  $\frac{7}{5}$ 

2.

ABCD kare  
 $\tan x = ?$

Cevap:  $\frac{1}{2}$ 

3.

ABC eşkenar  
 $\tan x = ?$

Cevap:  $2\sqrt{3}$ 

4.

$\sin x - \cos x = ?$

Cevap:  $\frac{7}{5}$ 

5.

$\cot x - \tan x = ?$

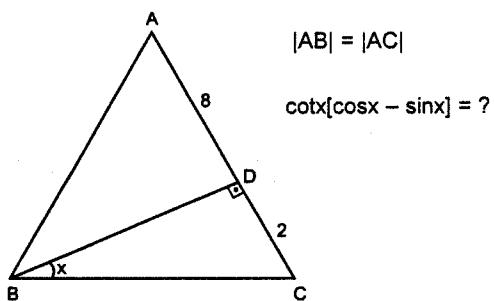
Cevap:  $\frac{7}{12}$ 

6.

ABCD yamuk  
 $\cot \alpha + \tan \alpha = ?$

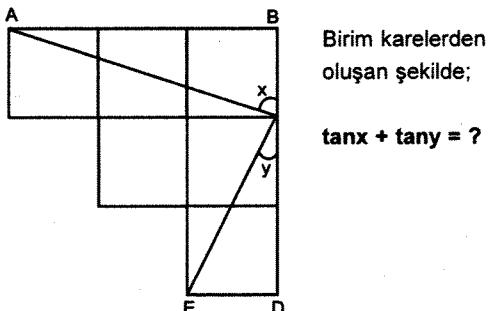
Cevap:  $\frac{25}{12}$

7.



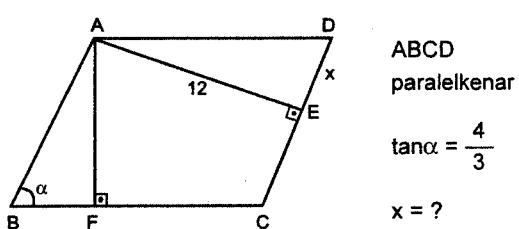
$$\text{Cevap: } \frac{3\sqrt{10}}{5}$$

8.



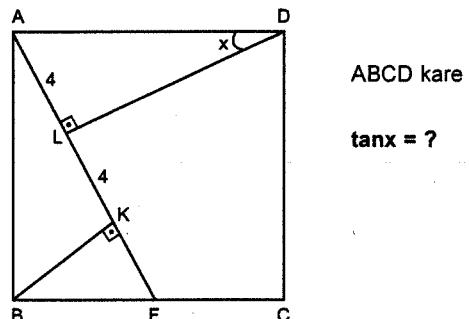
$$\text{Cevap: } \frac{7}{2}$$

9.



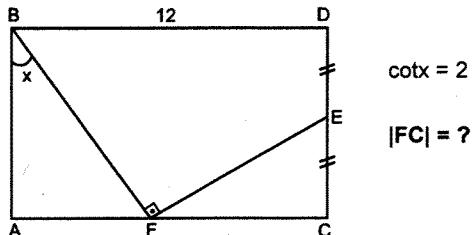
$$\text{Cevap: } 9$$

10.



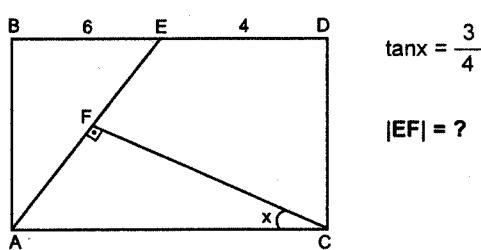
$$\text{Cevap: } \frac{1}{2}$$

11.



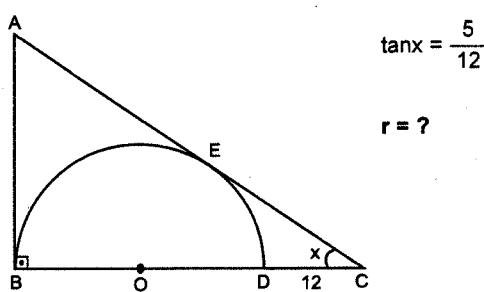
$$\text{Cevap: } 8$$

12.



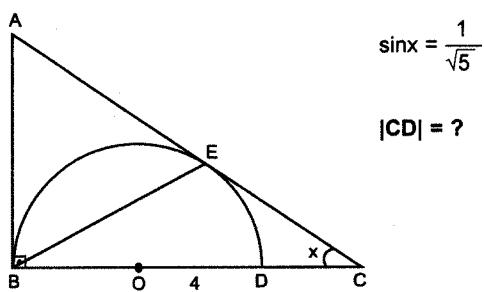
$$\text{Cevap: } 4$$

13.

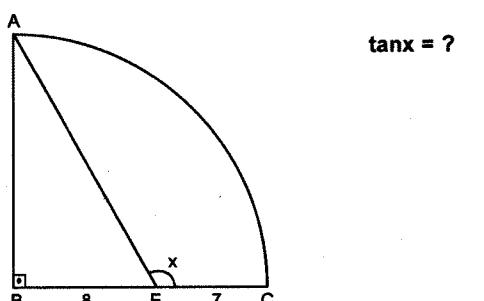


Cevap: 7,5

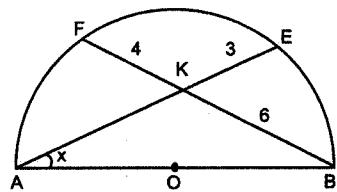
14.

Cevap:  
 $4\sqrt{5}-4$ 

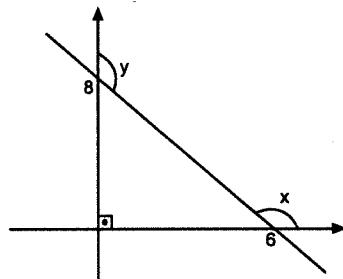
15.

Cevap:  $-\frac{15}{8}$ 

16.

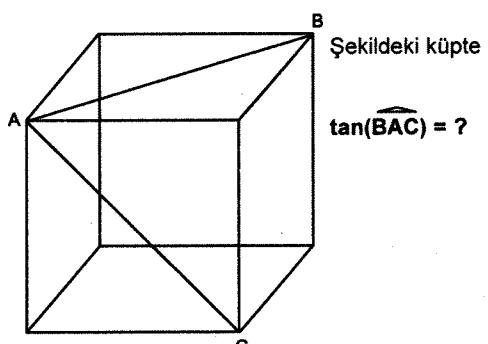
Cevap:  $\frac{3\sqrt{3}}{11}$ 

17.



Cevap: 1

18.

Cevap:  $\sqrt{3}$

1.  $\sin 240 - \sin 330 - \cos 120 - \cos 210 = ?$

Cevap: 1

$$\sin^2 x + \cos^2 x = 1$$

$$\tan x \cdot \cot x = 1$$

2.  $\cos 315 - \tan 225 + \cot 315 - \cos 135 = ?$

Cevap:  $\sqrt{2} - 2$

1.  $\frac{(1 - \sin x)(1 + \sin x)}{\cos x} = ?$

Cevap:  $\cos x$

3.  $\sin 270 - \cos 180 - \tan 180 - \cos 270 + \cot 270 = ?$

Cevap: 0

3.  $\sin^2 1 + \sin^2 2 + \sin^2 3 + \dots + \sin^2 89 = ?$

Cevap:  $\frac{89}{2}$

4.  $\cos 120 + \cos 135 - \sin 330 - \cos 60 + \sin 300 = ?$

Cevap:  $-\frac{1 + \sqrt{2} + \sqrt{3}}{2}$

4.  $\tan 1 \cdot \tan 2 \cdot \tan 3 \dots \tan 88 \cdot \tan 89 = ?$

Cevap: 1

5.  $\tan 135 - \tan 315 + \cot 150 - \cot 240 - \tan 120 = ?$

Cevap:  $-\frac{1}{\sqrt{3}}$

5.  $\frac{1 - \cos x}{\sin x} + \frac{\sin x}{1 - \cos x} = ?$

Cevap:  $2 \csc x$

6.  $\cot 150 - \sin 150 - \sin 210 + \cot 240 + \sin 330 + \cos 300 = ?$

Cevap:  $-\frac{2}{\sqrt{3}}$

6.  $\frac{1}{\sec x + \tan x} + \frac{1}{\sec x - \tan x} = ?$

Cevap:  $2 \sec x$

7.  $\tan x - \cot x = 2 \Rightarrow$

$$\tan^2 x + \cot^2 x = ?$$

Cevap: 6

8.  $\sin x - \cos x = \frac{1}{3} \Rightarrow \sin x \cdot \cos x = ?$

Cevap:  $\frac{4}{9}$

9.  $\sin x + \cos x = -\frac{1}{5} \Rightarrow \sin x \cdot \cos x = ?$

Cevap:  $-\frac{12}{25}$

10.  $6x = \frac{\pi}{2} \Rightarrow \frac{\sin x}{\cos 5x} + \frac{\tan 2x}{\cot 4x}$

Cevap: 2

11.  $7x = \pi \quad \frac{\sin x}{\sin 6x} + \frac{\cos x}{\cos 6x} - \frac{\tan 2x}{\tan 5x}$

Cevap: 1

12.  $13x = \pi \quad \frac{\sin 6x}{\sin 7x} + \frac{\cos 5x}{\cos 8x} = ?$

Cevap: 1

$$-1 \leq \sin x \leq 1, -1 \leq \cos x \leq 1$$

1.  $2\sin a - 6 = x \Rightarrow x$  in en büyük tamsayı değeri ?

Cevap: -4

2.  $\frac{3\cos a - 13}{2} = x \Rightarrow x$  in en büyük tamsayı değeri ?

Cevap: -5

3.  $\frac{\sin 2x - 2}{3} + \frac{\cos 2y + 6}{2}$  en büyük tamsayı değeri?

Cevap: 3

4.  $|1 - \sin x| + |2 - \cos x| - |4 - \cos x| + \sin x = ?$

Cevap: -1

5.  $|\cos x - 2| + |\sin x - 3| - |3 - \cos x| + |4 + \sin x| = ?$

Cevap: 6

## TRİGONOMETRİ – BÖLÜM II

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### Toplam – fark formülleri

$$\sin(a+b) = \sin a \cos b + \cos a \sin b$$

$$\sin(a-b) = \sin a \cos b - \cos a \sin b$$

$$\cos(a+b) = \cos a \cos b - \sin a \sin b$$

$$\cos(a-b) = \cos a \cos b + \sin a \sin b$$

$$\tan(a+b) = \frac{\tan a + \tan b}{1 - \tan a \cdot \tan b}$$

$$\tan(a-b) = \frac{\tan a - \tan b}{1 + \tan a \cdot \tan b}$$

$$\cot(a+b) = \frac{1}{\tan(a+b)}$$

### Yarım açı formülleri

$$\sin 2x = 2 \sin x \cos x$$

$$\begin{aligned} \cos 2x &= \cos^2 x - \sin^2 x \\ &= 2 \cos^2 x - 1 \\ &= 1 - 2 \sin^2 x \end{aligned}$$

$$\tan 2x = \frac{2 \tan x}{1 - \tan^2 x}$$

$$\cot 2x = \frac{1}{\tan 2x}$$

Örnek:

1.  $\sin 40 \cdot \cos 20 + \cos 40 \cdot \sin 20 = ?$

Cevap:  $\frac{\sqrt{3}}{2}$

2.  $\cos 60 \cdot \cos 15 + \sin 60 \cdot \sin 15 = ?$

Cevap:  $\frac{\sqrt{2}}{2}$

3.  $\sin 75 \cdot \cos 15 + \cos 75 \cdot \sin 15 = ?$

Cevap: 1

4.  $\frac{\tan 20 + \tan 10}{1 - \tan 20 \cdot \tan 10} = ?$

Cevap:  $\frac{1}{\sqrt{3}}$

5.  $\sin 15 = ?$

Cevap:  $\frac{\sqrt{6} - \sqrt{2}}{4}$

6.  $\cos 15 = ?$

Cevap:  $\frac{\sqrt{6} + \sqrt{2}}{4}$

7.  $\cos 105 = ?$

Cevap:  $\frac{\sqrt{2} - \sqrt{6}}{4}$

8.  $\tan 15 = ?$

Cevap:  $2 - \sqrt{3}$

9.  $\tan 165^\circ = ?$

Cevap:  $\sqrt{3} - 2$

10.  $\cos 345^\circ = ?$

Cevap:  $\frac{\sqrt{6} + \sqrt{2}}{4}$

11.  $\sin 255^\circ = ?$

Cevap:  $-\frac{\sqrt{6} + \sqrt{2}}{4}$

12.  $\sin 15^\circ + \cos 15^\circ = ?$

Cevap:  $\frac{\sqrt{6}}{2}$

13.  $\sin 15^\circ \cdot \cos 15^\circ = ?$

Cevap:  $\frac{1}{4}$

14.  $\sin 75^\circ \cdot \cos 75^\circ = ?$

Cevap:  $\frac{1}{4}$

15.  $\sin 105^\circ \cdot \cos 105^\circ = ?$

Cevap:  $-\frac{1}{4}$

16.  $\frac{\sin 36^\circ}{\sin 12^\circ} - \frac{\cos 36^\circ}{\cos 12^\circ} = ?$

Cevap: 2

17.  $0 < x < \frac{\pi}{2}$

$\sin x = \frac{3}{5} \Rightarrow \sin 2x = ?$

Cevap:  $\frac{24}{25}$

18.  $0 < x < \frac{\pi}{2}$

$\cos x = \frac{1}{3} \Rightarrow \sin 2x = ?$

Cevap:  $\frac{4\sqrt{2}}{9}$

19.  $0 < x < \frac{\pi}{2}$

$$\tan x = \frac{2}{3} \Rightarrow \sin 2x = ?$$

Cevap:  $\frac{12}{13}$

20.  $0 < x < \frac{\pi}{2}$

$$\cot x = \frac{3}{4} \Rightarrow \sin 2x = ?$$

Cevap:  $\frac{24}{25}$

21.  $0 < x < \frac{\pi}{2}$

$$\tan x = \frac{5}{12} \Rightarrow \cos 2x = ?$$

Cevap:  $\frac{119}{169}$

22.  $0 < x < \frac{\pi}{2}$

$$\cot x = 2 \Rightarrow \cos 2x = ?$$

Cevap:  $+\frac{3}{5}$

23.  $0 < x < \frac{\pi}{2}$

$$\cot x = \frac{1}{2} \Rightarrow \tan 2x = ?$$

Cevap:  $-\frac{4}{3}$

24.  $0 < x < \frac{\pi}{2}$

$$\sin x = \frac{3}{4} \Rightarrow \cos 2x = ?$$

Cevap:  $-\frac{1}{8}$

25.  $0 < x < \frac{\pi}{2}$

$$\sin x = \frac{4}{5} \Rightarrow \cot 2x = ?$$

Cevap:  $-\frac{7}{24}$

26.  $\frac{\pi}{2} < x < \pi$

$$\sin x = \frac{1}{3} \Rightarrow \cos 2x = ?$$

Cevap:  $\frac{7}{9}$

27.  $\frac{\pi}{2} < x < \pi$

$$\sin x = \frac{2}{3} \Rightarrow \sin 2x = ?$$

Cevap:  $-\frac{4\sqrt{5}}{9}$

28.  $\frac{\pi}{2} < x < \pi$

$$\cos x = -\frac{1}{4} \Rightarrow \cos 2x = ?$$

Cevap:  $-\frac{7}{8}$

**29.**  $\frac{\pi}{2} < x < \pi$

$$\tan x = -\frac{3}{4} \Rightarrow \tan 2x = ?$$

Cevap:  $-\frac{24}{7}$

**30.**  $\pi < x < \frac{3\pi}{2}$

$$\cos x = -\frac{5}{13} \Rightarrow \sin 2x = ?$$

Cevap:  $\frac{120}{169}$

**31.**  $\frac{3\pi}{2} < x < 2\pi$

- $\sin x = -\frac{4}{5}$
- a)  $\cos 2x = ?$
  - b)  $\tan 2x = ?$
  - c)  $\sin 2x = ?$
  - d)  $\cot 2x = ?$

Cevap: a)  $-\frac{7}{25}$

b)  $\frac{24}{7}$

c)  $-\frac{24}{25}$

d)  $\frac{7}{24}$

**32.**  $0 < x < \frac{\pi}{2}$

$$\sin 2x = \frac{4}{5} \Rightarrow \sin x = ?$$

Cevap:  $\frac{1}{\sqrt{5}}$

**33.**  $0 < x < \frac{\pi}{2}$

$$\tan 2x = 2 \Rightarrow \tan x = ?$$

Cevap:  $\frac{2}{\sqrt{5}+1}$

**34.**  $\frac{\pi}{2} < x < \pi$

$$\sin 2x = -\frac{5}{13} \Rightarrow \tan x = ?$$

Cevap:  $-\frac{1}{5}$

**35.**  $\frac{\pi}{2} < x < \pi$

$$\cos 2x = \frac{4}{5} \Rightarrow \cot x = ?$$

Cevap: -3

**36.**  $\pi < x < \frac{3\pi}{2}$

$$\tan 2x = 2 \Rightarrow \cot x = ?$$

Cevap:  $\frac{\sqrt{5}+1}{2}$

**37.**  $\frac{3\pi}{2} < x < 2\pi$

$$\cos 2x = -\frac{4}{5} \Rightarrow \cos x = ?$$

Cevap:  $\frac{3}{\sqrt{10}}$

38.  $\sin x + \cos x = \frac{1}{2} \Rightarrow \sin 2x = ?$

Cevap:  $-\frac{3}{4}$

39.  $\sin x - \cos x = \frac{1}{5} \Rightarrow \sin 2x = ?$

Cevap:  $\frac{24}{25}$

40.  $\sin x + \cos x = -\frac{2}{3} \Rightarrow \sin 2x = ?$

Cevap:  $-\frac{5}{9}$

41.  $\sin x - \cos x = -\frac{4}{5} \Rightarrow \sin 2x = ?$

Cevap:  $\frac{9}{25}$

42.  $\frac{3\pi}{2} < 2x < 2\pi$

$\sin x + \cos x = -\frac{1}{3} \Rightarrow \cos 2x = ?$

Cevap:  $\frac{\sqrt{17}}{9}$

43.  $0 < x < \frac{\pi}{2}$

$\sin x - \cos x = \frac{1}{5} \Rightarrow \tan 2x = ?$

Cevap:  $-\frac{24}{7}$

44.  $\sin x + \cos x = \frac{1}{4} \Rightarrow \sin 2x = ?$

Cevap:  $-\frac{15}{16}$

45.  $\cos 12 = m \Rightarrow \cos 24 = ?$

Cevap:  $2m^2 - 1$

46.  $\sin 16 = p \Rightarrow \sin 58 = ?$

Cevap:  $1 - 2p^2$

47.  $\tan 17 = k \Rightarrow \tan 34 = ?$

Cevap:  $\frac{2k}{1-k^2}$

48.  $\sin 32^\circ = t \Rightarrow \cos 26^\circ = ?$

Cevap:  $2t\sqrt{1-t^2}$

49.  $\cot 12^\circ = y \Rightarrow \tan 24^\circ = ?$

Cevap:  $\frac{2y}{y^2-1}$

50.  $\sin 14^\circ = b \Rightarrow \cos 28^\circ = ?$

Cevap:  $1-2b^2$

51.  $\frac{1}{\sin 15^\circ} + \frac{1}{\cos 15^\circ} = ?$

Cevap:  $2\sqrt{6}$

52.  $\frac{1}{\sin 15^\circ} - \frac{1}{\cos 15^\circ} = ?$

Cevap:  $2\sqrt{2}$

53.  $\frac{\cos 2x}{\cos x + \sin x} = ?$

Cevap:  $\cos x - \sin x$

54.  $\frac{\cos x - \sin x}{1 - \sin 2x} = ?$

Cevap:  $\frac{1}{\cos x - \sin x}$

55.  $\frac{\sin^3 x - \cos^3 x}{\sin x - \cos x} = \frac{1}{2} \Rightarrow \sin 2x = ?$

Cevap: -1

56.  $\frac{2\cos^2 15^\circ - 1}{\sin 15^\circ \cos 15^\circ} = ?$

Cevap:  $2\sqrt{3}$

57.  $\cos^2 x = \frac{1}{4} \Rightarrow \cos 2x = ?$

Cevap:  $-\frac{1}{2}$

58.  $\frac{1}{\cos x} - \frac{\sin 3x}{\cos 3x \cdot \sin x} = ?$

Cevap:  $-2\sec 3x$

59.  $\frac{1 - \cos 2x}{\sin x} = ?$

Cevap:  $2\sin x$

60.  $\frac{1 + \cos 2x}{\cos x} = ?$

Cevap:  $2\cos x$

61.  $\frac{1 + \cos 2x}{\sin 2x} = ?$

Cevap:  $\cot x$

62.  $\frac{1 - \cos 2x}{\sin 2x} = ?$

Cevap:  $\tan x$

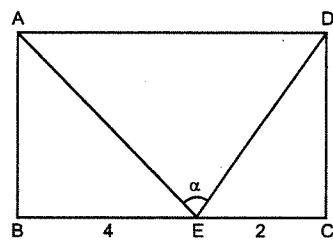
63.  $\frac{1 - \cos 2x}{2} = ?$

Cevap:  $\sin^2 x$

64.  $\frac{1 + \cos 2x}{2} = ?$

Cevap:  $\cos^2 x$

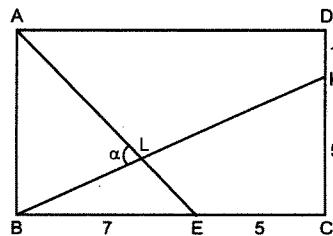
65.



ABCD  
dikdörtgen  
 $\tan \alpha = ?$

Cevap: 18

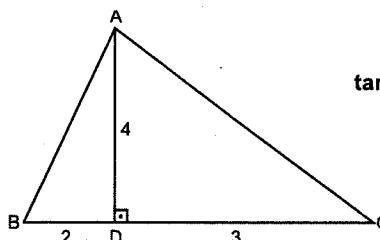
66.



ABCD  
dikdörtgen  
 $\tan \alpha = ?$

Cevap:  $\frac{107}{54}$

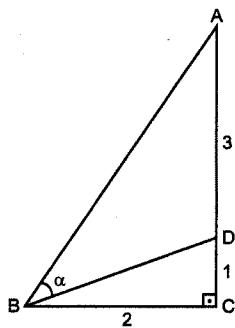
67.



$\tan(\widehat{BAC}) = ?$

Cevap: 2

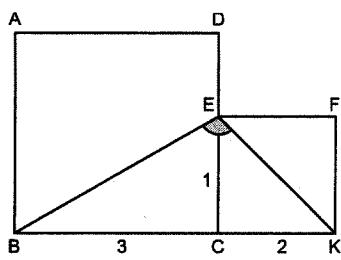
68.



$$\tan \alpha = ?$$

Cevap:  $\frac{3}{4}$

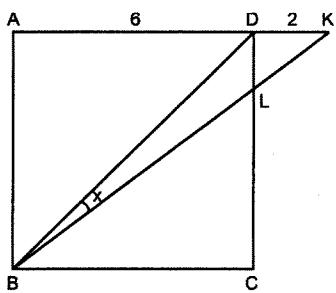
69.



ABCD kare  
ECKF  
dikdörtgen  
 $\tan(\widehat{BEK}) = ?$

Cevap: -1

70.

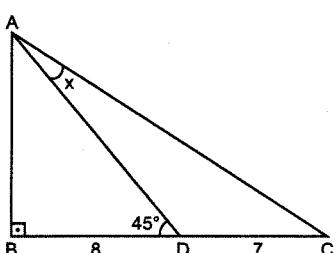


ABCD kare

$$\tan x = ?$$

Cevap:  $\frac{1}{7}$

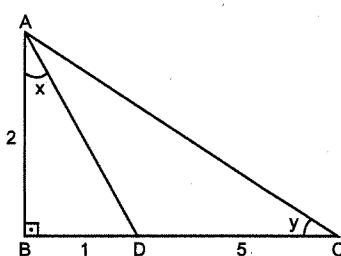
71.



$$\tan x = ?$$

Cevap:  $\frac{7}{23}$

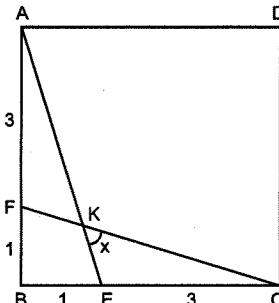
72.



$$y+x = ?$$

Cevap: 45°

73.

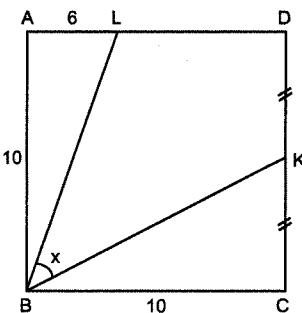


ABCD Kare

$$\tan x = ?$$

Cevap:  $\frac{15}{8}$

74.

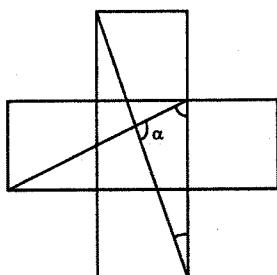


ABCD kare

$$\tan x = ?$$

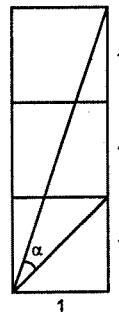
Cevap:  $\frac{7}{11}$

75.



Birim karelardan  
oluşan şekilde  
 $\tan\alpha = ?$

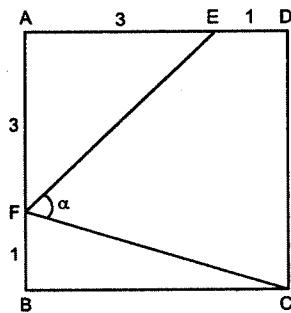
78.

 $\cot\alpha = ?$ 

Cevap: -7

Cevap: 2

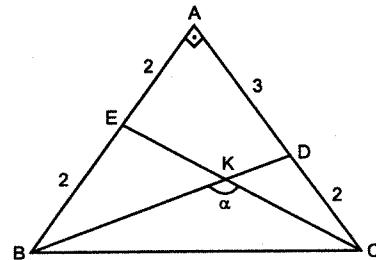
76.



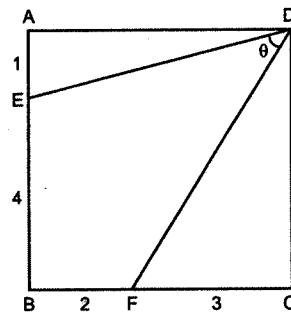
ABCD Kare

 $\tan\alpha = ?$ 

79.

 $\cot\alpha = ?$ Cevap:  $-\frac{23}{14}$ Cevap:  $\frac{5}{3}$ 

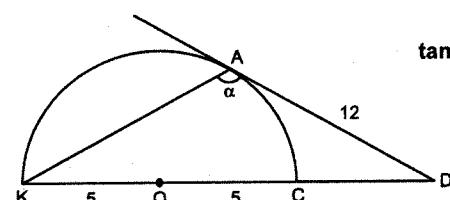
77.



ABCD kare

 $\tan\theta = ?$ 

80.

 $\tan\alpha = ?$ Cevap:  $\frac{11}{10}$ Cevap:  $-\frac{3}{2}$

**Ters Trigonometrik Fonksiyonlar**

$$\begin{aligned}\arcsin x = y &\Rightarrow \sin y = x \\ \arccos y = x &\Rightarrow \cos x = y \\ \arctan y = x &\Rightarrow \tan x = y \\ \operatorname{arccot} y = x &\Rightarrow \cot x = y\end{aligned}$$

**Örnek:**  $\arcsin \frac{1}{2} = x \Rightarrow x \in \left[0, \frac{\pi}{2}\right]$   
 $x = ?$

**Cevap:**  $x = \frac{\pi}{6}$

**Örnek:**  $\arcsin \frac{\sqrt{3}}{2} = x \Rightarrow x \in [0, \pi]$   
 $x = ?$

**Cevap:**  $x_1 = 60^\circ, 120^\circ$

**Örnek:**  $\arccos -\frac{1}{2} = x \Rightarrow x \in [0, 2\pi]$   
 $x = ?$

**Cevap:**  $x_1 = 120^\circ$   
 $x_2 = 240^\circ$

**Örnek:**  $x = \arctan \sqrt{3} \Rightarrow x \in \left[\pi, \frac{3\pi}{2}\right]$   
 $x = ?$

**Cevap:**  $240^\circ = x$

**Örnek:**  $\arctan -1 = x \Rightarrow x \in [\pi, 2\pi]$   
 $x = ?$

**Cevap:**  $315^\circ = x$

**Örnek:**  $\operatorname{arccot} \frac{1}{\sqrt{3}} = x \Rightarrow x \in \left[0, \frac{\pi}{2}\right]$

**Cevap:**  $x = 60^\circ$

**Örnek:**  $\sin\left(\arccos \frac{2}{3}\right) + \cos\left(\arcsin \frac{1}{4}\right) = ?$

**Cevap:**  $\frac{4\sqrt{5} + 3\sqrt{15}}{12}$

**Örnek:**  $\sin\left[\arccos \frac{3}{5} + \arctan 2\right] = ?$

**Cevap:**  $\frac{2}{\sqrt{5}}$

**Örnek:**  $\sin(2\arctan 2) = ?$

**Cevap:**  $\frac{4}{5}$

Örnek:  $\alpha = \arctan \frac{1}{3} + \arctan 2$        $\tan \alpha = ?$

Cevap: 7

Örnek:  $\arcsin \frac{3}{5} + \arcsin \frac{4}{5} = ?$

Cevap:  $\frac{\pi}{2}$

Örnek:  $\arccos\left(\frac{1}{4}\right) + \arccos\left(-\frac{1}{4}\right) = ?$

Cevap:  $\pi$

Örnek:  $\arctan 3 + \arctan 2 = ?$

Cevap:  $135^\circ$

Örnek:  $\cos\left(\arctan \frac{3}{4}\right) = ?$

Cevap:  $\frac{4}{5}$

Örnek:  $\sin\left(2 \arcsin \frac{1}{3}\right) = ?$

Cevap:  $\frac{4\sqrt{2}}{9}$

Örnek:  $\tan\left(\arcsin \frac{\sqrt{3}}{2}\right) = ?$

Cevap:  $\sqrt{3}$

Örnek:  $\sin\left(\arccos \frac{1}{3}\right) = ?$

Cevap:  $\frac{2\sqrt{2}}{3}$

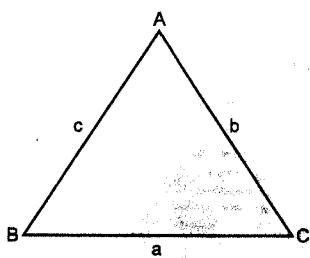
Örnek:  $\arcsin\left(\sin \frac{3\pi}{5}\right) = ?$

Cevap:  $\frac{3\pi}{5}$

Örnek:  $\tan\left(\arcsin \frac{3}{5} + \arccos \frac{5}{13}\right) = ?$

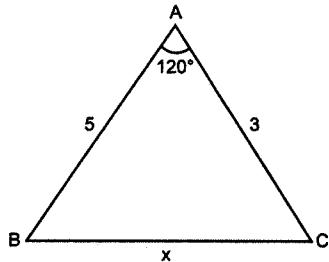
Cevap:  $-\frac{63}{16}$

## Cosinüs Teoremi



$$a^2 = b^2 + c^2 - 2bc \cdot \cos A$$

Örnek:



$$x^2 = 5^2 + 3^2 - 2 \cdot 5 \cdot 3 \cdot \cos 120^\circ$$

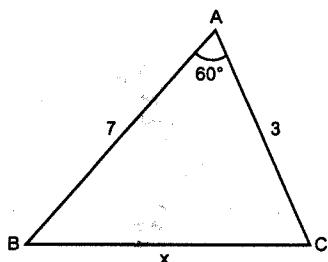
$$x^2 = 25 + 9 + 30 \cdot \left(-\frac{1}{2}\right)$$

$$x^2 = 34 + 15$$

$$x^2 = 49$$

$$x = 7$$

Örnek:

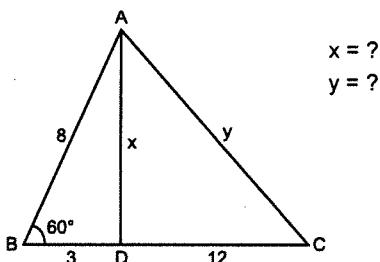


$$x^2 = 7^2 + 3^2 - 2 \cdot 7 \cdot 3 \cdot \cos 60^\circ$$

$$x^2 = 49 + 9 - 42 \cdot \frac{1}{2}$$

$$x^2 = 58 - 21 = 37 \Rightarrow x = \sqrt{37}$$

Örnek:



$$x^2 = 8^2 + 3^2 - 2 \cdot 8 \cdot 3 \cdot \cos 60^\circ$$

$$x^2 = 64 + 9 - 48 \cdot \frac{1}{2}$$

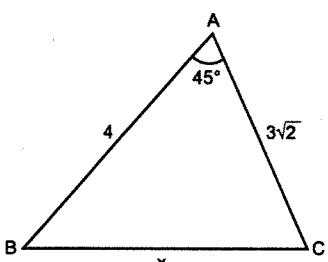
$$x^2 = 73 - 24 = 49$$

$$x = 7$$

$$y^2 = 8^2 + 15^2 - 2 \cdot 8 \cdot 15 \cdot \cos 60^\circ$$

$$y = 13$$

Örnek:



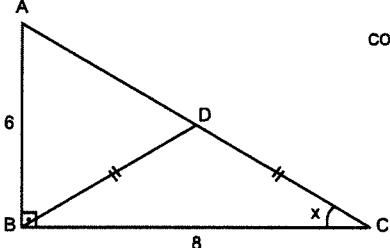
$$x^2 = 16 + 18 - 2 \cdot 4 \cdot 3\sqrt{2} \cdot \cos 45^\circ$$

$$x^2 = 34 - 24\sqrt{2} \cdot \frac{\sqrt{2}}{2}$$

$$x^2 = 34 - 24$$

$$x = \sqrt{10}$$

Örnek:



$$\cos 2x = ?$$

$$\text{Cevap: } \frac{7}{25}$$

Örnek:

$$\cos x = ?$$

Cevap:  $\frac{\sqrt{20}}{5}$

Örnek:

$$\cos x = ?$$

Cevap:  $\frac{\sqrt{53}}{2}$

Örnek:

$$\cos x = ?$$

Cevap:  $\frac{\sqrt{317}}{2}$

Örnek:

$$\cos x = ?$$

Cevap:  $\frac{\sqrt{117}}{5}$

Örnek:

$$\cos x = ?$$

Örnek:

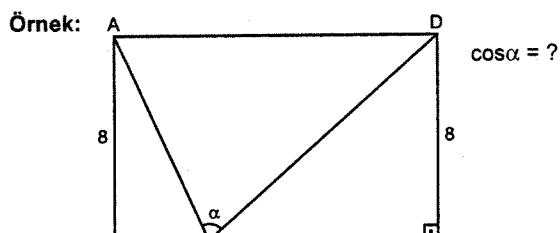
$$\cos \alpha = ?$$

Örnek:

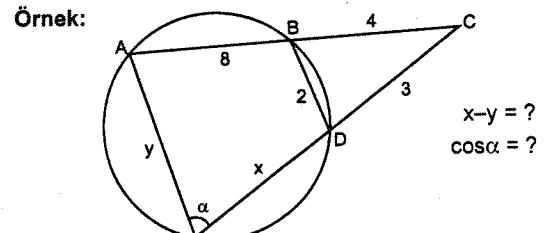
$$\cos x = ?$$

Örnek:

$$\cos \alpha = ?$$

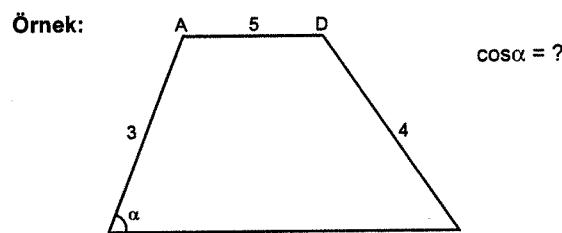


Cevap:  $-\frac{13}{85}$

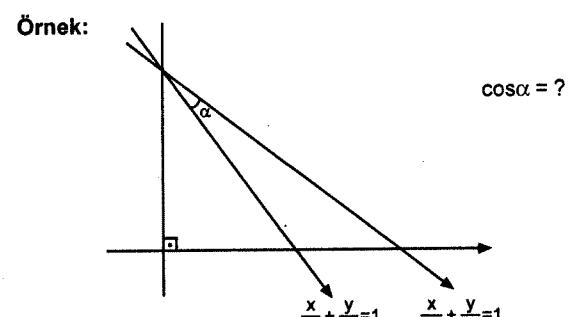


Cevap:  $x-y = 5$

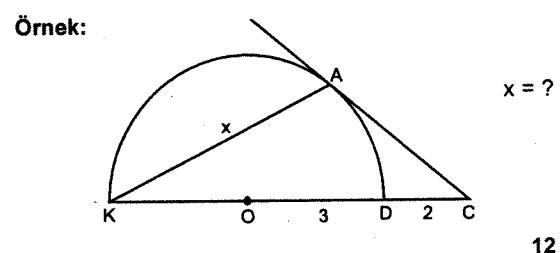
$\cos \alpha = \frac{11}{16}$



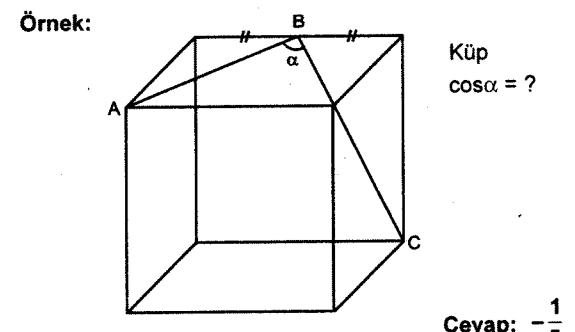
Cevap:  $\frac{3}{8}$



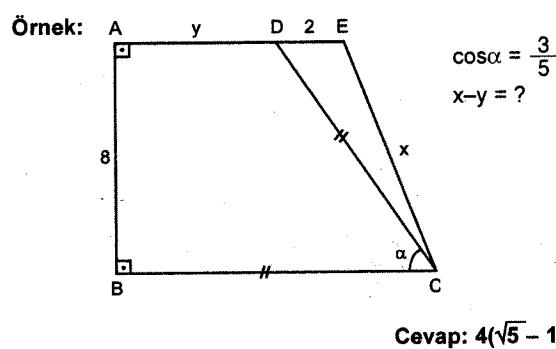
Cevap:  $\frac{77}{85}$



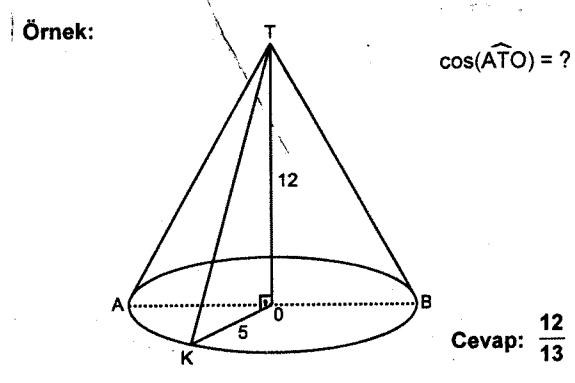
Cevap:  $\frac{12}{\sqrt{5}}$



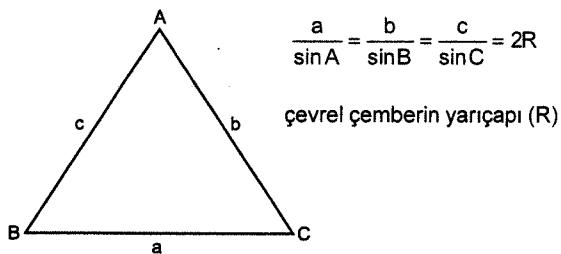
Cevap:  $-\frac{1}{5}$



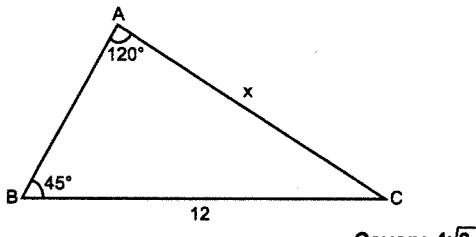
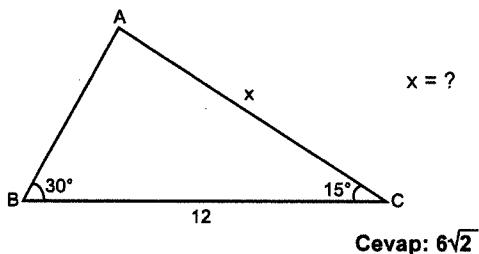
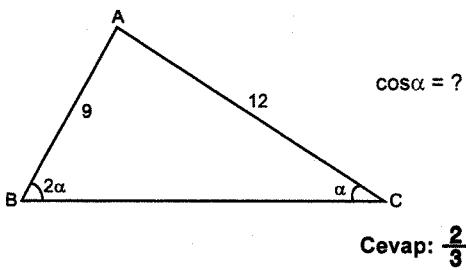
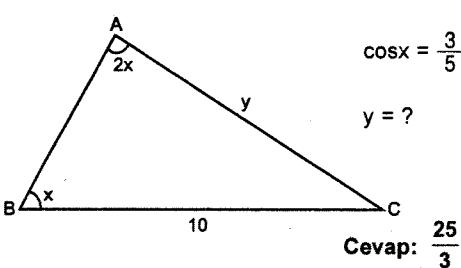
Cevap:  $4(\sqrt{5} - 1)$



Cevap:  $\frac{12}{13}$

**Sinüs Teoremi**

$$\text{Alan}(\widehat{\triangle ABC}) = \frac{a \cdot b \cdot c}{4R}$$

**Örnek:****Örnek:****Örnek:****Örnek:****Esas Periyot:**

$$\begin{cases} \frac{2\pi}{|a|}, & n \text{ tek ise} \\ \frac{\pi}{|a|}, & n \in \mathbb{Z} \\ \end{cases}$$

$$\begin{cases} \frac{\pi}{|a|}, & n \in \mathbb{Z} \\ \end{cases}$$

**Örnek:** Aşağıdaki fonksiyonların esas periyotlarını bulunuz.

$\sin(2x-1) =$

$\sin^2(3x+6) =$

$\cos(2x+6) =$

$\cos^6(12x-5) =$

$\tan^7(3x-5) = ?$

$\cot^6(5x-5) =$

$\sin^3(3x-2) + \cos^2(3x+1) = ?$

$\sin^4(5x-5) + \tan^3(3x-1)$

$\text{ökek}\left(\frac{\pi}{5}, \frac{\pi}{3}\right) = 360^\circ$

$\cot(5x-5) + \cot^7(6x+6) = ?$

$\text{ökek}\left(\frac{\pi}{5}, \frac{\pi}{6}\right) = 180^\circ$

$\sin^3x + \cos^2(2x-1) + \tan(5x-5) = ?$

$\text{ökek}\left(2\pi, \frac{\pi}{2}, \frac{\pi}{5}\right) = 360^\circ$

**Dönüşüm Formülleri**

$\sin x + \sin y = 2 \sin \frac{x+y}{2} \cdot \cos \frac{x-y}{2}$

$\sin x - \sin y = 2 \cos \frac{x+y}{2} \cdot \sin \frac{x-y}{2}$

$\cos x + \cos y = 2 \cos \frac{x+y}{2} \cdot \cos \frac{x-y}{2}$

$\cos x - \cos y = -2 \sin \frac{x+y}{2} \cdot \sin \frac{x-y}{2}$

**Not:** Baştaki terim ile sondaki terimin toplamının yarısı ortadaki terimi veriyorsa ortadaki terimlerin birbirine oranı sonucu verir.

$$\text{Örnek: } \frac{\cos 20 + \cos 40}{\sin 20 + \sin 40} = ?$$

**Cevap:**  $\sqrt{3}$

$$\text{Örnek: } \frac{\cos 2x + \cos 6x + \cos 10x}{\sin 2x + \sin 6x + \sin 10x} = \frac{\cos 6x}{\sin 6x} = \cot 6x$$

gibi

$$\frac{\cos 6x + \cos 2x}{\cos 4x}$$

Pay için dönüşüm formülü uygula sonra  $2x$  yerine  $45^\circ$  yaz.

**Cevap:**  $\sqrt{2}$

$$\text{Örnek: } \cos 40 + \cos 80 = ?$$

**Cevap:**  $\cos 20$

$$\text{Örnek: } 7x = \frac{\pi}{2}$$

$$\frac{\cos 6x + \cos 8x}{\sin 8x + \sin 6x}$$

2 dönüşüm formülü uygula.

**Cevap:** 0

$$\text{Örnek: } \frac{\sin 64 + \sin 26}{2} = ?$$

**Cevap:**  $\frac{\sqrt{2}}{2} \cos 19$

$$\text{Örnek: } \frac{\cos 80 + \cos 20}{\cos 70 - \cos 10}$$

2 dönüşüm formülü uygula.

**Cevap:**  $-\sqrt{3}$

Örnek:  $a+b = \frac{\pi}{2}$

$$\frac{\sin a - \cos b}{\sin a + \cos b} = ?$$

Birbirini  $90^\circ$  ye tamamlayan açıların kuralını aklına getir.

Cevap: 0

Örnek:  $\frac{\cos 7x + \cos 8x + \cos 9x}{\sin 7x - \sin 8x + \sin 9x} = ?$

Not'a bak.

Cevap:  $-\cot 8x$

Örnek:  $\cos 10 \cdot \cos 20 \cdot \cos 40 \cdot \cos 80 = ?$

Çözüm: Pay ve paydayı  $2\sin 10$  ile çarp, böl.

$$\frac{2\sin 10 \cdot \cos 10 \dots}{2\sin 10} = \frac{\sin 20 \cos 20 \dots}{2\sin 10} =$$

2 ile çarp, böl

Cevap:  $\frac{\cos 10}{8}$

Örnek:  $\frac{1}{\cos 10} + \frac{\sqrt{3}}{\sin 10} = ?$

Çözüm:  $\sqrt{3} = \tan 60$  dönüşümü yap, paydayı eşitle işlem hatası yapma.

Cevap:  $4\cot 20$

Örnek:  $\sin 20 + \sin 40 + \sin 80 = ?$

Çözüm:  $\sin 20 + \sin 40$  için dönüşüm formülü uygula.

Cevap:  $2\cos 10$

Örnek:  $\sin 75 + \sqrt{3} \cdot \cos 75 = ?$

Çözüm:  $\sqrt{3} = \tan 60$  dönüşümü yap paydayı eşitle.

Cevap:  $\sqrt{2}$

### BÖLÜM III – TRİGONOMETRİK DENKLEMLER

$$\sin x = \sin \alpha \Rightarrow x_1 = \alpha + 2k\pi \quad k \in \mathbb{Z}$$

$$x_2 = (180 - \alpha) + 2\pi k$$

$$\cos x = \cos \alpha \Rightarrow x_1 = \alpha + 2k\pi \quad k \in \mathbb{Z}$$

$$x_2 = -\alpha + 2k\pi$$

$$\tan x = \tan \alpha \Rightarrow x = \alpha + k\pi \quad k \in \mathbb{Z}$$

$$\cot x = \cot \alpha$$

**Örnek:**  $x \in [0, 2\pi]$

$$\sin 2x = \frac{1}{2} \Rightarrow 2x = 30^\circ + 2k\pi \Rightarrow x_1 = 15 + k\pi$$

$$2x = (180 - 30) + 2k\pi \Rightarrow x_2 = 75 + k\pi$$

$$\text{Ç.K.} = \left\{ x_1 = 15, x_2 = 75, x_1 = 195, x_2 = 255 \right\}$$

**Örnek:**  $\cos x = -\frac{1}{2} \Rightarrow x \in [0, 2\pi]$

$$\begin{aligned} \text{Çözüm: } x_1 &= 120^\circ + 2k\pi \\ x_2 &= 240^\circ + 2k\pi \\ x_1 &= -120^\circ + 2k\pi \end{aligned}$$

$$\text{Ç.K.} = \left\{ 120, 240 \Rightarrow \text{Ç.K.} = 120, 240 \right\}$$

**Örnek:**  $\sin 3x = \cos 2x \Rightarrow x \in [0, 2\pi] \quad \text{Ç.K.} = ?$

**Çözüm:**  $\sin 3x = \sin(90 - 2x)$

$$\begin{aligned} 3x &= 90 - 2x + 2k\pi & 3x &= 180 - [90 - 2x] + 2k\pi \\ 5x &= 90 + 2k\pi & 3x &= 90 + 2x - 2k\pi \\ x_1 &= 18^\circ + \frac{2k\pi}{5} & x_2 &= 90 + 2k\pi \end{aligned}$$

$$\text{Ç.K.} = \left\{ \begin{array}{l} x_1, x_2 \\ \hline k=0 & 18^\circ, 90^\circ \\ k=1 & 90^\circ, 90^\circ \\ k=2 & 162^\circ, 90^\circ \\ k=3 & 234^\circ, 90^\circ \\ k=4 & 306^\circ, 90^\circ \end{array} \right.$$

$$\text{Ç.K.} = \{18^\circ, 90^\circ, 162^\circ, 243^\circ, 306^\circ\}$$

$$\text{Örnek: } \tan 3x = \cot 5x \Rightarrow x \in \left[ 0, \frac{\pi}{2} \right] \quad \text{Ç.K.} = ?$$

$$\begin{aligned} \tan 3x &= \tan(90 - 5x) \\ 3x &= 90 - 5x + k\pi \end{aligned}$$

$$8x = 90 + k\pi \Rightarrow x = \frac{90}{8} + \frac{k\pi}{8} \quad k \in \mathbb{Z}$$

$$\text{Ç.K.} = \left\{ \frac{90}{8}, \frac{90+180}{8}, \frac{90+360}{8}, \frac{90+540}{8}, \dots \right\}$$

$$\text{Ç.K.} = \left\{ \frac{90}{8}, \frac{135}{4}, \frac{300}{4}, \frac{225}{4}, \frac{375}{4}, \frac{450}{4}, \dots \right\}$$

$$\left[ 0, \frac{\pi}{2} \right] \text{ aralığında } \text{Ç.K.} = \left\{ \frac{90}{8}, \frac{135}{4}, \frac{225}{4}, \frac{300}{4} \right\}$$

**Örnek:**  $\tan x \cdot \tan 3x = 1 \quad \left[ 0, \frac{\pi}{2} \right] \text{ aralığında kökler toplamı?}$

**Çözüm:**

$$\begin{aligned} \tan x &= \frac{1}{\tan 3x} \Rightarrow \tan x = \cot 3x \Rightarrow \tan x = \tan(90 - 3x) \\ \Rightarrow x &= 90 - 3x + k\pi \quad 4x = 90 + k\pi \Rightarrow x = \frac{90}{4} + \frac{k\pi}{4} \end{aligned}$$

**Örnek:**

$$1 - \sin^2 x + 2 \sin x \cos x = 0 \quad x \in [0, 2\pi] \rightarrow \text{Ç.K.} = ?$$

**Çözüm:**

$$\begin{aligned} 1 - 2 \sin^2 x &= \cos 2x \\ 2 \sin x \cos x &= \sin 2x \end{aligned} \Rightarrow \cos 2x + \sin 2x = 0$$

$$\begin{aligned} -\tan 2x &= 1 \\ \tan 2x &= -1 \end{aligned}$$

$$2x = 135 + k\pi$$

$$x = \frac{135}{2} + \frac{k\pi}{2} \Rightarrow \text{Ç.K.} = \left\{ \frac{135}{2}, \frac{315}{2}, \frac{495}{2}, \frac{675}{2} \right\}$$

**Örnek:**  $2\sin^2 2x + 3\sin 2x - 2 = 0 \Rightarrow x \in [0, \pi]$  aralığında kökler toplamı?

**Cözüm:**

$$2\sin^2 2x + 3\sin 2x - 2 = 0 \quad (2\sin 2x - 1)(\sin 2x + 2) = 0$$

$$\begin{array}{lll} 2\sin 2x & -1 & \sin 2x = \frac{1}{2} \quad \sin 2x = -2 \\ \sin 2x & +2 & \end{array}$$

$$\sin 2x = \frac{1}{2} \Rightarrow 2x = 30 + 2k\pi \Rightarrow x_1 = 15 + k\pi$$

$$2x = (180 - 30) + 2k\pi \quad x_2 = 75 + k\pi$$

$$\text{Toplam } \rightarrow \frac{x_1}{15} + \frac{x_2}{75} = 90$$

**Not:**  $a \cos x + b \sin x$  ifadesinin

en büyük değeri  $\sqrt{a^2 + b^2}$

en küçük değeri  $-\sqrt{a^2 + b^2}$

**Örnek:**  $3\sin x - 4\cos x$  in en büyük değeri kaçtır?

$$\sqrt{3^2 + (-4)^2} = 5 \text{ tir.}$$

**Örnek:**  $7\sin x + 24\cos x$  in en küçük değeri kaçtır?

$$-\sqrt{7^2 + 24^2} = -25 \text{ tir.}$$

**Örnek:**  $\cos x + \sqrt{3} \sin x = \sqrt{3} \Rightarrow x$  dar açısı kaç derecedir?

$$\sqrt{3} = \tan 60$$

$$\cos x + \frac{\sin 60}{\cos 60} \sin x = \sqrt{3}$$

$$\frac{\cos x \cos 60 + \sin 60 \sin x}{\cos 60} = \sqrt{3} \Rightarrow \frac{\cos(x-60)}{\frac{1}{2}} = \sqrt{3}$$

$$\Rightarrow \cos(x-60) = \frac{\sqrt{3}}{2}$$

$$x-60 = 30 + 2k\pi \Rightarrow x_1 = 90 + 2k\pi$$

$$x-60 = -30 + 2k\pi \Rightarrow x_2 = 30 + 2k\pi$$

$$\Rightarrow x = 30^\circ \text{ olur.}$$

### Karışık Örnekler

$$1. \quad \frac{1}{1-\sin x} + \frac{1}{1+\sin x} = \frac{8}{3}$$

denklemini sağlayan  $x$  dar açısı kaç derecedir?

**Cözüm:** payda eşitlenir.

$$\frac{1+\sin x+1-\sin x}{(1+\sin x)(1-\sin x)} = \frac{8}{3} \Rightarrow \frac{2}{1-\sin^2 x} = \frac{8}{3}$$

$$\Rightarrow \cos^2 x = \frac{3}{4}$$

$$\cos x = \pm \frac{\sqrt{3}}{2} \Rightarrow$$

$$\cos x = \frac{\sqrt{3}}{2} \Rightarrow x = 30^\circ$$

$$2. \quad \pi < x < 2\pi$$

$\cos 2x + \sin x = 0$  denklemini sağlayan kaç olabilir?

**Cözüm:**  $\cos 2x$  in açılımının  $\sin x$  cinsinden yazmamızı.

$$1 - 2\sin^2 x + \sin x = 0 \Rightarrow 2\sin^2 x - \sin x - 1 = 0$$

$$\begin{array}{ll} 2\sin x & +1 \\ \sin x & -1 \end{array}$$

$$(2\sin x + 1)(\sin x - 1) = 0 \Rightarrow \sin x = -\frac{1}{2} \text{ veya } \sin x = 1$$

$$x = 210, 330, \quad x = 90^\circ \text{ olabilir.}$$

$$3. \quad 2\sin x + \sin 2x = 0 \Rightarrow x \in [0, 2\pi] \text{ aralığında kaç kök vardır?}$$

**Cözüm:**  $2\sin x + 2\sin x \cos x = 0$

$$2\sin x[1 + \cos x] = 0 \Rightarrow \sin x = 0 \rightarrow x_1 = 0, 180, 360^\circ$$

$$1 + \cos x = 2 \Rightarrow \cos x = -1$$

$$x_2 = 180^\circ$$

$$\Rightarrow \text{Ç.K} = \{0, 180, 360\} \text{ 3 tane}$$

4.  $\frac{\cos^2 x}{1 + \sin x} = \frac{1}{2} \Rightarrow x$  dar açısı kaç derece olabilir?

**Çözüm:**

$$2\cos^2 x = 1 + \sin x$$

$$2\cos^2 x - 1 = \sin x$$

$$\cos 2x = \sin x \Rightarrow \sin x = \sin(90 - 2x)$$

$$x = 90 - 2x + 2k\pi \Rightarrow 3x = 90 + 2k\pi$$

$$x = 180 - [90 - 2x] + 2k\pi$$

$$x = 30 + \frac{2k\pi}{3}$$

$$-x = 90 + 2k\pi$$

$$x = -90 - 2k\pi \text{ ise}$$

$x = 30^\circ$  olabilir.

5.  $1 + \cos x = \sin x + \tan x \Rightarrow x \in [0, \pi]$  de kaç kökü vardır?

**Çözüm:**

$$1 + \cos x = \sin x + \frac{\sin x}{\cos x}$$

$$1 + \cos x = \frac{\sin x \cos x + \sin x}{\cos x} \Rightarrow$$

$$\cos x + \cos^2 x = \sin x [\cos x + 1]$$

$$\cos x [1 + \cos x] = \sin x [\cos x + 1]$$

sadeleştirme yapılmaz.

$$\Rightarrow \cos x [1 + \cos x] - \sin x [\cos x + 1] = 0$$

$$[1 + \cos x][\cos x - \sin x] = 0 \Rightarrow \cos x = -1 \text{ ve } \cos x = \sin x$$

$$x = 180^\circ \quad \tan x = 1$$

$$x = 45^\circ$$

2 kökü vardır.

6.  $2\sin^2 x - 3\cos x = 3 \Rightarrow$  ve  $[0, 2\pi]$  aralığındaki kökleri bulun?

**Çözüm:**

$$2(1 - \cos^2 x) - 3\cos x - 3 = 0$$

$$2 - 2\cos^2 x - 3\cos x - 3 = 0$$

$$2\cos^2 x + 3\cos x + 1 = 0 \quad (2\cos x + 1)(\cos x + 1) = 0$$

$$\begin{array}{lll} 2\cos x & +1 & \cos x = -1/2 \quad \cos x = -1 \\ \cos x & +1 & \end{array}$$

$$\mathcal{C}\mathcal{K} = \{120, 180, 240\}$$

7.  $\frac{1}{\sin x} - \frac{1}{\cos x} = 1 \Rightarrow x$  in çözüm kümelerini bulunuz?

**Çözüm:**

$$\frac{1}{\sin x} - \frac{1}{\cos x} = 1 \quad \frac{\cos x - \sin x}{\sin x \cos x} = 1$$

$$\cos x - \sin x = \sin x \cos x$$

(Her iki tarafın karesini alalım.)

$$\cos^2 x - 2\sin x \cos x + \sin^2 x = \sin^2 x \cos^2 x$$

$$1 - \sin 2x = \frac{\sin^2 2x}{4} \Rightarrow \sin^2 2x - 4\sin 2x + 4 = 0$$

$$(\sin 2x - 2)^2 = 0$$

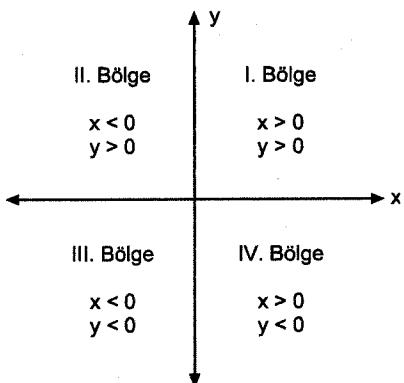
$$\sin 2x = 2$$

$$\mathcal{C}\mathcal{K} = \{ \} \text{ dir.}$$

# ANALİTİK GEOMETRİ

## Noktanın Analitik İncelenmesi

1.

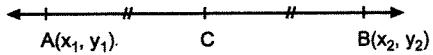


## 2. İki Nokta Arasındaki Uzaklık:

$$A(x_1, y_1) \quad B(x_2, y_2)$$

$$|AB| = \sqrt{(x_1 - x_2)^2 + (y_1 - y_2)^2}$$

## 3. Orta Nokta:

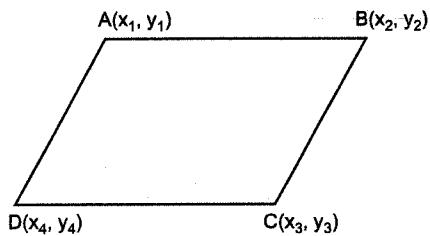


$$C\left(\frac{x_1 + x_2}{2}, \frac{y_1 + y_2}{2}\right)$$

## 4. A(x<sub>1</sub>, y<sub>1</sub>), B(x<sub>2</sub>, y<sub>2</sub>), C(x<sub>3</sub>, y<sub>3</sub>) köşeleri A, B, C olan bir üçgenin ağırlık merkezinin koordinatları

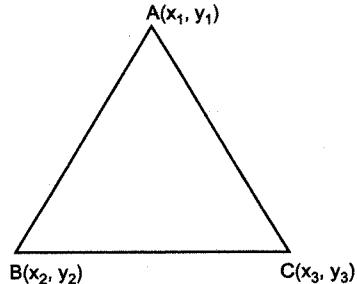
$$G\left(\frac{x_1 + x_2 + x_3}{3}, \frac{y_1 + y_2 + y_3}{3}\right)$$

## 5. Paralelkenar



$$\boxed{x_1 + x_3 = x_2 + x_4 \\ y_1 + y_3 = y_2 + y_4}$$

6.



$$\text{Alan}(\Delta ABC) = \frac{1}{2} \begin{vmatrix} x_1 & y_1 \\ x_2 & y_2 \\ x_3 & y_3 \\ x_1 & y_1 \end{vmatrix} = \dots$$

(Bu açılımı hocana sor.)

**Eğim:** Bir doğrunun Ox eksenile pozitif yönde yaptığı açının tanjantıdır.

## a) İki noktası bilinen doğrunun eğimi:

$$A(x_1, y_1), B(x_2, y_2)$$

$$\boxed{m_{AB} = \frac{y_2 - y_1}{x_2 - x_1}}$$

- b) Eğimi ve bir noktası bilinen doğrunun denklemi:

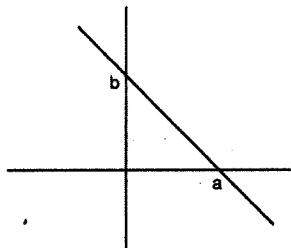
$$y - y_1 = m(x - x_1)$$

- c) İki noktası bilinen doğrunun denklemi:

$A(X_1, Y_1), B(X_2, Y_2)$

$$\frac{y_2 - y_1}{x_2 - x_1} = \frac{y - y_1}{x - x_1}$$

- d) Eksenleri kestiği noktaları bilinen doğrunun denklemi:

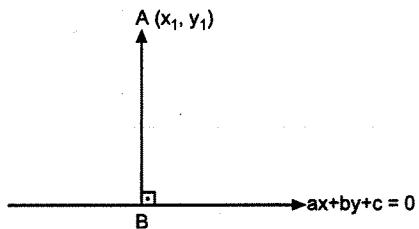


$$\frac{x}{a} + \frac{y}{b} = 1$$

#### Bilinmesi gereken bazı kurallar

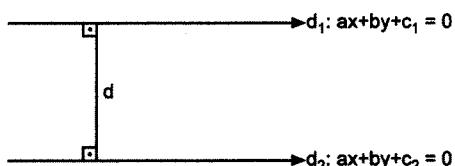
- \*  $ax + by + c = 0$  doğrusunun eğimi  $\frac{-a}{b}$  dir.
- \*  $y = mx + n$  doğrusunun eğimi  $m$  dir.
- \* İki doğru birbirine平行 ise eğimleri eşittir.
- $d_1 \parallel d_2 \Rightarrow m_1 = m_2$
- \* İki doğru birbirine dik ise eğimleri çarpımı  $-1$  e eşittir.
- $d_1 \perp d_2 \Rightarrow m_1 \cdot m_2 = -1$
- \* Bir doğru bir noktadan geçiyorsa bu nokta bu doğruya sağlar.
- \* İki doğrunun kesim noktası, iki denklem ortak çözümlere bulunur veya yok etme yöntemi ile  $x$  ve  $y$  bulunur. Bulunan  $x$  ve  $y$   $A(x, y)$  gibi bir noktadır.

- Bir noktanın bir doğruya olan uzaklığı



$$|AB| = \frac{|ax_1 + by_1 + c|}{\sqrt{a^2 + b^2}}$$

- \* Paralel iki doğru arasındaki uzaklık:

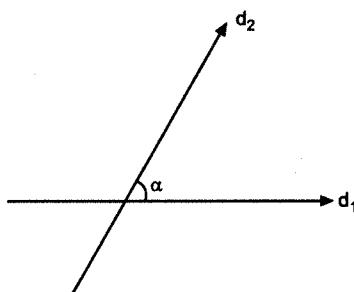


$$d = \frac{|c_1 - c_2|}{\sqrt{a^2 + b^2}}$$

#### İki Doğrunun Açıortay Denklemleri

$$\frac{|a_1x + b_1y + c_1|}{\sqrt{a_1^2 + b_1^2}} = \frac{|a_2x + b_2y + c_2|}{\sqrt{a_2^2 + b_2^2}}$$

#### İki Doğru Arasındaki Açıının Tanjantı



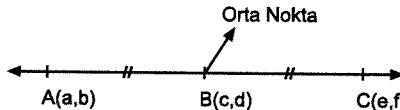
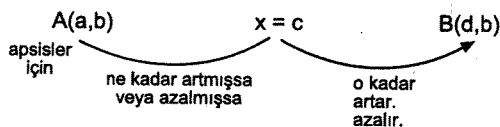
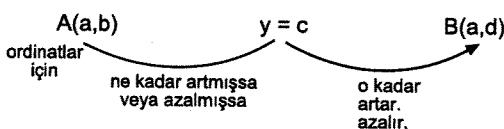
$$\tan \alpha = \frac{m_2 - m_1}{1 + m_1 \cdot m_2}$$

## SİMETRİ

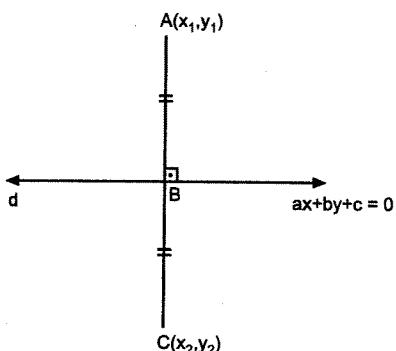
A(a,b) noktasının;

- \* Orjine göre simetriği  $B(-a, -b)$
- \*  $y = x$ 'e göre simetriği  $B(b, a)$
- \*  $y = -x$ 'e göre simetriği  $B(-b, -a)$
- \*  $Ox$ 'e göre simetriği  $B(a, b)$
- \*  $Oy$ 'e göre simetriği  $B(-a, b)$

\* A(a,b) noktasının B(c,d)'ye göre simetriği C(e,f) ise

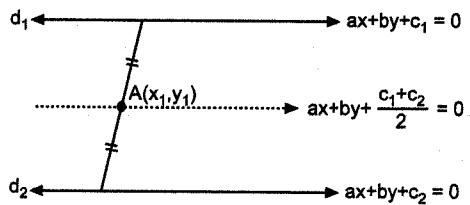
\* A(a,b) noktasının  $x = c$ 'ye göre simetriği;\* A(a,b) noktasının  $y = c$ 'ye göre simetriği;

Bir noktanın bir doğruya göre simetriği



- A noktasının d doğrusuna göre simetriği C(x<sub>2</sub>,y<sub>2</sub>) dir.
- B, A ile C'nin orta noktasıdır.
- B noktası d doğrusunu sağlar.
- [AC] ⊥ d olduğundan  $mAC \cdot md = -1$  (eğimleri çarpımı)
- A noktasının d doğrusuna olan uzaklığının iki katı A ile C noktaları arasındaki uzaklıktır.

## Bir doğrunun bir noktaya göre simetriği



Bir doğrunun bir noktaya göre simetriği alınırken x ve y'nin katsayılarını değiştirmeden bir doğru seçilir.  $d_1$  ile  $d_2$  doğruları A noktasına eşit uzaklıktadır.  $d_1$  ile  $d_2$  doğrularının sabit noktaları toplamının yarısı x ve y nin katsayılarını değiştirmeden bir doğru seçilir ve A noktası bir doğruya sağlayacağından sabit nokta bulunur ve simetri alınmış olur.

## Pratik Simetrliler

 $ax+by+c = 0$  doğrusunun;

- $y = x$ 'e göre simetriği  
Doğruda  
 $x$  yerine  $y$ ,  $y$  yerine  $x$  yazılarak bulunur.
- $y = -x$ 'e göre simetriği  
Doğruda  
 $x$  yerine  $-y$ ,  $y$  yerine  $-x$  yazarak bulabiliriz.
- $Ox$ 'e göre simetriği  $y$ 'nin önündeki işaret değişir.  
 $ax-by+c = 0$
- $Oy$ 'e göre simetriği:  $x$ 'in önündeki katsayının işaretini değişir.  $-ax+by+c = 0$
- Bir doğrunun  $y = x+2$ ,  $y = -x+2$  gibi eğimleri 1 veya -1 olan doğrulara göre simetriğinde.  
Örneğin; bir doğrunun  $y = x+2$  doğrusuna göre simetriğini bulalım.  
Doğruda  $y$  yerine  $x+2$ ,  $x$  yerine ise  $y-2$  yazarak bulabiliriz.
- $d_1 \perp d_2 \Rightarrow d_1$  doğrusunun  $d_2$  doğrusuna göre simetriği kendisidir. (yani  $d_1$  dir.)

- 1.**  $A(a, -b)$  2. bölgede ise  
 $B(-b, -a)$  kaçinci bölgdededir?

Cevap: 1

- 2.**  $A(a^2b, a+b)$  2. bölgede ise  
 $B(-a, b)$  kaçinci bölgdededir?

Cevap: 3

- 3.**  $A(a.b, a^2+b)$  3. bölgede ise  
 $B(\frac{a}{b}, a-b)$  kaçinci bölgdededir?

Cevap: 2

- 4.**  $A(|2-a|, |2-a|)$  ( $a \neq 2$ )  
 kaçinci bölgdededir?

Cevap: 1

- 5.**  $A(a^2-b^2, a-b)$  2. bölgede ise  
 $B(a-b, a+b)$  kaçinci bölgdededir?

Cevap: 4. bölge

- 6.**  $A(2m-8, m+1)$  2. bölgede ise  
 A noktalarından orjine en yakın olanı hangisidir?

Cevap: (-2,4)

- 7.**  $A(2m-8, m+6)$  2. bölgede ise  
 m nin tam sayı değerleri toplamı kaçtır?

Cevap: -9

- 8.**  $A(6; 4), B(-1, -10) \Rightarrow |AB| = ?$

Cevap:  $7\sqrt{5}$

9.  $A(-2, 3), B(3, -9) \Rightarrow |AB| = ?$

Cevap: 13

10.  $A(a, 4), B(3, -20) |AB| = 25$   
 $\Rightarrow a$  nin alabileceği değerler toplamı?

Cevap: 6

11.  $A(a, a), B(4, 2), |AB| = 10$  ise  
 $a$  nin alabileceği değerler toplamı?

Cevap: 6

12.  $A(m, 2), B(6, 2), C(9, -2)$   
 $\Rightarrow |AB| = |AC|$  ise  $m = ?$

Cevap:  $\frac{61}{6}$

13.  $A(0, 4), B(m, -4), C = (1, 2)$   
 $\Rightarrow |AB| = |BC|$  ise  $m = ?$

Cevap:  $-\frac{27}{2}$

14.  $A(6,4), B(9,2)$  noktaları Ox eksenindeki C noktasına eşit uzaklıkta ise C'nin apsis?

Cevap:  $\frac{11}{2}$

15.  $A(-2,6), B(4,8)$  noktaları Oy eksenindeki bir C noktasına eşit uzaklıkta ise C'nin ordinatı kaçtır?

Cevap: 10

16.  $A(m-2, m+4)$  noktası Ox ve Oy eksenine eşit uzaklıkta ise A noktası ne olabilir?

Cevap:  $(-3, 3)$

17.  $A(2,1)$  noktasının Ox eksenindeki B noktasına uzaklığı  $5\sqrt{2}$  br ise B nin apsisleri toplamı?

Cevap: 4

18.  $A(2,6)$  ve  $B(-10,12)$  noktaları veriliyor  $|AB|$  nin orta noktası nedir?

Cevap:  $(-4, 9)$

19.  $A(m,4)$ ,  $B(-2,8)$  orta noktası Oy ekseni üzerinde ise  $m = ?$

Cevap: 2

20.  $A(6,m-2)$ ,  $B(-2,4)$  noktaları için  $|AB|$  nin orta noktası Ox ekseni üzerinde ise  $m = ?$

Cevap: -2

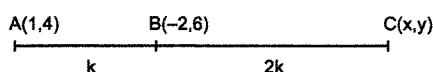
21.  $A(m+n, 2m-n)$ ,  $B(m-2, m+2)$   $[AB]$  nin orta noktası orjin ise,  $(m, n) = ?$

Cevap: (0, 2)

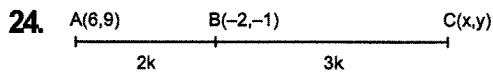
22.  $A(4,6)$ ,  $B(-2,8)$ ,  $C(2,4)$  noktaları ABC üçgeninin köşeleridir.

$|AB|$  ye ait kenarortay uzunluğu kaçtır?

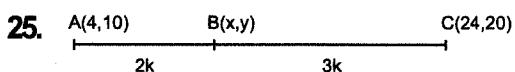
Cevap:  $\sqrt{10}$

23.  $A(1,4)$        $B(-2,6)$        $C(x,y)$   


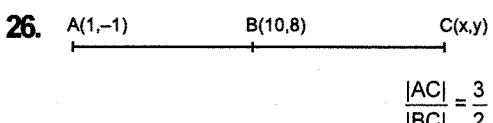
Cevap: (-8, 10)

24.  $A(6,9)$        $B(-2,-1)$        $C(x,y)$   


Cevap: (-14, -16)

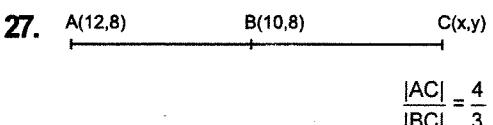
25.  $A(4,10)$        $B(x,y)$        $C(24,20)$   


Cevap: (12, 14)

26.  $A(1,-1)$        $B(10,8)$        $C(x,y)$   


$$\frac{|AC|}{|BC|} = \frac{3}{2}$$

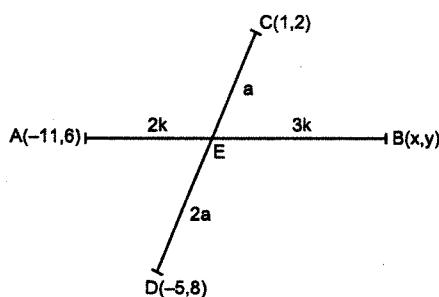
Cevap: (28,26)

27.  $A(12,8)$        $B(10,8)$        $C(x,y)$   


$$\frac{|AC|}{|BC|} = \frac{4}{3}$$

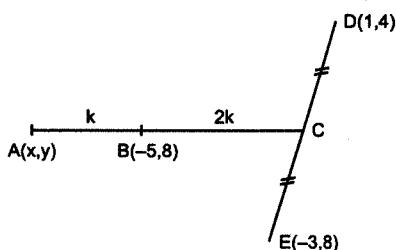
Cevap: (4,8)

28.



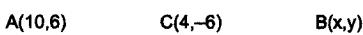
Cevap: (14, 1)

29.



Cevap: (-7, 9)

30.



$$\frac{|AC|}{|BC|} = \frac{2}{3}$$

Cevap: (-5, -24)

31. A(1, 4), B(-2, 3), C(-2, 2)

ÜçgeninIN ağırlık merkezinIN koordinatlarını bulunuz?

Cevap: (-1, 3)

32. A(1, 4), B(-2, 3), C(-5, 5)

ÜçgeninIN alanı kaç  $br^2$  dir?Cevap:  $\frac{9}{2}$ 

33. A(a, 4), B(6, 2), C(-1, 3)

ÜçgeninIN alanı  $4 br^2$  ise a nin alabilecegi değerler toplamı?

Cevap: -16

34. A(4, 8), B(-2, 6) ve ağırlık merkezi

G(1, 3) ise C(x, y) = ?

Cevap: (1, -5)

35. Köşeleri A(6, 4), B(-2, 12) ve C(x, y) olan bir üçgen için ağırlık merkezi x- eksenİ üzerinde ise C'nin ordinatı kaçtır?

Cevap: -16

36. Köşeleri A(1, 1), B(-2, 4), C(6, 9) ve D(-4, -2) olan ABCD dörtgeninin alanı kaç br<sup>2</sup> dir?

Cevap: 24

37. Köşeleri A(1, 2), B(4, -2), C(6, 12) ve D(x, y) olan paralelkenarın D köşesinin koordinatları kaçtır?

Cevap: (3, 16)

- 38.
- 
- D(-4,5) Paralelkenarın A köşesi- nin koordi- natlarını bu- lun.

Cevap: (-1, 2)

- 39.
- 
- D(-6,10) F noktasının koordinatla- rını bulunuz.

Cevap:  $\left(\frac{10}{3}, 8\right)$

40. A(4, 2), B(-6, 10) noktalarından geçen doğrunun eğimi nedir?

Cevap:  $-\frac{4}{5}$

41. A(-2, m), B(4, 2) noktalarından geçen doğrunun eğimi 2 ise m=?

Cevap: -10

42. A(2,k), B(-1,4), C(6,-2)

noktaları aynı doğru üzerinde ise k=?

Cevap:  $\frac{10}{7}$

43. A(4,2) noktasından geçen ve eğimi  $\frac{1}{2}$  olan doğrunun denklemi?

Cevap:  $y = \frac{x}{2}$

- 44.** A(-2,4) ve B(6,m) noktalarından geçen doğrunun eğimi m ise, m=?

Cevap:  $-\frac{4}{7}$

- 45.** A(4,6) noktasından geçen doğrunun denklemi  $y=4x+m$  ise, m=?

Cevap: -10

- 46.** A(-2,3) noktasından geçen doğrunun denklemi  $y=mx+4$  ise, m=?

Cevap:  $\frac{1}{2}$

- 47.** A(6,k) noktasından geçen doğrunun denklemi  $y=2x+4$  ise, k=?

Cevap: 16

- 48.**  $y=2x-m$  doğrusu üzerindeki noktalar A(1,m) ve B(m,n) ise, n=?

Cevap: 1

- 49.**  $y=4x$  doğrusu üzerindeki nokta A(k,k+6) ise, k=?

Cevap: 2

- 50.**  $y=2x+3$  doğrusu üzerindeki noktaların en genel gösterimi nasıl olabilir?  
 $a \in \mathbb{R}$

Cevap:  $(a, 2a+3)$

- 51.**  $x=2y-6$  doğrusu üzerindeki noktaların en genel gösterimi nasıl olabilir?

Cevap:  $(2m-6, m)$

- 52.** Eğimi 2 ve A(1,4) noktasından geçen doğrunun x eksenini kestiği nokta nedir?

Cevap: (-1,0)

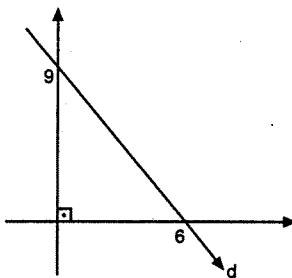
- 53.** Eğimi 3 ve A(4,18) noktasından geçen doğrunun y eksenini kestiği noktanın ordinatı?

Cevap: 6

54. Eğimi  $\frac{3}{4}$  ve A(2,6) noktasından geçen doğrunun eksenlerle oluşturduğu bölgenin alanı?

Cevap:  $\frac{27}{2}$

59.



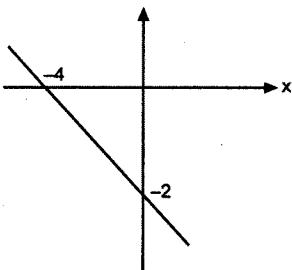
Doğrunun denklemi bulunuz?

Cevap:  $3x+2y-18=0$

55.  $2x+3y-12=0$  doğrusunun Ox ve Oy'yi kestiği noktalar arası uzaklık kaç br dir?

Cevap:  $2\sqrt{13}$

60.



Doğrunun denklemi bulunuz?

Cevap:  $x+2y+4=0$

56. A(4,2), B(6,-2) noktalarından geçen doğrunun denklemi nedir?

Cevap:  $y+2x-10=0$

57. A(-2,1), B(2,6) noktasından geçen doğrunun denklemi nedir?

Cevap:  $4y-5x-14=0$

61. Ox eksenini 4'te Oy eksenini 3'te kesen doğrunun denklemi bulunuz?

Cevap:  $3x+4y-12=0$

58. A(6,4) ve B(-2,8) noktalarından geçen doğrunun x eksenini kestiği noktası ile y eksenini kestiği noktası arasındaki uzaklık kaç br dir?

Cevap:  $7\sqrt{5}$

62. Ox'i 6 Oy'yi -8 de kesen doğrunun eğimi kaçtır?

Cevap:  $\frac{4}{3}$

63.  $Ox$  i  $A$  da,  $Oy$  yi  $B$  de kesen doğru için  $|AB|=13$  ve eğimi  $\frac{12}{5}$  ise doğrunun denklemi ne olabilir?

Cevap:  $-12x+5y-60=0$

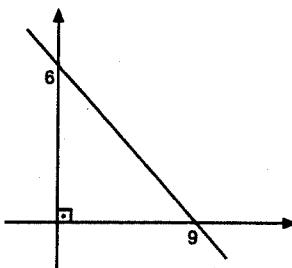
64.  $ax+by+c=0$  doğrusunun  $Ox$  i kestiği nokta 6,  $Oy$  yi kestiği noktası  $-8$  ise  $C$  kaç olabilir?

Cevap: -24

65.  $Ox$  i 4,  $Oy$  yi  $-3$  te kesen doğru  $A(1,m)$  noktasından geçtiğine göre  $m$  kaç olur?

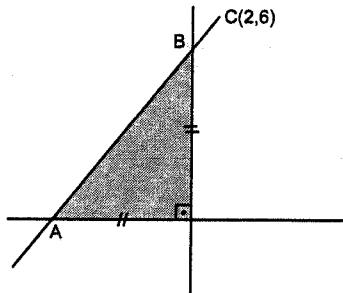
Cevap:  $-\frac{9}{4}$

66. eğimi?



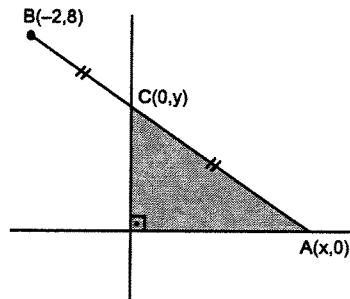
Cevap:  $-\frac{2}{3}$

67. T.A=?



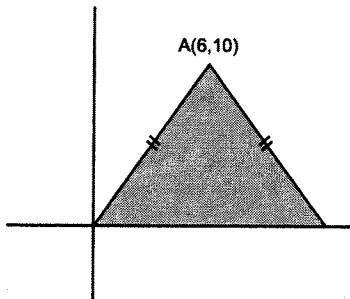
Cevap: 8

68. T.A=?



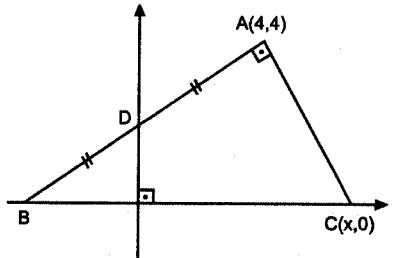
Cevap: 4

69. T.A=?



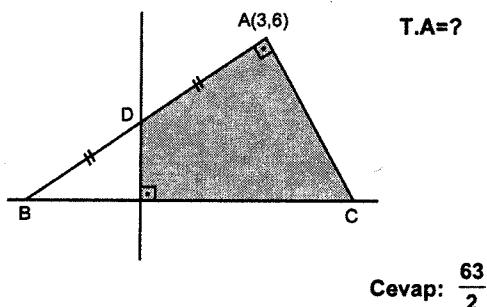
Cevap: 60

70. x=?

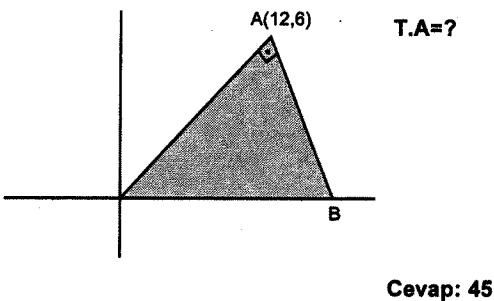


Cevap: 6

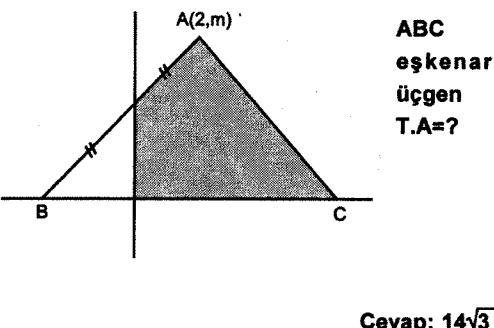
71.



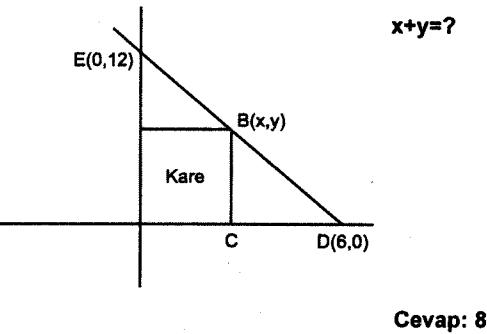
72.



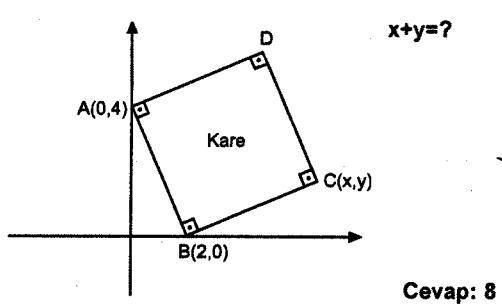
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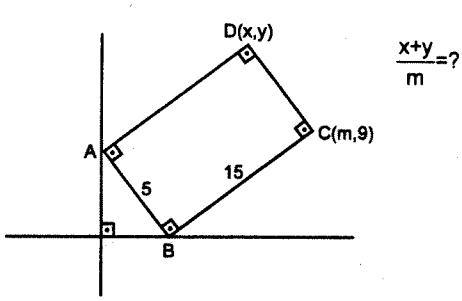
74.



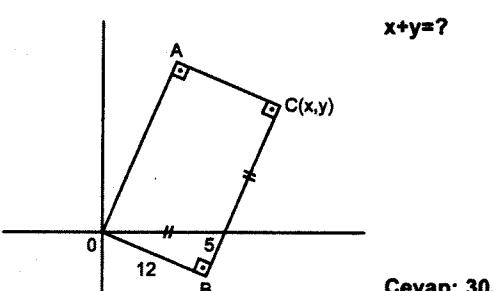
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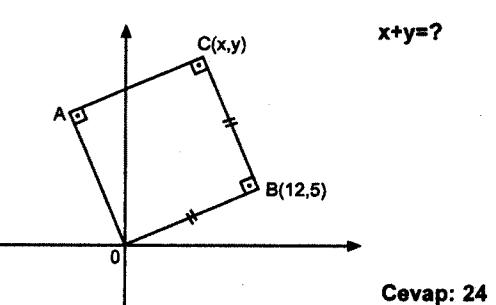
76.



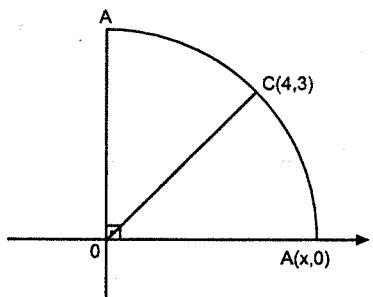
77.



78.

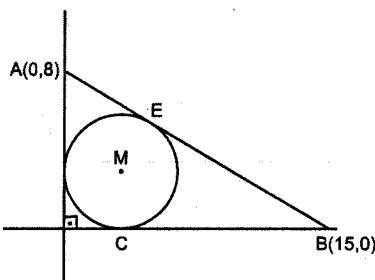


79.



$x = ?$

83.

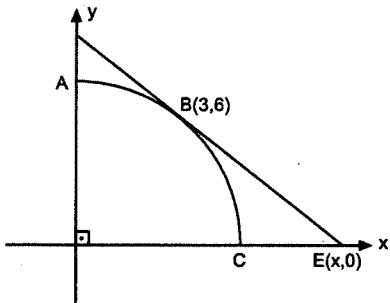


$m(x,y) = ?$

Cevap: 5

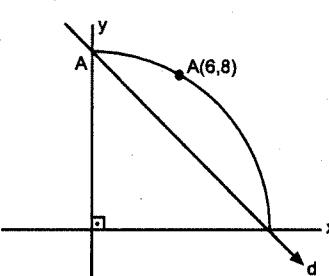
Cevap: (3,3)

80.

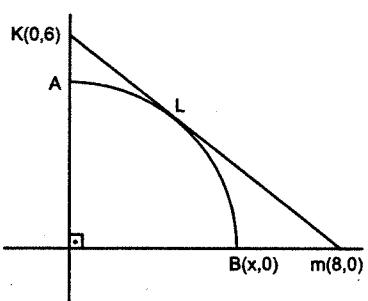


$x = ?$

84.

d doğrusunun  
denklemini  
bulunuz.Cevap:  $x+y-10=0$ 

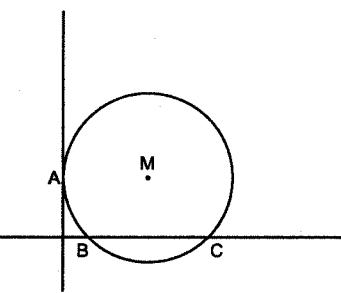
81.



$x = ?$

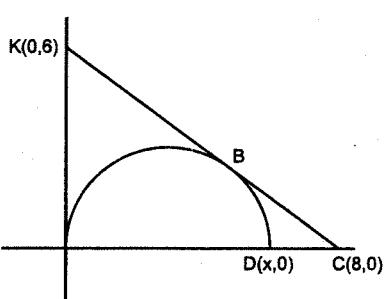
Cevap:  $\frac{24}{5}$ 

85.

 $B(2,0)$   
 $C(8,0)$   
 $m(x,y) = ?$ 

Cevap: (5,4)

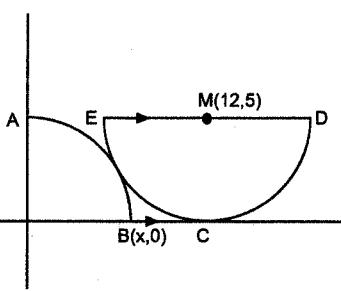
82.



$x = ?$

Cevap: 6

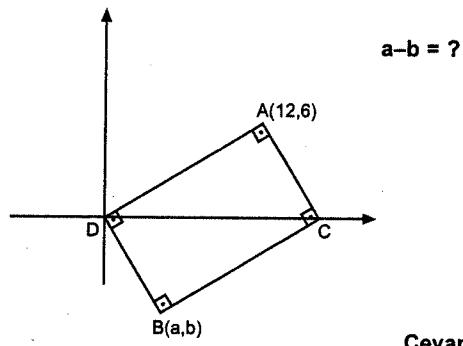
86.



$x = ?$

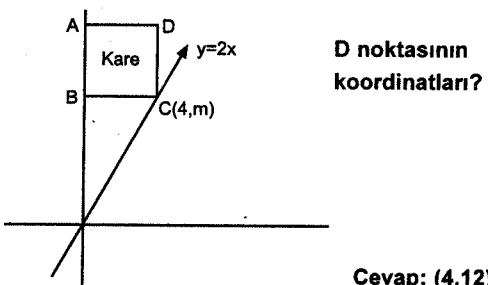
Cevap: 8

87.



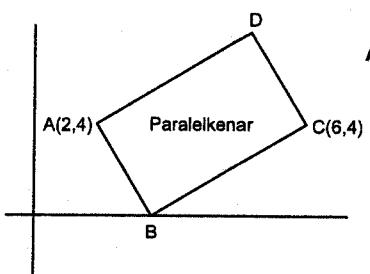
Cevap: 9

88.



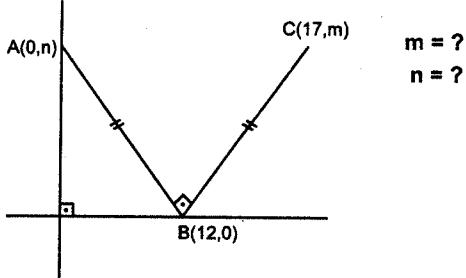
Cevap: (4, 12)

91.

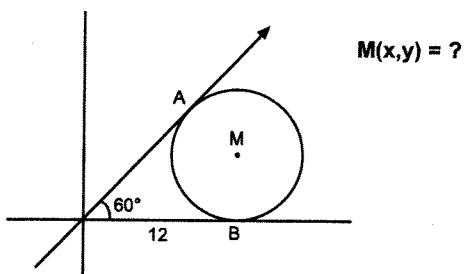


Cevap: 16

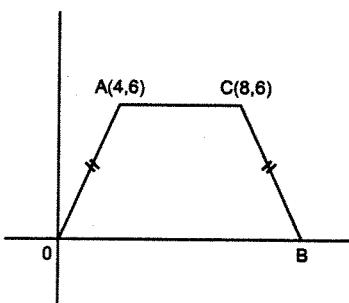
92.

Cevap:  $m = 12$   
 $n = 5$ 

89.

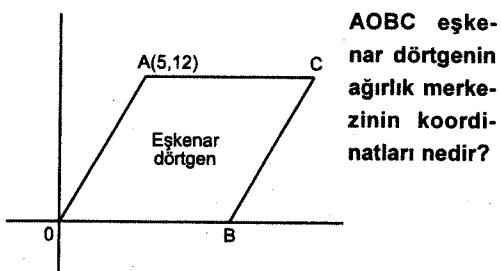
Cevap:  $(12, 4\sqrt{3})$ 

93.



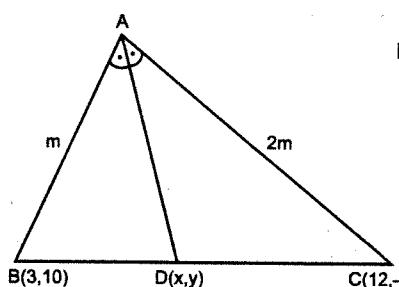
Cevap: 48

90.



Cevap: (9, 6)

94.



Cevap: (6, 6)

95.  $2x+3y+6 = 0$  doğrusunun eğimi?

Cevap:  $-\frac{2}{3}$

96.  $ax+3y-5 = 0$  doğrusunun eğimi  $\frac{2}{3}$  ise

$a = ?$

Cevap: -2

97.  $2x-3y+6 = 0$  doğrusu  $3x-my+n = 0$  doğrusuna paralel ise,  $a = ?$

Cevap:  $\frac{9}{2}$

98.  $-2x+y+6 = 0$  doğrusu  $3x+ay = 0$  doğrusuna paralel ise,  $a = ?$

Cevap:  $-\frac{3}{2}$

99.  $d_1 : ax+2y-3 = 0$   
 $d_2 : (a-1)x + 4y - 6 = 0$   $d_1 \parallel d_2 \Rightarrow a = ?$

Cevap: -1

100.  $d_1 : ax+4y-5 = 0$

$d_2 : 2x-3y+1 = 0$

doğruları birbirine dik  
ise  $a = ?$

Cevap: 6

101.  $(a+1)x-(a+1)y-2 = 0$

$d_2 : ax+y-1 = 0$

$d_1 \perp d_2 \Rightarrow a = ?$

Cevap: 1

102.  $2x+3y-5 = 0$  doğrusuna paralel ve A(1,2) noktasından geçen doğrunun denklemi nedir?

Cevap:  $2x + 3y - 8 = 0$

103.  $x-2y-2 = 0$  doğrusuna paralel ve A(2,6) noktasından geçen doğrunun denklemi nedir?

Cevap:  $x - 2y + 10 = 0$

104.  $2x-y+6 = 0$  doğrusuna dik ve A(1,2) noktasından geçen doğrunun denklemi?

Cevap:  $x + 2y - 5 = 0$

- 105.**  $3x-y+6=0$  doğrusu üzerindeki  $A(3,k)$  noktasında dik kesişen doğrunun denklemi?

Cevap:  $x+3y-48=0$

- 106.**  $2x+y-6=0$  doğrusu ile  $Ox$  ekseni üzerinde dik kesişen doğrunun denklemi?

Cevap:  $2y-x+3=0$

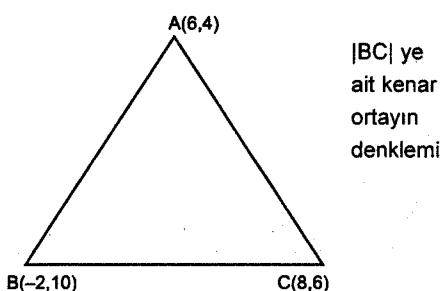
- 107.**  $3x-4y+12=0$  doğrusu ile  $Oy$  ekseni üzerindeki dik kesişen doğrunun denklemi?

Cevap:  $3y+4x-9=0$

- 108.**  $2x-y+6=0$  doğrusu ile  $Oy$  ekseni üzerinde dik kesişen doğrunun denklemi?

Cevap:  $x+2y-12=0$

- 109.**



Cevap:  $3y+4x-36=0$

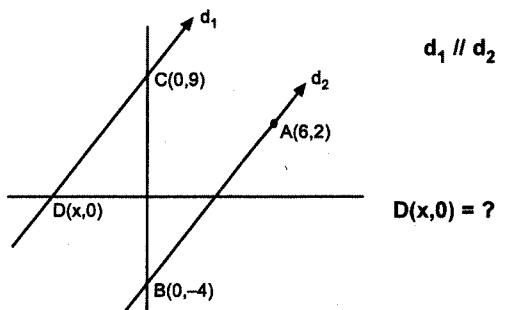
- 110. 109.** sorudaki şekil için  $A$  dan geçen  $|BC|$  ye paralel olan doğrunun denklemi?

Cevap:  $5y+2x-32=0$

- 111. 109.** sorudaki şekil için  $A$  dan geçen  $[BC]$  ye dik olan doğrunun denklemi?

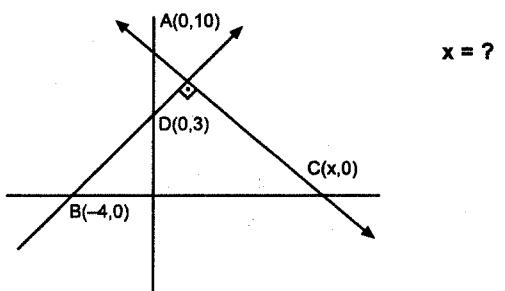
Cevap:  $2y-5x+22=0$

- 112.**



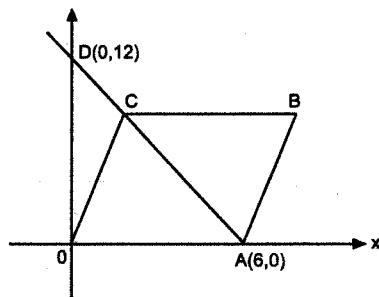
Cevap:  $(-9,0)$

- 113.**



Cevap:  $\frac{15}{2}$

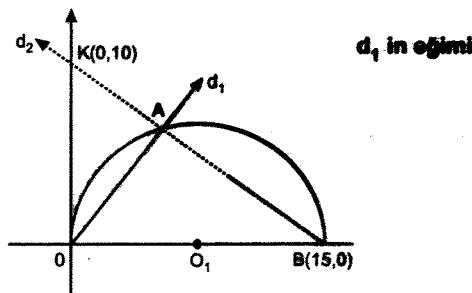
114.



COAB  
eşkenar  
dörtgen  
 $|OB|$  nin  
denklemi

$$\text{Cevap: } y = \frac{x}{2}$$

115.

 $d_1$  in eğimi

$$\text{Cevap: } \frac{3}{2}$$

116.

$$x-y+6=0 \text{ ve } x+y-4=0$$

doğrularının kesim noktasını bulunuz?

$$\text{Cevap: } (-1, 5)$$

117.

$$2x-y+6=0, \quad 3x+y+m=0$$

doğrularının kesim noktası  $(2, k)$  ise  $m = ?$ 

$$\text{Cevap: } -16$$

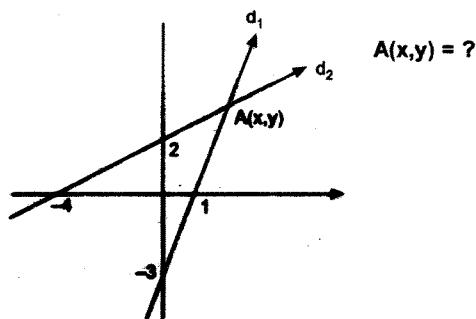
118.

$$x+y-2=0, \quad 2x-y+8=0$$

doğrularının kesim noktasından geçen ve  
 $3x-y+6=0$  doğrusuna平行 olan doğrunun  
denklemi?

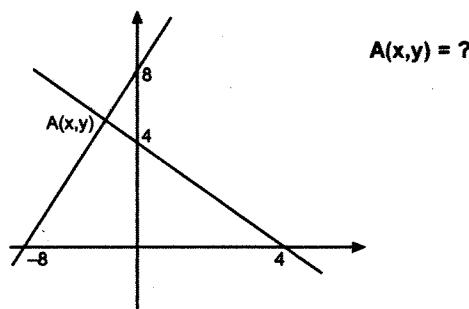
$$\text{Cevap: } y=3x+10$$

119.



$$\text{Cevap: } (2, 3)$$

120.



$$\text{Cevap: } A(-2, 6)$$

121.  $x-y+3=0$ 

$$2x+y-12=0$$

doğrularının kesim noktasından geçen ve  
 $2x+3y-4=0$  doğrusuna dik olan doğrunun  
denklemi?

$$\text{Cevap: } 2y-3x-3=0$$

**122.**  $3x-y+4=0$   
 $x+y-12=0$   
 $mx+2y-10=0$

doğruları aynı noktada kesişiyor ise  $m = ?$

Cevap: -5

**123.**  $4x-y-12=0$   
 $x+y+n=0$

doğruları O<sub>x</sub> eksenini üzerinde kesişiyor ise  $n = ?$

Cevap: -3

**124.**  $3x+4y+24=0$   
 $3x+ay-18=0$

doğruları O<sub>y</sub> eksenini üzerinde kesişiyor ise  $a = ?$

Cevap: -3

**125.**  $ax+2y-8=0$  ve  
 $mx+y+4=0$

doğruları dik kesişiyor ise kesim noktasının orjine olan uzaklığı kaç br dir?

Cevap: 4

**126.**  $4x+3y+24=0$   
 $ax+3y-6=0$

doğruları  $x = 2$  doğrusu üzerinde kesişiyor ise  $a = ?$

Cevap: 19

**127.**  $2x-3y+12=0$   
 $x+my-2=0$

doğruları  $y=4$  doğrusu üzerinde kesiştiğine göre  $m = ?$

Cevap:  $\frac{1}{2}$

**128.**  $2x-y+12=0$   
 $ax+3y-4=0$

doğruları  $y=x$  doğrusu üzerinde kesiştiğine göre  $a = ?$

Cevap:  $-\frac{10}{3}$

**129.**  $13x+5y-18=0$   
 $7x+3y+9=0$

doğrularının kesim noktasından ve orjinden geçen doğrunun eğimi?

Cevap:  $-\frac{27}{11}$

**130.**  $16x-17y+4=0$   
 $9x+28y-8=0$

doğrularının kesim noktasından ve orjinden geçen doğrunun eğimi kaçtır?

Cevap:  $\frac{41}{6}$

**131.**  $-2 \leq x \leq 4$   
 $-3 \leq y \leq 0$

doğrularının sınırlandırdığı bölgenin alanı kaç  $br^2$  dir?

Cevap: 18

**132.**  $|x| \leq 4$   
 $|y-2| \leq 3$

doğrularının sınırlandırdığı bölgenin alanı?

Cevap: 48

**133.**  $y-x+6 = 0$   
 $y+x-4 = 0$

ve Ox eksenleri arasında kalan bölgenin alanı?

Cevap: 1

**134.**  $2x+y+12 = 0$   
 $x-y+3 = 0$

ve Oy eksenleri arasında kalan bölgenin alanı?

Cevap:  $\frac{75}{2}$

**135.**  $3x+y-18 = 0$   
 $x-y-8 = 0$

doğrularının eksenlerle oluşturduğu bölgenin alanı?

Cevap:  $\frac{61}{2}$

**136.**  $x-y-4 = 0$   
 $x+y+6 = 0$   
 $x = 6$

doğrularının sınırlandırdığı bölgenin alanı?

Cevap: 49

**137.**  $2x-3y-6 = 0$   
 $x = 4$   
 $Ox$

doğrularının sınırlandırdığı bölgenin alanı?

Cevap:  $\frac{1}{3}$

**138.**  $3x-4y-12 = 0$   
 $y = 6$   
 $Oy$

doğrularının sınırlandırdığı bölgenin alanı?

Cevap: 54

**139.**  $6x-y+12 = 0$   
 $x+y+2 = 0$

doğruları ve Oy eksenleri arasında kalan bölgenin alanı kaç  $br^2$  dir?

Cevap: 14

**140.**  $y \geq 2x$   
 $y \leq -x$   
 $x \leq 6$

ile sınırlanan bölgenin alanı?

Cevap: 54

**141.**  $(m-1)x + (n+1)y - 2 = 0$   
 $2x - 3y + 6 = 0$

doğruları çakışık ise  $m+n=?$

Cevap:  $\frac{1}{3}$

**142.**  $(m+1)x - (2m-6)y + 16 = 0$

doğrularının geçtiği sabit nokta?

Cevap:  $(-4, -2)$

**143.**  $(m+1)x - (2m-6)y + 16 = 0$

doğrularının kesim noktasından geçen doğru  $2x-3y+k=0$  ise  $k=?$

Cevap: 2

**144.**  $x-(m+1)y-12 = 0$

doğrularının kesim noktasının Oy ye olan uzaklığı kaç brdir?

Cevap: 12

**145.**  $(m-3)x + (m-4)y - 12 = 0$

doğrularının kesim noktasından geçen ve  $2x-3y-6 = 0$  doğrusuna paralel olan doğrunun denklemi?

Cevap:  $2x-3y-60 = 0$

**146.**  $(2m-6)x + (m+1)y - 16 = 0$

doğrularının kesim noktasından geçen  $x-y-2=0$  doğrusuna dik olan doğrunun denklemi?

Cevap:  $x+y-2 = 0$

**147.**  $mx + (m-2)y - 4m + 12 = 0$

doğrularının kesim noktası ve orjinden geçen doğrunun denklemi?

Cevap:  $3x+y = 0$

**148.**  $(m+1)x - (m-2)y - 4m + 20 = 0$

doğrularının kesim noktasından geçen ve  $x=2$  ye paralel olan doğrunun denklemi?

Cevap:  $x=4$

**149.**  $(m-6)x + 12(m-1)y - 12 = 0$

doğrularının kesim noktasından geçen ve  $y=2$  ye paralel olan doğrunun denklemi?

Cevap:  $y = \frac{1}{5}$

**150.** A( $m-1, m+1$ )

noktalarının belirtilen doğrunun denklemi?

Cevap:  $x-y+2 = 0$

**151.** A( $m+1, 2m-3$ )

noktalarının geçen doğrunun denklemi?

Cevap:  $2x-y-5 = 0$

**152.**  $A(k-2, 2k+1)$ 

noktalarından geçen doğrunun eksenlerle oluşturduğu bölgenin alanı?

Cevap:  $\frac{25}{4}$

**153.**  $A\left(\frac{k+1}{2}, 3k\right)$ 

noktalarının geometrik yer denlemesini bulunuz?

Cevap:  $y=6x-3$

**154.**  $A(4m-1, 2m+6)$ ,  $B(3m-8, m)$ 

noktalarının orta noktasının geometrik yer denlemesini bulunuz?

Cevap:  $6x-14y+69 = 0$

**155.**  $A(t, 2t-2)$  noktalarından geçen doğru  $y=ax$  doğrusuna paralel ise  $a=?$ 

Cevap: 2

**156.**  $A(2p, p-4)$  noktalarından geçen doğru  $y+ax-5=0$  doğrusuna dik ise  $a=?$ 

Cevap: 2

**157.**  $A(m-2, m+1)$  noktalarının oluşturduğu doğru ile  $B(t+2, t-1)$  noktalarının oluşturduğu doğrusunun kesim noktası nedir?

Cevap: Boş kümə

**158.**  $A(1, 5)$  noktasının,  $3x-4y+8=0$  doğrusuna olan uzaklığı kaç br?

Cevap:  $\frac{9}{5}$

**159.**  $A(-2, 5)$  noktasının  $5x+12y+15=0$  doğrusuna olan uzaklığı kaç br dir?

Cevap: 5

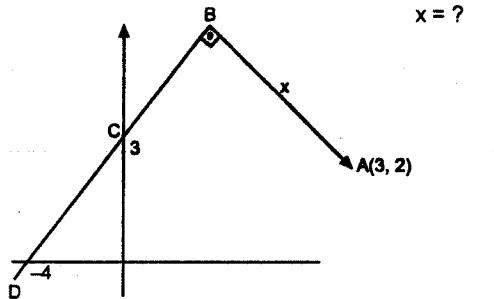
**160.**  $A(m, 2)$  noktasının  $x-y+6 = 0$  doğrusuna olan uzaklığı  $2\sqrt{2}$  br ise m nin alabileceği değerler?

Cevap:  $\{0, -8\}$

**161.**  $A(4, 6)$  noktasının  $3x+4y+m = 0$  doğrusuna olan uzaklığı 2 ise m kaç olabilir?

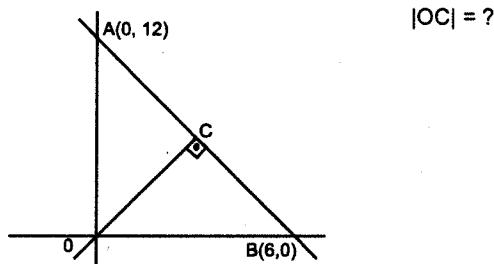
Cevap:  $\{-26, -46\}$

162.



$$\text{Cevap: } \frac{13}{5}$$

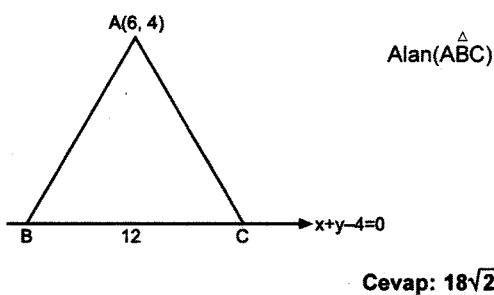
163.



$$|OC| = ?$$

$$\text{Cevap: } \frac{12}{\sqrt{5}}$$

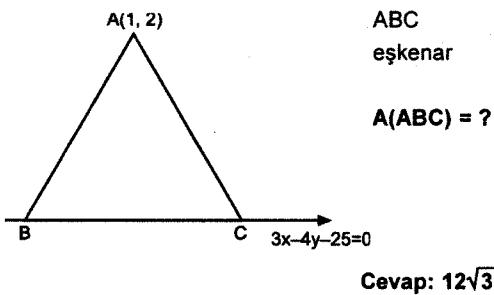
164.



$$\text{Cevap: } 18\sqrt{2}$$

$$\text{Alan}(\triangle ABC)$$

165.



ABC  
eşkenar

$$\text{A(ABC)} = ?$$

$$\text{Cevap: } 12\sqrt{3}$$

166.  $2x-3y-3=0$ 

$$2x-3y-16=0$$

doğruların arasındaki uzaklık?

Cevap:  $\sqrt{13}$ 167.  $d_1 : 2x+3y+6=0$   $d_1 // d_2$   
 $d_2 : (m-2)x+4y-8=0$  ised<sub>1</sub> ile d<sub>2</sub> doğruları arasındaki uzaklık kaç br dir?Cevap:  $\frac{12}{\sqrt{13}}$ 168.  $x-y-2=0$   
 $x-y+m=0$ doğruların arasındaki uzaklık  $\sqrt{2}$  br ise m kaç olabilir?Cevap: m = 0  
m = -4169.  $4x-3y+12=0$   
 $-8x+6y+24=0$ 

doğruların arasındaki uzaklık kaçtır?

Cevap:  $\frac{24}{5}$ 170.  $4x-3y-12=0$   
 $4x-3y+18=0$ 

doğruların arasındaki yerleştirilebilecek en büyük eşkenar üçgenin alanı?

Cevap:  $12\sqrt{3}$

**171.**  $x - y - 6 = 0$

$$x - y - 16 = 0$$

doğruları arasındaki yerleştirebilecek en büyük karenin alanı?

Cevap: 50

**172.**  $4x + 3y - 12 = 0$

$$4x + 3y - 42 = 0$$

doğrularının  $30^\circ$ lik açıyla kesen doğrunun paralel doğrular arasındaki kalan doğru parçasının uzunluğu kaç br dir?

Cevap: 12

**173.**  $x - 2y - 6 = 0$

$$2x + y - 2 = 0$$

doğrularının açıortay denkleminden biri nedir?

Cevap:  $x + 3y + 4 = 0$

**174.**  $4x - 3y - 12 = 0$  ile  $Ox$

doğrularının açıortay denklemelerinden birinin eğimi kaçtır?

Cevap:  $\frac{1}{2}$

**175.**  $3x - y - 6 = 0$

$$x - 3y + 12 = 0$$

doğrularına eşit uzaklıkta bulunan noktaların geometrik yeri ne olabilir?

Cevap:  $x + y - 9 = 0$

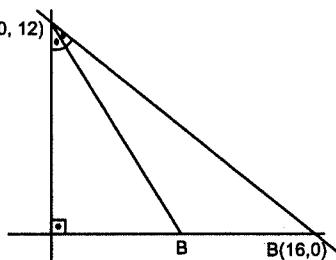
**176.** Eğimleri  $2$  ile  $\frac{1}{2}$  olan doğruların açıortay denklemelerinden birinin eğimi kaç olabilir?

Cevap: 1

**177.** Eğimleri  $\frac{3}{4}$  ile  $\frac{4}{3}$  olan doğruların açıortay denklemelerinden birinin eğimi kaç olabilir?

Cevap: -1

**178.**



[AB] nin  
denklemi?

Cevap:  $2x + y - 12 = 0$

**179.**  $\sqrt{3}x - y - 6 = 0$

$$\sqrt{3}x + y - 12 = 0$$

doğrular arasındaki dar açı?

Cevap: 60

**180.**  $\frac{\sqrt{3}}{3}x - y - 12 = 0$

$$x - y - 6 = 0$$

doğruları arasındaki geniş açı?

Cevap: 165

**181.**  $\sqrt{3}x - y = 0$

$$x + y - 6 = 0$$

doğruları arasındaki geniş açı?

Cevap: 105

**182.**  $x - y - 4 = 0$

$$x + y - 6 = 0$$

doğruları arasındaki açı kaç derecedir?

Cevap: 90

**183.**  $mx - 4y - 6 = 0$

$$2x - y + 2 = 0$$

doğruları arasındaki açı  $45^\circ$  ise  $m = ?$

Cevap: -12

**184.**  $2x - y - 6 = 0$

$$3x + y + 4 = 0$$

doğruları arasındaki geniş açısının tanjantı?

Cevap: -1

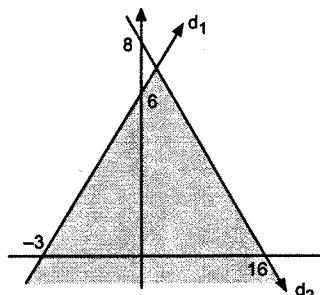
**185.**  $ax - 2y + 6 = 0$

$$4x - 2y - 2 = 0$$

doğruları arasındaki açısının tanjantı  $\frac{3}{2}$  ise  $a = ?$

Cevap:  $-\frac{7}{2}$

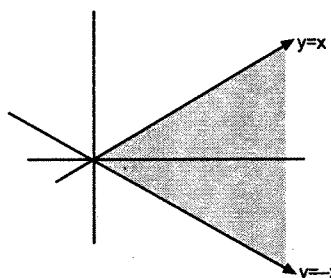
**186.**



Taralı bölgeyi ifade eden eşitsizlik sistemi nedir?

Cevap:  $x + 2y - 16 \leq 0$   
 $2x - y + 6 \geq 0$

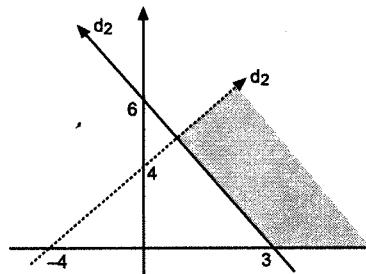
**187.**



Taralı bölgeyi ifade eden eşitsizlik sistemi nedir?

Cevap:  $y \leq |x|$

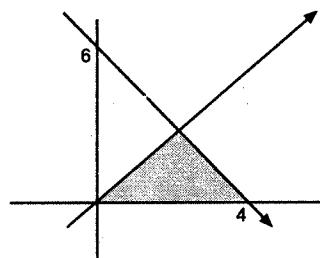
**188.**



Taralı bölgeyi ifade eden eşitsizlik sistemi nedir?

Cevap:  $x - y + 4 > 0$   
 $2x + y - 6 \geq 0$

**189.**



Taralı bölge nasıl ifade edilir?

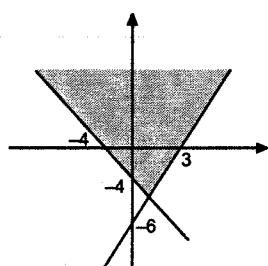
Cevap:  $y \leq x$   
 $3x + 2y - 12 \leq 0$   
 $xy \geq 0$

190.  $2x-y-6 \leq 0$

$x+y+4 \geq 0$

eşitsizliği analitik düzlemde gösterimi?

Cevap:

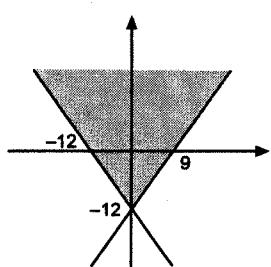


191.  $4x-3y-36 \leq 0$

$x+y+12 \geq 0$

eşitsizliği analitik düzlemde gösterimi?

Cevap:



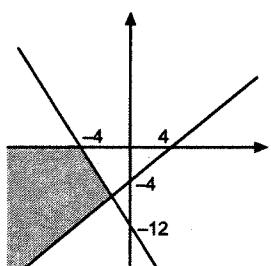
192.  $3x+y+12 \leq 0$

$x-y-4 \leq 0$

$x.y \geq 0$

analitik düzlemde gösterimi?

Cevap:



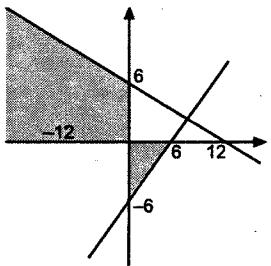
193.  $y-x+6 \geq 0$

$2y+x-12 \leq 0$

$x.y \leq 0$

analitik düzlemde gösterimi?

Cevap:



194.  $(x-y+6) . (x+y-4) = 0$

doğrularının kesim noktasını bulunuz?

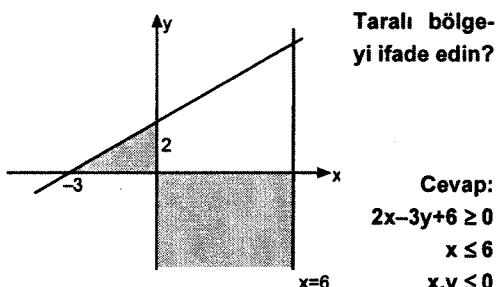
Cevap: (-1, 5)

195.  $x^2+y^2-2xy-9 \leq 0$  ve  $x.y \leq 0$

analitik düzlemde belirttiği bölgenin alanı?

(Cevap: 9)

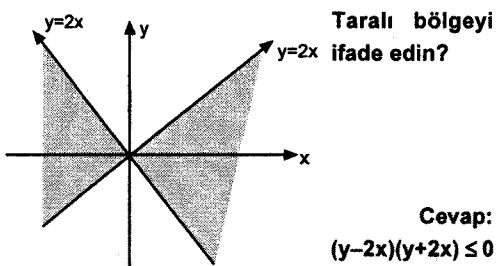
196.



Taralı bölgeyi ifade edin?

Cevap:  
 $2x-3y+6 \geq 0$   
 $x \leq 6$   
 $x.y \leq 0$ 

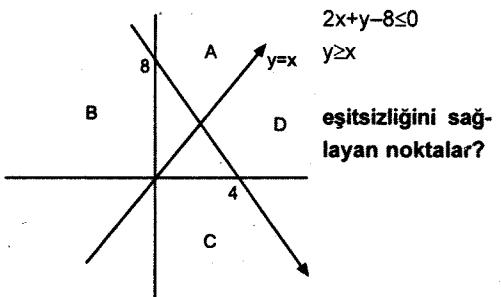
197.



Taralı bölgeyi ifade edin?

Cevap:  
 $(y-2x)(y+2x) \leq 0$ 

198.



$2x+y-8 \leq 0$   
 $y \geq x$

eşitsizliğini sağlayan noktalar?

Cevap: B bölgesi

**199.** A(1,2) noktasının B(-6, 4) noktasına göre simetriği C;

- C nin Ox'e göre simetriği D
- D nin orjine göre simetriği E
- E nin F(4, 12) göre simetriği G
- G nin Oy ye göre simetriği H
- H in  $x=4$  e göre simetriği I
- I nin  $y=-2$  e göre simetriği J
- J nin  $y=-x$  e göre simetriği K
- K nin A(1,2) ye göre simetriği L
- L nin M(6,3) e göre simetriği N
- N nin Ox e göre simetriği O
- O nun orjine göre simetriği Ö
- Ö nun P(3,5) göre simetriği R
- R nin O ya göre simetriği S
- S nin  $\$(-1, -2)$  göre simetriği T
- T nin  $x=3$  e göre simetriği U
- U nun  $y=6$  ya göre simetriği V
- V nin  $y=x$  e göre simetriği Y
- Y nin  $y=-x$  e göre simetriği Z=?

Cevap: (-5, 18)

**200.** A(6,4) noktası  $x-y-6=0$  doğrusuna göre simetriği B ise  $|AB|=?$

Cevap:  $4\sqrt{2}$

**201.** A(3,4) noktasının  $3x+4y+a=0$  doğrusuna göre simetriği B ise  $|AB|=6$  ise a nin alabileceği değerler toplamı?

Cevap: -50

**202.** A(1, -1) noktasının  $x-y+6=0$  doğrusuna göre simetriği B(x,y)=?

Cevap: (-7, 7)

**203.** A(4, -6) noktasının  $2x+y-2=0$  doğrusuna göre simetriği B nedir?

Cevap: A(4, -6)

**204.** A(2, 3) noktasının  $y=mx+n$  doğrusuna göre simetriği B(-12, 7) ise  $m+n=?$

Cevap: 26

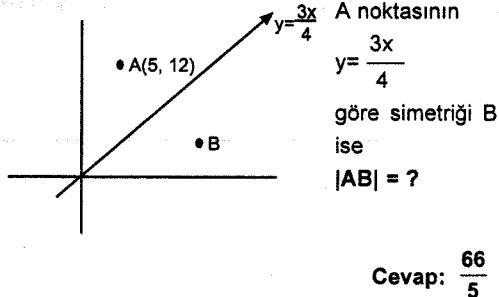
**205.** A(4, m) noktasının  $2x-3y+k=0$  doğrusuna göre simetriği B(m,2) ise m=?

Cevap: 8

**206.** A(6, 3) noktasının  $3x-ny+k=0$  doğrusuna göre simetriği B(2, -3) ise n-k = ?

Cevap:  $\frac{15}{2}$

207.

208.  $4x-y-2=0$  doğrusunun A(1, 4) noktasına göre simetriği nedir?

Cevap:  $4x-y+2=0$

209.  $3x-2y+6=0$  doğrusunun A(-4, 2) ye göre simetriği nedir?

Cevap:  $3x-2y+26=0$

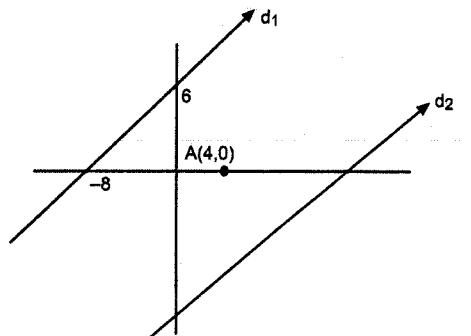
210.  $3x-6y+4=0$  doğrusunun A(k, 2) noktasına göre simetriği  $ax+6y+12=0$  ise a + k=?

Cevap:  $\frac{7}{3}$

211.  $4x-3y+10=0$  doğrusunun orijen göre simetriği nedir?

Cevap:  $4x-3y-10=0$

212.



Cevap:  $3x-4y-48=0$

213.  $3x+6y-24=0$  doğrusunun A(k, -2) ye göre simetriği B(-3, 4) noktasından geçtiğine göre k=?

Cevap:  $\frac{21}{2}$

214.  $4x-y+6=0$  doğrusunun  
 $4x-y-2=0$  doğrusuna göre simetriği?

Cevap:  $4x-y-10=0$

215.  $2x-3y+6=0$  doğrusunun  
 $2x-3y+1=0$  doğrusuna göre simetriği?

Cevap:  $2x-3y-4=0$

216.  $2x-y+12=0$  doğrusunun  $2x-y+k$  doğrusuna göre simetriği A(4,2) noktasından geçtiğine göre k=?

Cevap: 3

**217.**  $4x+3y-12=0$  doğrusunun  $Ox$  e göre simetriği?

Cevap:  $4x-3y-12=0$

**218.**  $-4x+3y-48=0$  doğrusunun  $Oy$  ye göre simetriği?

Cevap:  $4x+3y-48=0$

**219.**  $2y-3x+6=0$  doğrusunun  $y=x$  e göre simetriği?

Cevap:  $2x-3y+6=0$

**220.**  $4x-y+16=0$  doğrusunun  $y=-x$  e göre simetriği?

Cevap:  $x-4y+16=0$

**221.**  $4x-y+k=0$  doğrusunun  $y=x$  e göre simetriği  
A(4,1) noktasından geçtiğine göre  $k=?$

Cevap: 0

**222.**  $2x-y+m=0$ . doğrusunun  $y=-x$  e göre simetriği  
A(4,6) noktasından geçtiğine göre  $m=?$

Cevap: 8

**223.**  $2x+3y-12=0$  nin  $x=2$  ye göre simetriği?

Cevap:  $2x-3y+4=0$

**224.**  $4x+3y-12=0$  doğrusunun  $y=6$  ya göre simetriği?

Cevap:  $4x-3y+24=0$

**225.**  $4x-5y+20=0$  doğrusunun  $y=-2$  ye göre simetriği?

Cevap:  $4x+5y+40=0$

**226.**  $4x+5y-20=0$  doğrusunun  $x=6$  ya göre simetriği?

Cevap:  $4x-5y-28=0$

- 227.**  $d_1: 4x+3y-24=0$  doğrusunun  $y=2$  ye göre simetriği  $d_2$  dir.  
 $d_1, d_2$  ve Oy doğruları arasında kalan bölgenin alanı?

Cevap: 27

- 228.**  $y+2x-6=0$  doğrusunun  
 $y-x+1=0$  doğrusuna göre simetriği?

Cevap:  $x+2y-5=0$

- 229.**  $2y-x-4=0$  doğrusunun  
 $x+y-2=0$  doğrusuna göre simetriği?

Cevap:  $2x-y+2=0$

- 230.**  $4x-3y-2=0$  doğrusunun  
 $y-x-2=0$  doğrusuna göre simetriği nedir?

Cevap:  $3x-4y+16=0$

- 231.**  $2x+3y+6=0$  doğrusunun  
 $y+x+6=0$  doğrusuna göre simetriği?

Cevap:  $3x+2y+24=0$

- 232.** A(-2, 6) ve B(10, 4) noktalarına eşit uzaklıktaki noktaların geometrik yer denklemini bulunuz?

Cevap:  $y=6x-19$

- 233.** A(6,2), B(4,-12) noktaları için  $|AB|$  nin orta dikmesi nedir?

Cevap:  $7y+x+30=0$

- 234.** A(1,2) noktasının  $x-y+4=0$  doğrusuna en yakın noktasını bulunuz?

Cevap:  $(-\frac{1}{2}, \frac{7}{2})$

- 235.** A(4,a) noktasının  $2x+y+k=0$  doğrusuna en yakın noktası B(-2, 2) ise a+k=?

Cevap: 7

- 236.** Orjinin  $4x+3y+48=0$  doğrusuna en yakın noktasını bulunuz?

Cevap:  $(-\frac{192}{25}, -\frac{144}{25})$

- 237.** A(4,8) B(8,2) ve C(x,0) noktaları veriliyor.  
 $|AC| + |BC|$  nin en küçük olması için x=?

Cevap:  $\frac{36}{5}$

- 238.** A(-2,12), B(-8,6) ve C(0,y) noktaları veriliyor.  
 $|AC| + |BC|$  nin en küçük olması için y=?

Cevap:  $\frac{54}{5}$

- 239.** A(6,2) B(8,-4) ve C(x,0) noktaları veriliyor.  
 $|AC| + |BC|$  nin en küçük olması için x=?

Cevap:  $\frac{20}{3}$

- 240.** A(12,4), B(8,1) ve C(x,0) noktaları veriliyor.  
 $|AC| - |BC|$  nin en büyük olması için x=?

Cevap:  $\frac{20}{3}$

- 241.** A(-2,12), B(-6,4) ve C(x,0) için  
 $|AC| - |BC|$  nin en büyük olması için x=?

Cevap: -8

- 242.** A(6,2), B(4,6) ve C(0,y) için  
 $|AC| - |BC|$  nin en büyük olması için y=?

Cevap: 14

- 243.**  $x^2+y^2-2xy-16=0$   
 doğruları arasındaki uzaklık kaç br dir?

Cevap:  $4\sqrt{2}$

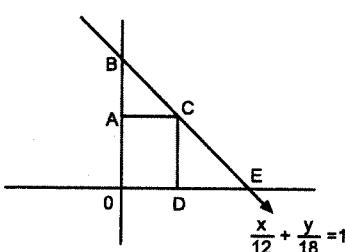
- 244.**  $x^2+2x-y^2+6y-8=0$   
 doğrularının kesim noktası?

Cevap: (-1, 3)

- 245.**  $f(x) = 2x+6$  ise  
 $2[f(x) + f^{-1}(x)]$  in grafiği?

Cevap:  $y=5x+6$ 'nın grafiği

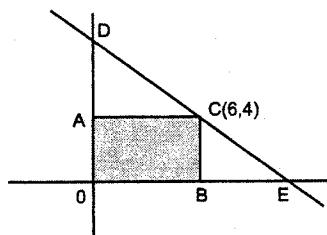
**246.**



AODC  
 dikdörgeninin alanın en  
 büyük değeri?

Cevap: 54

247.



$AOBC$  dikdörtgeninin en büyük alanını aldığı durumda  $[DE]$  doğrusunun denklemi?

Cevap:  $2x+3y-24=0$

248.  $A(1,2)$  ve  $B(m,4)$  noktaları  $2x-y+6=0$  doğrusunun farklı taraflarında ise  $m$  in en büyük tam sayı değeri kaçtır?

Cevap: -2

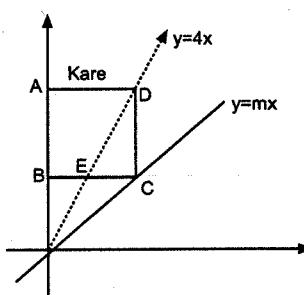
249.  $A(-2, 12)$  ve  $B(4, m)$  noktaları  $3x-4y+12=0$  doğrusun farklı bölgelerinde ise  $m$  in en büyük değeri kaçtır?

Cevap: 5

250.  $3x-4y+24=0$  doğrusu üzerinde olup apsisi ordinatına eşit olan noktayı bulunuz?

Cevap: (24, 24)

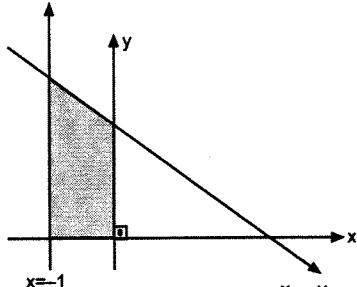
251.



$m = ?$

Cevap: 3

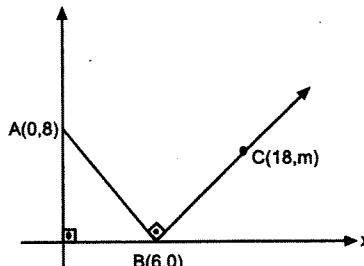
252.



$$T \cdot A = 10 \\ \text{ise} \\ a = ?$$

$d: \frac{x}{a} + \frac{y}{b} = 1$  Cevap:  $\frac{3}{4}$

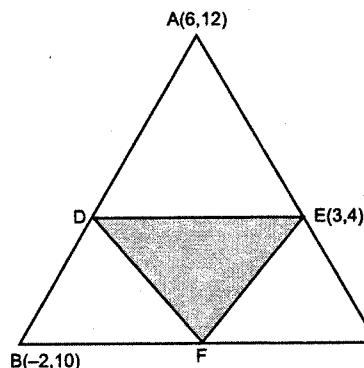
253.



$m = ?$

Cevap: 9

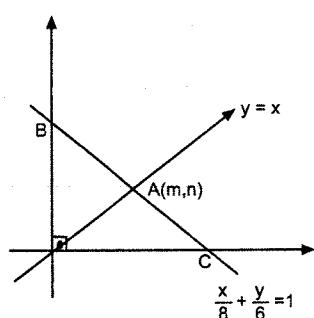
254.



$$D, E, F \text{ noktası ise} \\ T \cdot A = ?$$

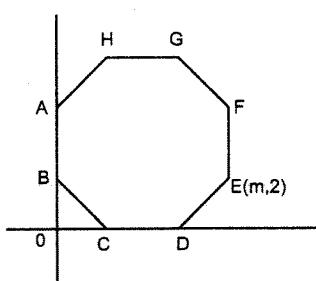
Cevap:  $\frac{29}{2}$

255.



$$(m, n) = ?$$

258.

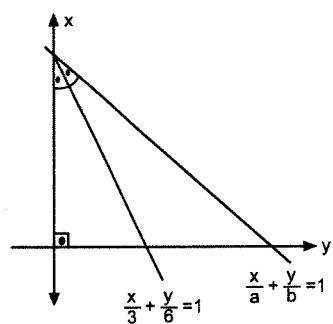


Düzgün  
sekizgen  
 $m = ?$

Cevap:  $4+2\sqrt{2}$

$$\text{Cevap: } \left( \frac{24}{7}, -\frac{24}{7} \right)$$

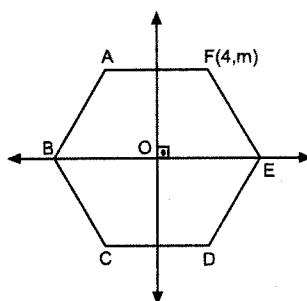
256.



$$a+b = ?$$

Cevap: 14

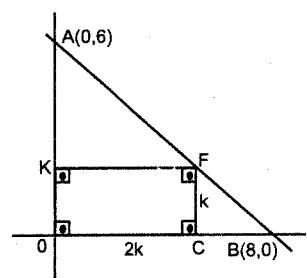
258.



O, düzgün  
altigenin ağırlık  
merkezi  
 $m = ?$

Cevap:  $4\sqrt{3}$

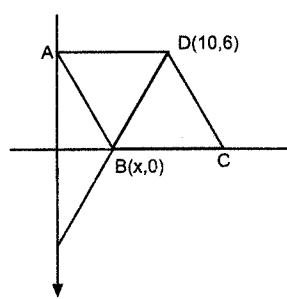
257.



$$\text{Alan(KOFC)} = ?$$

$$\text{Cevap: } \frac{288}{25}$$

259.



ABCD Eşkenar  
dörtgen  
 $x = ?$

Cevap: 8

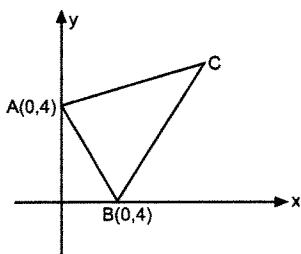
**261.**  $4x - 3y - 12 = 0$

$$3x + 4y + 10 = 0$$

doğrularına eşit uzaklıkta bulunan noktaların geometrik yerlerini bulunuz?

Cevap:  $x - 7y - 22 = 0$   
 $7x + y - 2 = 0$

**262.**



$\text{Alan}(\widehat{ABC})$  sabit kalmak şartıyla C noktalarının geometrik yeri ne olabilir?

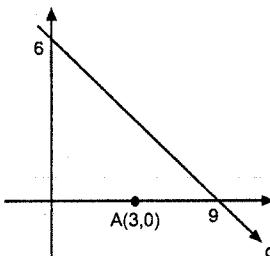
Cevap:  $x + y + m = 0$

**263.**  $y = mx + 6$  doğrusu  $Ox$  i A da  $Oy$  yi B de kesiyor.

C de  $Ox$  eksenü üzerinde ve  $\text{Alan}(\widehat{ABC}) = 24$  ise  $C(x, 0)$  noktalarının apsisleri farkı kaçtır?

Cevap: 16

**264.**



A noktasının d doğrusu üzerindeki en yakın noktasına olan uzaklığı kaç br dir?

Cevap:  $\frac{12}{\sqrt{13}}$

**265.**  $|x| + |y| \leq 3$

eşitsizliğini sağlayan A(x, y) tamsayı ikilileri kaç tanedir?

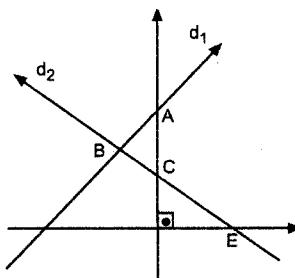
Cevap: 25

**266.**  $|x+y| \leq 4$

eşitsizliğini sağlayan ve eksenler üzerinde olan koordinatları tamsayı olan kaç nokta vardır?

Cevap: 17

**267.**

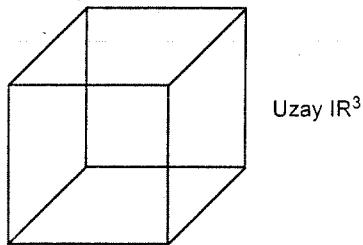


ABC eşkenar

$$m_1 + m_2 = ?$$

Cevap: 0

# UZAY GEOMETRİ

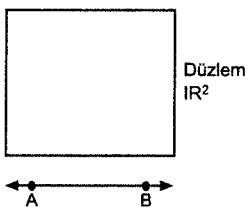


**Nokta:** Boyutsuzdur.

**Doğru:** Bir boyutludur.

**Düzlem:** İki boyutlu ( $\text{IR}^2$ ) Alan belirtir.

**Uzay:** Üç boyutludur ( $\text{IR}^3$ ) Hacim belirtir.



**$\text{IR}^2$  de**

- I. İki doğru birbirine平行 olabilir.
- II. İki doğru kesişebilir.
- III. Çakışık olabilir.

**$\text{IR}^3$  te**

- İki doğru paralel olabilir.
- İki doğru kesişebilir.
- Birbirile kesişmeyen ve paralel olmayan iki doğru aykırı doğrular olabilirler.

## Düzlem Belirtme Şartları

- Doğrusal olmayan üç nokta bir düzlem belirtir.
- Bir doğru ile dışındaki bir nokta bir düzlem belirtir.
- Kesişen iki doğru bir düzlem belirtir.
- Paralel iki doğru bir düzlem belirtir.

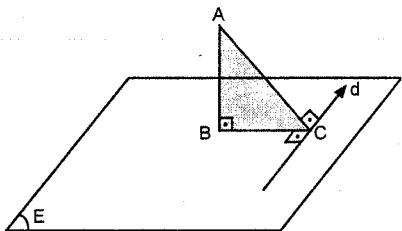
## Doğru ile Düzlem arasındaki İlişki

- Doğru ile düzlemin ortak iki noktası varsa, doğru düzlem içindedir.
- Doğru ile düzlemin ortak bir noktası varsa doğru düzlemi keser.
- Doğru ile düzlemin ortak noktaları yoksa doğru düzleme paraleldir.
- Uzayda veya düzlemede bir doğuya dışındaki bir noktadan ancak bir paralel doğru çizilebilir.
- Uzayda veya düzlemede aynı doğuya paralel olan doğrular birbirine paraleldir.
- Uzayda paralel iki doğrudan birini kesen doğru diğerini kesmeyebilir. Düzlemede paralel iki doğrudan birini kesen doğru diğerini keser.
- Uzayda bir doğuya üzerindeki bir noktadan sonsuz tane, düzlemede ise bir doğuya üzerindeki bir noktadan bir tane dik doğru çizilir.
- Uzayda paralel iki doğrudan birine dik olan bir doğru diğerine ya diktir ya da dik durumluudur.
- Bir doğrudan sonsuz tane düzlem geçer.
- Bir doğru bir düzleme dik ise, doğrunun düzleme dik olduğu noktadan geçen düzlem içindeki her doğuya diktir.
- Aykırı doğrular vardır fakat aykırı düzlem diye bir şey yoktur.
- $\text{R}^2$  de farklı iki noktaya eşit uzaklıktaki noktalar kümesine kenar orta dikme denir.
- $\text{R}^3$  te farklı iki noktaya eşit uzaklıktaki noktalar kümesine orta dikme düzlemi denir.

## Uzay Belirtme Şartları

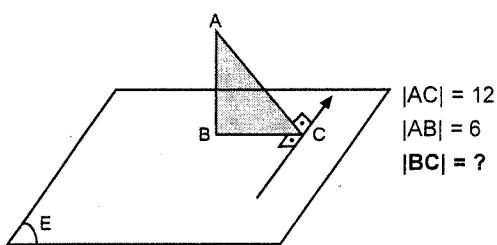
- Paralel iki düzlem
- Kesişen iki düzlem
- Bir düzlem ve dışındaki bir nokta
- Aynı düzlem içinde olmayan dört nokta UZAY belirtir.

## ÜÇ DİKME TEOREMİ



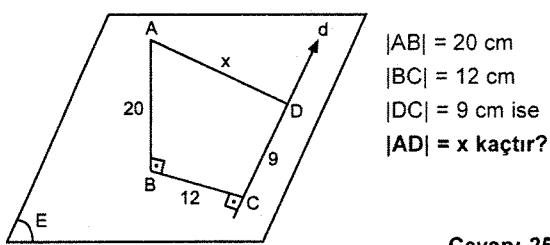
Şekilde E düzlemini ve düzlemin içindeki d doğrusuna A noktasından indirilen dikmeler Düzleme B, doğruya C noktasında kesmektedir. Bu durumda:  $[AC] \perp d$ ,  $[AB] \perp (E)$  ise  $[BC] \perp d$  olur. Bu üç dikmenin herhangi ikisi verilirse diğeride gönül rahatlığı ile dik yazılır.

**Örnek:**



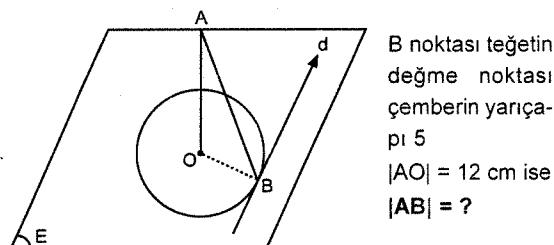
Cevap:  $6\sqrt{3}$

**Örnek:**



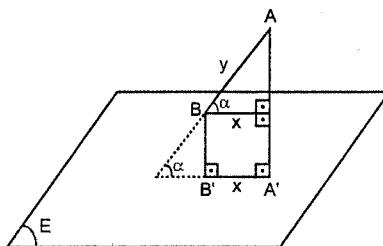
Cevap: 25

**Örnek:**



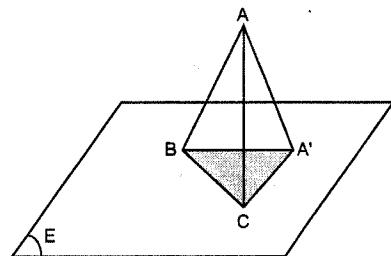
Cevap: 13

Bir doğrunun bir düzlemdeki izdüşümü ile yaptığı dar açıya doğru ile düzlem arasındaki açı denir.



$|AB|$  nin dik izdüşümü  $|A'B'|$  dur.  $[AB]$  ile E düzlemini arasındaki açı  $\alpha$  dir.

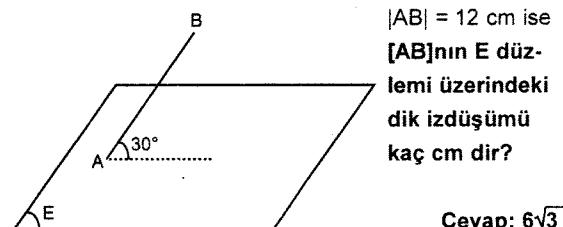
$$\cos\alpha = \frac{x}{y} \Rightarrow |AB| \cdot \cos\alpha = |A'B'|$$



ABC üçgeninin E düzlemini üzerindeki dik izdüşümü A'BC üçgenidir.

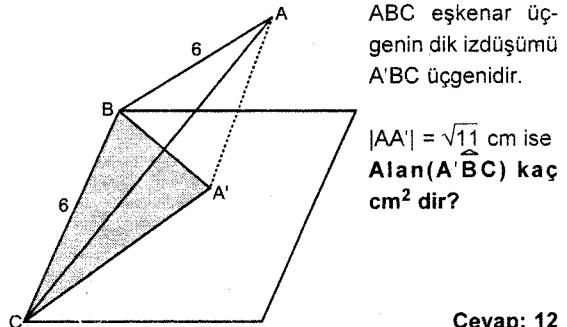
$\text{Alan}(ABC) \cdot \cos\alpha = \text{Alan}(A'BC)$  dir.

**Örnek:**



Cevap:  $6\sqrt{3}$

**Örnek:**



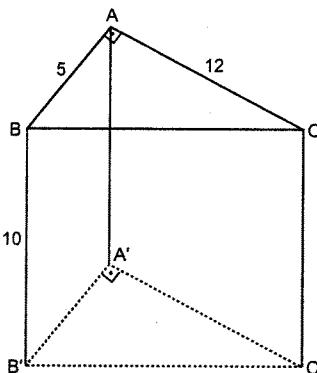
Cevap: 12

# PRİZMA

## Dik Prizma:

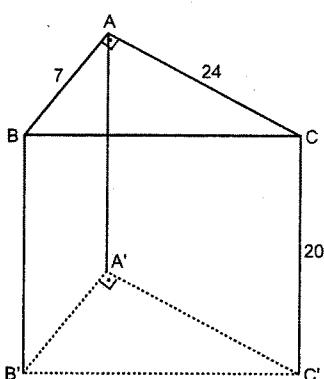
Yanal aynırıları taban düzlemine dik olan prizmaya dik prizma denir.

- Tabanı üçgen olan dik Prizma, üçgen dik Prizma diye okunur.
- Tabanı kare olan dik Prizma kare dik Prizma diye okunur.
- Tabanı düzgün altigen olan dik Prizma Düzgün altigen dik Prizma diye okunur.
- Taban çevresi çarpı yükseklik Yanal Alanıdır.
- Bütün Prizmaların hacimleri taban alanı çarpı yüksekliktir.
- $Y.A = \text{Yanal Alan}$  demektir.



Hacim = ?  
Y. Alan = ?  
Bütan Alan = ?

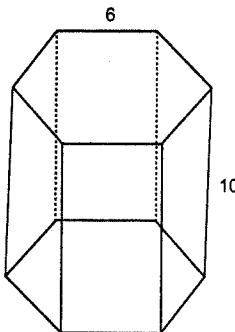
Cevap: V = 300  
Y.A = 300  
Alan = 360



a) Bütan Alan = ?  
b) V = ?

Cevap: a = Alan = 1288  
b) V = 1680

## Örnek:

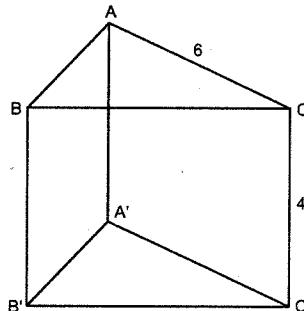


### Düzgün Altigen Dik Prizma

- a) Yanal Alan = ?  
b) Bütan Alan = ?  
c) Hacim = ?

Cevap: a) 360  
b)  $360 + 108\sqrt{3}$   
c)  $540\sqrt{3}$

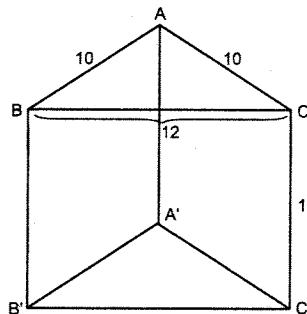
## Örnek:



ABC eşkenar üçgen  
Üçgen dik Prizma  
 $V = ?$

Cevap:  $36\sqrt{3}$

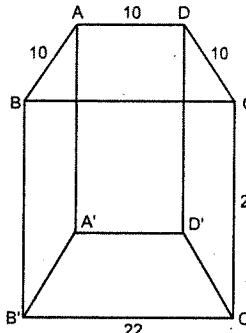
## Örnek:



$V = ?$   
Y.A = ?  
Tüm Alan = ?

Cevap: a) V = 480  
b) Y.A = 320  
c) Tüm Alan: 416

## Örnek:



$V = ?$

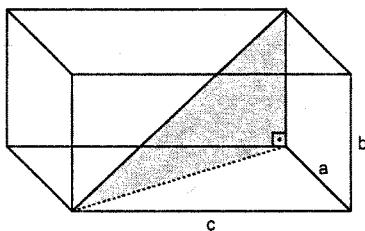
Cevap: 2560

## DİKDÖRTGENLER PRİZMASI

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$a, b, c$  ayrıtlar olmak üzere;

$$V = \text{Hacim} = a.b.c$$

$$\text{Alan} = 2ab + 2bc + 2ac$$

- Yüzey köşegenleri farklı dikdörtgenlerin köşegen uzunluklarıdır.
- Cisim köşegeni  $\sqrt{a^2 + b^2 + c^2}$

$$(a + b + c)^2 = a^2 + b^2 + c^2 + 2ab + 2bc + 2ac$$

$$\Rightarrow (a + b + c)^2 = (\text{cisim köşegeninin karesi}) + \text{Alan}$$

**Örnek:**

Bir dikdörtgenler prizmasının ayrıtları 2, 3 ve 5 sayıları ile orantılıdır. Hacmi  $810 \text{ cm}^3$  ise Alanı kaç  $\text{cm}^2$  dir?

**Cevap: 558**

**Örnek:**

Ayrıtları 5, 10, 15 cm olan bir dikdörtgenler prizmasının cisim köşegeni kaç cm dir?

**Cevap:  $5\sqrt{14}$**

**Örnek:**

Alanı  $400 \text{ cm}^2$  ve cisim köşegeninin uzunluğu 15 cm olan dikdörtgenler prizmasının ayrıtları toplamı kaç cm dir?

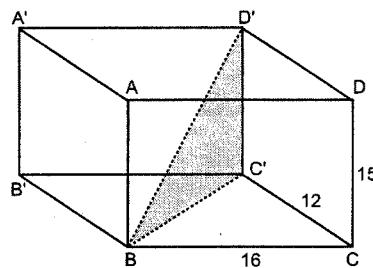
**Cevap: 25**

**Örnek:**

Bir dikdörtgenler prizmasının farklı yüzeylerinin alanları sırasıyla  $12, 18, 24 \text{ cm}^2$  ise prizmanın hacmi kaç  $\text{cm}^3$  tür?

**Cevap: 72**

**Örnek:**



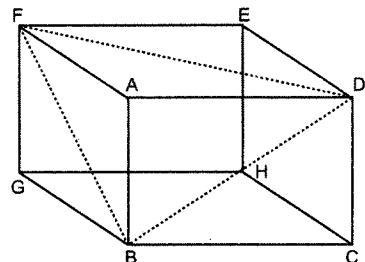
$$\text{A) Alan } (\widehat{B'C'D'}) = ?$$

$$\text{B) } \hat{\triangle}(B'C'D') = ?$$

**Cevap: A → 150**

**B → 60**

**Örnek:**



$$|FB| = 8 \text{ cm}$$

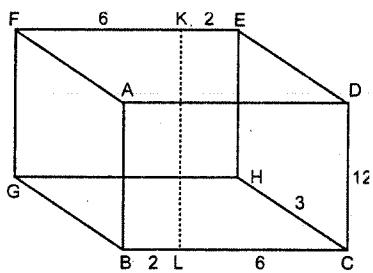
$$|BD| = 5 \text{ cm}$$

$$|FD| = 7 \text{ cm} \text{ ise}$$

cisim köşegenin uzunluğu kaç cm dir?

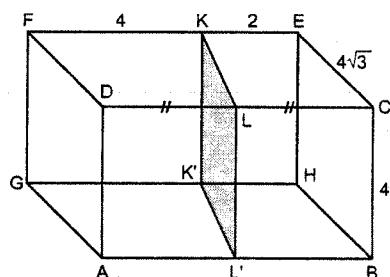
**Cevap:  $\sqrt{69}$**

Örnek:



Cevap: 13

Örnek:

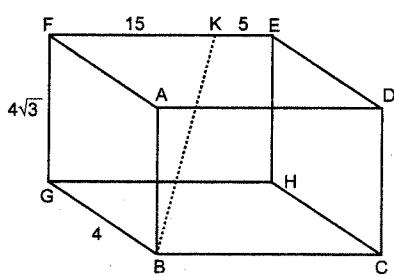


$$|KE| = |K'H|$$

KLL'K' dikdörtgeninin alanı kaç  $\text{cm}^2$  dir?

Cevap: 28

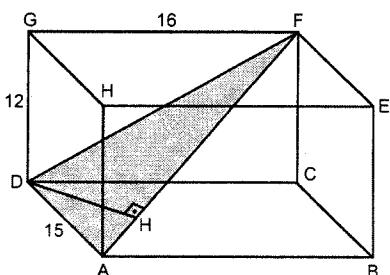
Örnek:



$$|BK| = ?$$

Cevap: 17

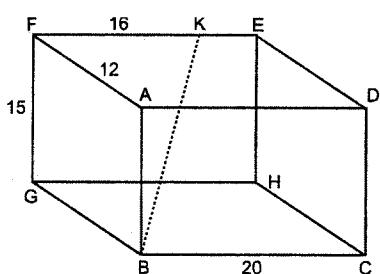
Örnek:



$$|DH| = ?$$

Cevap: 12

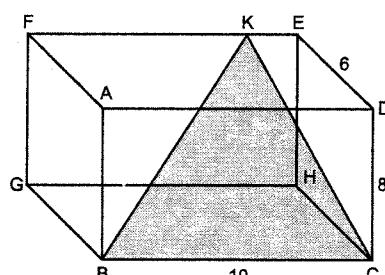
Örnek:



$$|BK| = ?$$

Cevap: 25

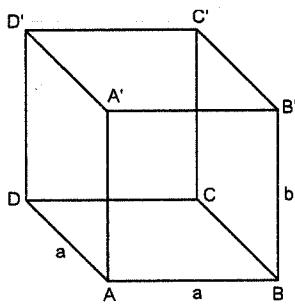
Örnek:



Taralı Alan kaç  $\text{cm}^2$  dir?

Cevap: 50

## KARE DİK PRİZMA



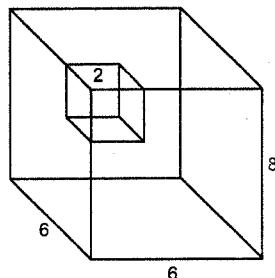
ABCD kare

$$V = a^2 \cdot b$$

$$\text{Alan: } 2.(a.a + a.b + a.b) = 2(a^2 + 2ab)$$

$$\text{Cisim Köşegeni: } \sqrt{a^2 + a^2 + b^2} = \sqrt{2a^2 + b^2}$$

Örnek:



Kare dik Prizma şeklindeki bir cisimden bir ayırtı 2 cm olacak şekilde bir küp çıkartılıyor.

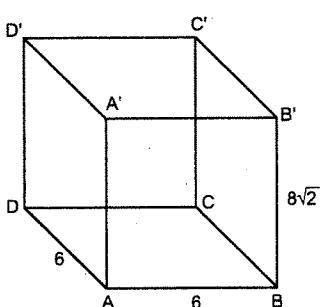
a) Yeni Şeklin Alanı?

b) Yeni Şeklin Hacmi?

Cevap: Alanı Değişmez (264)

Hacmi: 280

Örnek:



Cisim Köşegeni = ?

V = ?

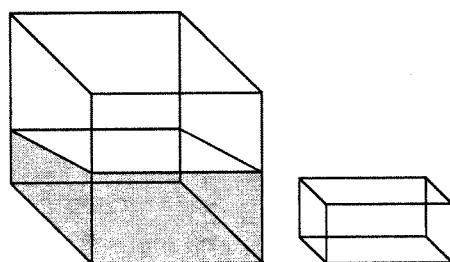
Alanı = ?

Cevap: C.K =  $10\sqrt{2}$

$V = 288\sqrt{2}$

Alanı =  $19\sqrt{2} + 72$

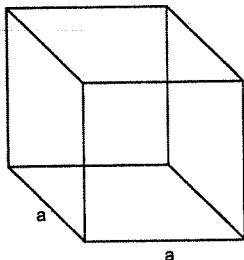
Örnek:



Bir ayırtının uzunluğu 6 cm ve yüksekliğinin yarısına kadar su dolu bir kübün içine ayırtları 2,2, 3 cm olacak şekilde bir kare-dik prizma atılıyor. Suyun yüksekliği kaç cm olur?

Cevap:  $\frac{10}{3}$

# KÜP



$$V = a^3$$

$$\text{Alan} = 6a^2$$

$$\text{Yüzey köşegeni} = a\sqrt{2}$$

$$\text{Cisim köşegeni} = a\sqrt{3}$$

Örnek:

Bir ayrıtının uzunluğu 4 cm olan küpün hacminin, alanı ve cisim köşegenini bulunuz?

$$\text{Cevap: } V = 64$$

$$\text{Alan} = 96$$

$$\text{C.k} = 4\sqrt{3}$$

Örnek:

Alanı sayıca hacmine oranı  $\frac{2}{3}$  olan bir kübün yüzey köşegeni?

$$\text{Cevap: } 9\sqrt{2}$$

Örnek:

Bir kübün ayrıtlarını 3 cm artırdığımızda hacmi  $216 \text{ cm}^3$  oluyor, ayrıtlarını 1 cm küçülttüğümüzde hacmi kaç  $\text{cm}^3$  olur?

$$\text{Cevap: } 8$$

Örnek:

Ayrıtları 2, 4 ve 8 cm olan bir dikdörtgenler prizmasının hacmine eşit olan bir kübün alanı kaç  $\text{cm}^2$  dir?

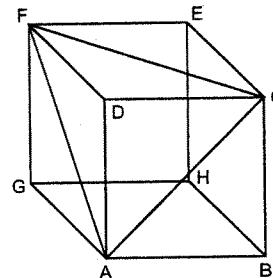
$$\text{Cevap: } 96$$

Örnek:

Bir kübün hacminden-alanını çıkardığımızda bir ayrıtinin 7 katı çıkarıyor.

Bu kübün cisim köşegeni kaçtır?

$$\text{Cevap: } 7\sqrt{3}$$

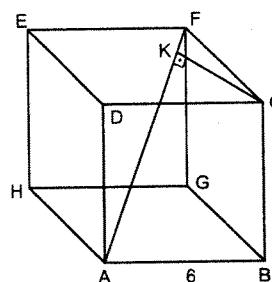


Örnek:

Küp

$$\text{Alan}(AFC) = ?$$

$$\text{Cevap: } 18\sqrt{3}$$

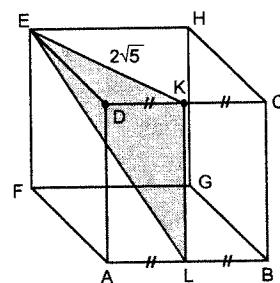


Örnek:

Küp

$$|KC| = ?$$

$$\text{Cevap: } 2\sqrt{6}$$



Örnek:

Küp

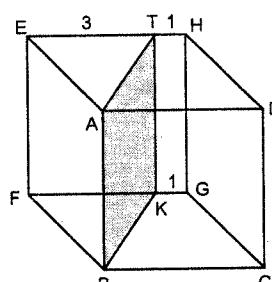
$$|DK| = |KC|$$

$$|AL| = |LB|$$

$$|EK| = 2\sqrt{5}$$

$$|EL| = ?$$

$$\text{Cevap: } 6$$



Örnek:

Küp

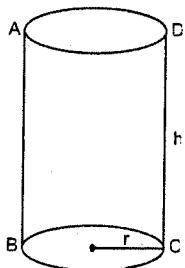
$$|TH| = |KG| = 1 \text{ cm}$$

$$|ET| = 3 \text{ cm ise}$$

$$\text{Alan}(ABKT) = ?$$

$$\text{Cevap: } 20$$

# SİLİNDİR



Tabanı daire olan Prizmaya Silindir denir.

Hacim: Taban Alanı x Yükseklik

$$V = \pi r^2 \cdot h$$

$$\text{Yanal Alan} = 2\pi r \cdot h$$

$$\text{Tüm Alan} = 2\pi r^2 + 2\pi r h$$

Örnek:

Taban yarıçapı 3 cm, yüksekliği 4 cm olan dik silindirin Hacmini bulunuz?

Cevap:  $36\pi$

Örnek:

Yanal Alanının hacmine oranı  $\frac{1}{3}$  olan silindirin yarıçapı kaçtır?

Cevap: 6

Örnek:

Hacmi  $216\pi$ , Yanal Alanı  $144\pi$  olan dik silindirin Tüm Alanı kaç  $br^2$  dir?

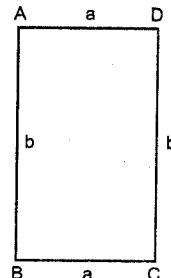
Cevap:  $162\pi$

Örnek:

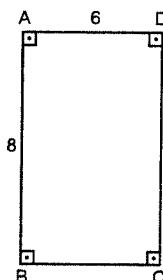
Yüksekliği, taban yarıçapının 3 katı olan bir dik silindirin tüm alanı  $128\pi$  ise bu silindirin hacmi kaç  $br^3$  tür?

Cevap:  $192\pi$

NOT:



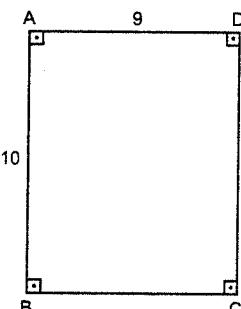
ABCD dikdörtgenini [AB] etrafında  $360^\circ$  döndürsek yarıçapı a, yüksekliği b olan bir dik silindir elde ederiz.  $180^\circ$  döndürürsek yarınl silindir,  $90^\circ$  döndürürsek silindirin dörtte birini elde ederiz.



Örnek:

Yandaki dikdörtgeni [AB] etrafında  $360^\circ$  döndürürsek elde edilen cismin hacmi kaç  $cm^3$  olur?

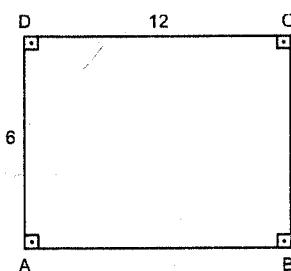
Cevap:  $288\pi$



Örnek:

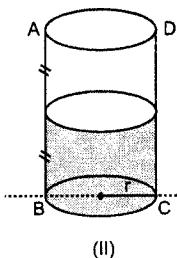
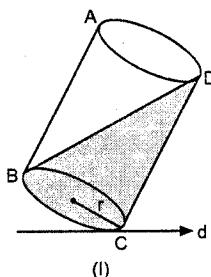
Yandaki dikdörtgeni [AB] etrafında  $360^\circ$  döndürürsek elde edilen cismin hacmi kaç  $cm^3$  olur?

Cevap:  $810\pi$



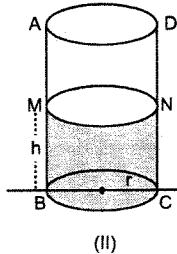
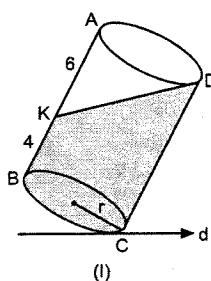
Örnek:

Yandaki dikdörtgeni [AB] etrafında  $180^\circ$  döndürürsek elde edilen cismin hacmi kaç  $\text{cm}^3$  olur?

Cevap:  $432\pi$ 

Şekilde I deki gibi silindirin içindeki suyu dipteki B köşesini görünceye kadar boşaltıp, Şekil II deki gibi düzeltirsek suyun yarısını boşaltmış oluruz.

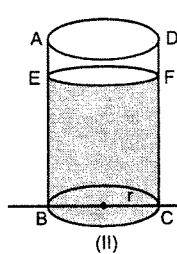
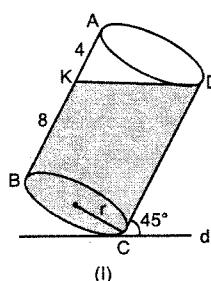
Örnek:



Şekil I, Şekil II ye geldiğinde suyun yüksekliği (h) kaç cm olur?

Cevap: 7

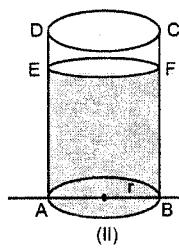
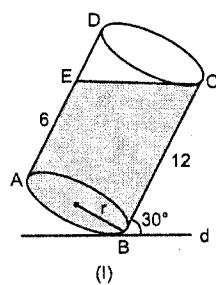
Örnek:



Şekil I, Şekil II ye geldiği zaman silindirdeki suyun hacmi kaç  $\text{cm}^3$  olur?

Cevap:  $40\pi$ 

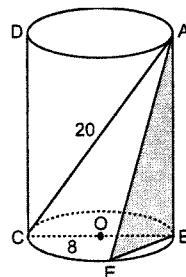
Örnek:



Şekil I, Şekil II ye getirildiğinde silindirdeki suyun hacmi kaç  $\text{cm}^3$  olur?

Cevap:  $27\pi$ 

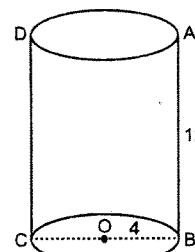
Örnek:



$$\begin{aligned} A(\widehat{ABE}) &= ? \\ |AC| &= 20 \text{ cm} \\ |BE| &= 5 \text{ cm} \end{aligned}$$

Cevap: 30

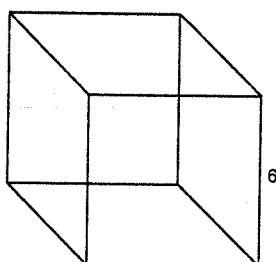
Örnek:



Şekildeki silindirin içine yerleştirilebilecek en büyük kare dik prizmanın hacmi kaç  $\text{cm}^3$  tür?

Cevap: 384

Örnek:



Şekildeki bir kenarı 6 cm olan kübüne içerişine en büyük hacimli yarıçapı 1 cm olan en çok kaç silindir yerleştirilebilir?

Cevap: 9

Örnek:

Bir kenarı 4 cm olan küp içerisinde en büyük hacimli bir silindir yerleştiriliyor. Bu silindirin yanal alanı kaç  $\text{cm}^2$  dir?

Cevap:  $16\pi$ 

Örnek:

Bir kenarı 6 cm olan düzgün altıgen dik prizmanın içerisinde en büyük hacimli bir silindir yerleştiriliyor.

Bu prizmanın hacmi  $216\sqrt{3} \text{ cm}^3$  ise silindirin hacmi kaç  $\text{cm}^3$  tür?

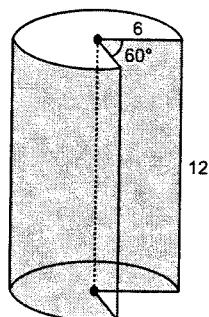
Cevap:  $108\pi$ 

Örnek:

Yarıçapı 4 cm olan bir dik silindirin hacmi  $96\pi \text{ cm}^3$  ise bu silindirin içerisinde yerleştirilebilecek en büyük düzgün altıgen dik prizmanın hacmi kaç  $\text{cm}^3$  olur?

Cevap:  $144\sqrt{3}$ 

Örnek:



Şekildeki cismin hacmi kaç  $\text{cm}^3$  tür?

Cevap:  $360\pi$ 

Örnek:

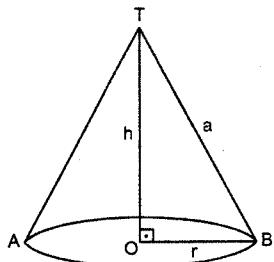
Bir dik silindir biçimindeki cismin tamamı su ile doludur. Suyun  $20 \text{ cm}^3$  ü boşaltılırsa su yüksekliği 1,5 cm azalıyor. 50  $\text{cm}^3$  daha boşaltılırsa su yüksekliği silindirin yarısına geliyor.

Silindirin yüksekliği kaç cm dir?

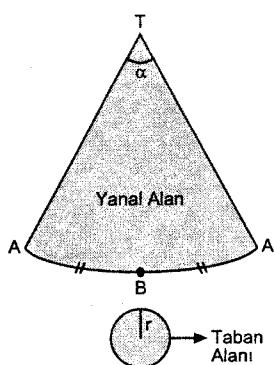
Cevap:  $\frac{21}{2}$

# KONİ

Tabanı daire olan ve yüksekliği taban merkezi olan cisimde dik KONİ denir.



a → Ana doğru  
h → Yükseklik  
r → Taban yarıçapı  
(Dik Koni)



$$\text{Yanal Alan} = \pi \cdot r \cdot a$$

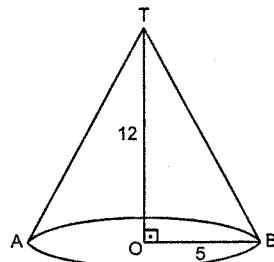
$$\text{Taban Alanı} = \pi \cdot r^2$$

$$\text{Tüm Alanı} : \pi r^2 + \pi \cdot r \cdot a$$

$$\text{Hacim} = V = \frac{1}{3} \pi r^2 \cdot h$$

$$\frac{\alpha}{360^\circ} = \frac{r}{a}$$

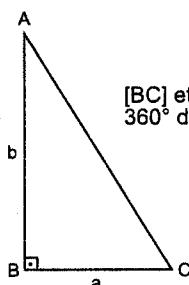
Örnek:



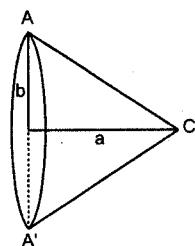
- a)  $\text{Y.A} = ?$   
b) Tüm Alanı  
c) Hacmi

Cevap: a)  $65\pi$   
b)  $90\pi$   
c)  $100\pi$

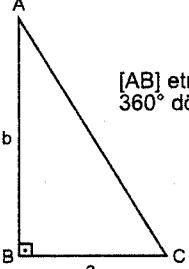
I.



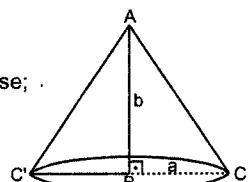
[BC] etrafında  $360^\circ$  döndürülürse;



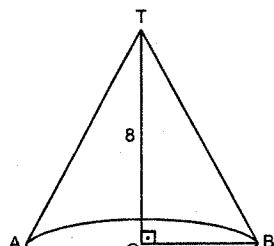
II.



[AB] etrafında  $360^\circ$  döndürülürse;



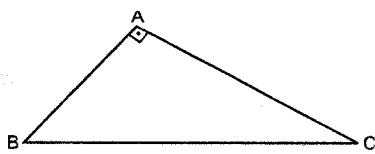
Örnek:



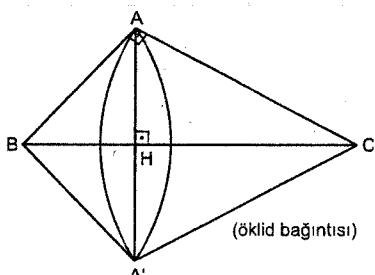
- a) Yanal Alanı  
b) Tüm Alanı  
c) Hacmi  
d) Açılımındaki merkez açı

Cevap: a)  $60\pi$   
b)  $96\pi$   
c)  $96\pi$   
d)  $216^\circ$

III.

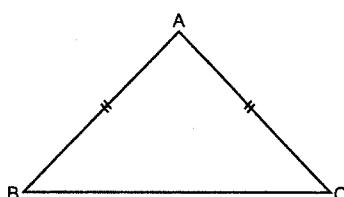


Hipotenüs  
etrafında  
 $360^\circ$   
döndürülürse;

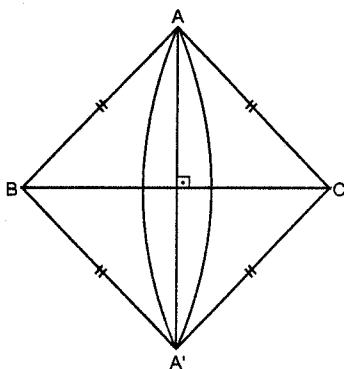


(öklid bağıntısı)

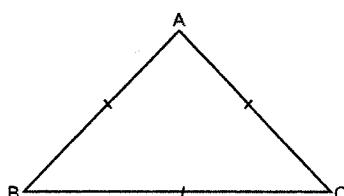
IV.



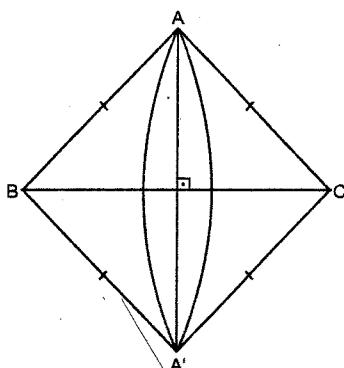
[BC] etrafında  
 $360^\circ$   
döndürülürse;



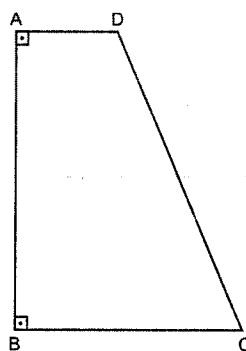
V.



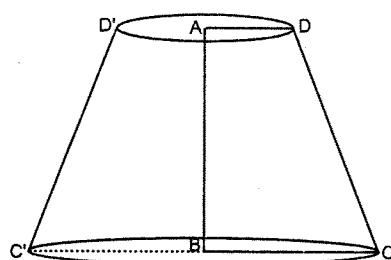
ABC eşkenar üç-  
geni herhangi bir  
kenarı etrafında  
 $360^\circ$  döndürülür-  
se;



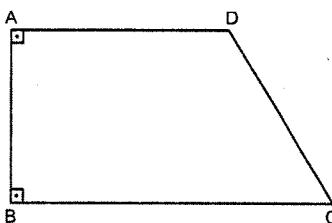
VI.



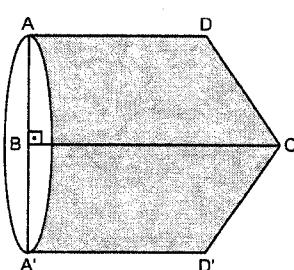
ABC dik yamuğu  
[AB] etrafında  
 $360^\circ$  döndürülürse;



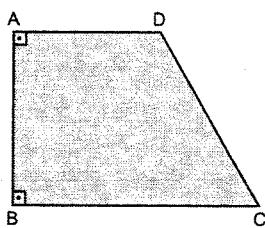
VII.



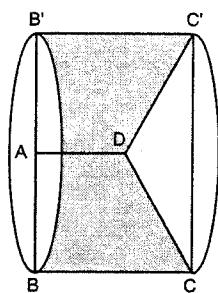
[BC]  
etrafında  
 $360^\circ$  döndü-  
rülürse;



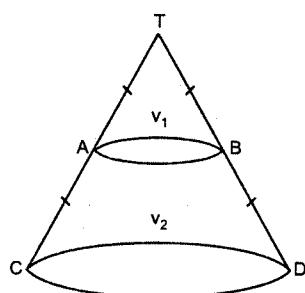
VIII.



[AD] etrafında  
360° döndürülürse,



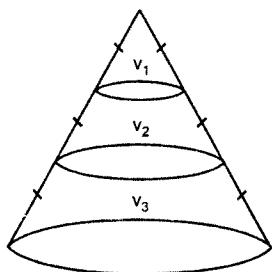
IX.



$$\frac{v_1}{v_1 + v_2} = \left(\frac{1}{2}\right)^3 = \frac{1}{8} \quad v_1 = 1$$

$$v_2 = 7$$

\*

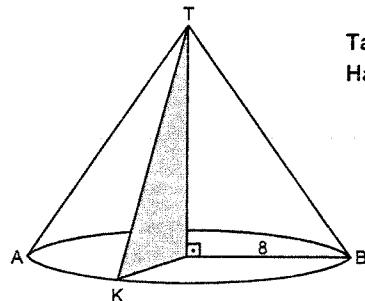


$$v_1 = 1$$

$$v_2 = 7 \quad \frac{v_1}{v_1 + v_2 + v_3} = \left(\frac{1}{3}\right)^3 = \frac{1}{27}$$

$$v_3 = 19$$

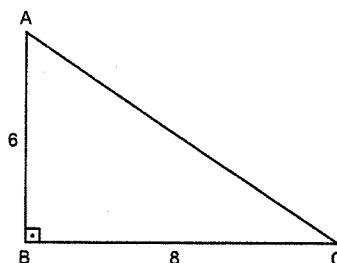
Örnek:



Taralı Alan = 60 cm<sup>2</sup>  
Hacim = ?

Cevap:  $320\pi$

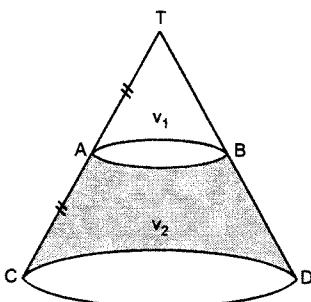
Örnek:



[AB] etrafında  
360° döndürülürse  
oluşan şeklin hac-  
mi kaç cm<sup>3</sup> tür?

Cevap:  $128\pi$

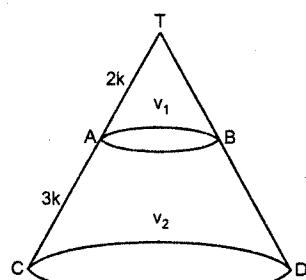
Örnek:



$v_2 = 49\text{cm}^3 \Rightarrow v_1$   
kaç cm<sup>3</sup> tür?

Cevap: 7

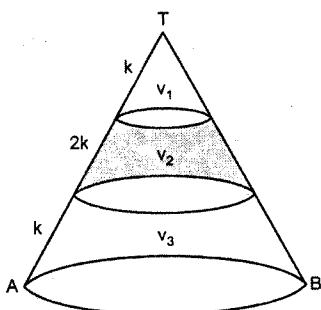
Örnek:



$$\frac{v_1}{v_2} = ?$$

Cevap:  $\frac{8}{117}$

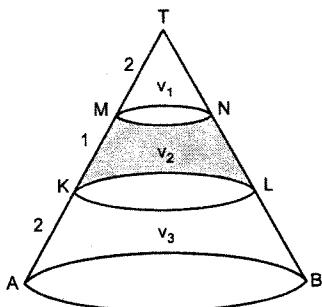
Örnek:



$$\frac{v_3 - v_1}{v_2} = ?$$

Cevap:  $\frac{18}{13}$ 

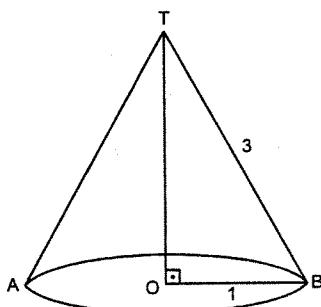
Örnek:



$$\frac{v_1 + v_3}{v_2} = ?$$

Cevap:  $\frac{106}{19}$ 

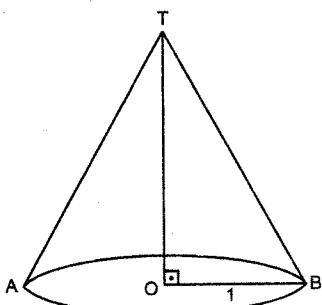
Örnek:



Şekildeki dik koniyi açtığımız zaman oluşacak daire diliminin merkez açısı kaç derece olur?

Cevap:  $120^\circ$ 

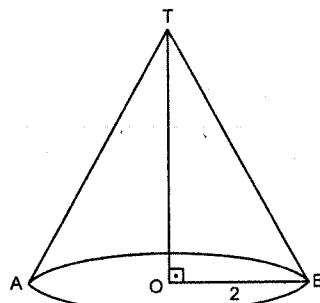
Örnek:



Şekildeki dik koninin yanal alanı  $4\pi$  ise bu koninin açılımındaki merkez açı kaç derecedir?

Cevap:  $90^\circ$ 

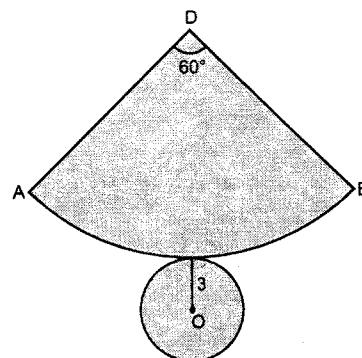
Örnek:



Şekildeki dik koninin hacmi  $\frac{4\sqrt{21}\pi}{3}$   $\text{cm}^3$  ise bu koninin açılımındaki merkez açı kaç derecedir?

Cevap:  $144^\circ$ 

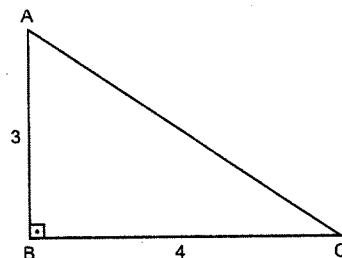
Örnek:



Şekilde görülen bir dik koninin açık şeklidir. Bu koninin yüksekliği kaç cm dir?

Cevap:  $3\sqrt{35}$ 

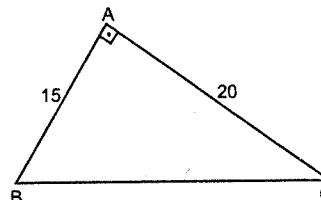
Örnek:



Şekildeki dik üçgenin [AB] etrafında  $360^\circ$  döndürülürse oluşan yeni şeklin hacmi kaç  $\text{cm}^3$  tür?

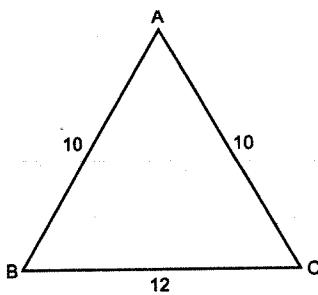
Cevap:  $16\pi$ 

Örnek:



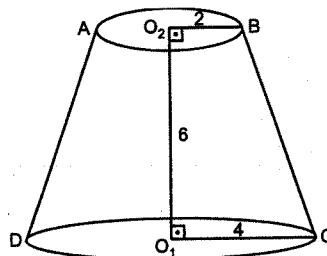
Şekildeki dik üçgenin hipotenüs etrafında  $360^\circ$  döndürsek oluşan şekil hacmi kaç  $\text{cm}^3$  tür?

Cevap:  $1200\pi$



Örnek:

Şekildeki ikizkenar üçgenin  $[BC]$  etrafında  $360^\circ$  döndürülmesi ile oluşan yeni şeklin hacmi kaç  $\text{cm}^3$  tür?

Cevap:  $256\pi$ 

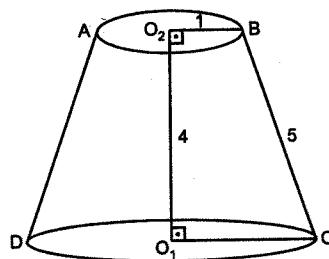
Örnek:

Şekildeki kesik koninin hacmi kaç  $\text{cm}^3$  tür?

Cevap:  $56\pi$ 

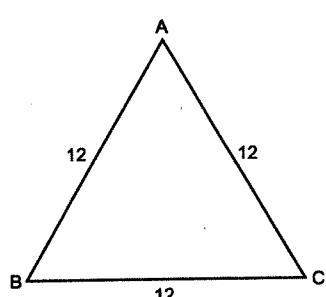
Örnek:

Yanal Alanı  $175\pi$ , Tüm Alanı  $224\pi$  olan bir dik koninin Hacmi kaç  $\text{cm}^3$  tür?

Cevap:  $392\pi$ 

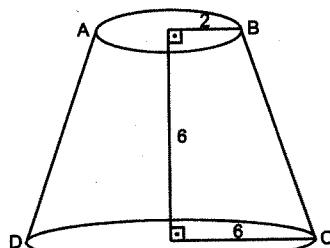
Örnek:

Şekildeki kesik koninin hacmi kaç  $\text{cm}^3$  tür?

Cevap:  $28\pi$ 

Örnek:

ABC eşkenar üçgenin herhangi bir kenarının etrafında  $360^\circ$  döndürürsek oluşan yeni şeklin hacmi kaç  $\text{cm}^3$  tür?

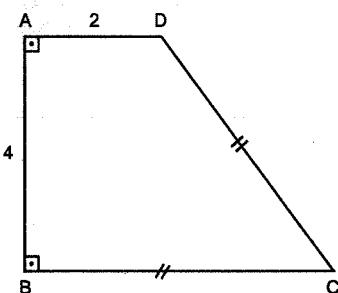
Cevap:  $432\pi$ 

Örnek:

Şekildeki kesik koninin hacmi kaç  $\text{cm}^3$  tür?

Cevap:  $104\pi$

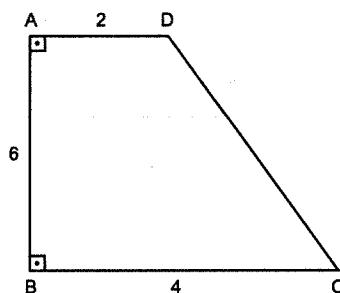
Örnek:



Şekildeki dik ya-  
muğu [AB] etra-  
fında  $360^\circ$  döndü-  
rürsek oluşacak  
cismin hacmi kaç  
 $\text{cm}^3$  olur?

Cevap:  $52\pi$ 

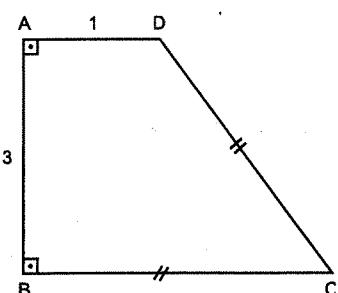
Örnek:



Şekildeki dik ya-  
muğu [BC] etra-  
fında  $360^\circ$  döndü-  
rürsek oluşacak  
şeklin hacmi kaç  
 $\text{cm}^3$  olur?

Cevap:  $96\pi$ 

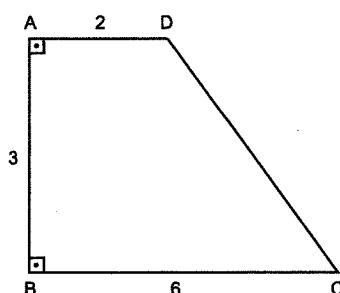
Örnek:



Şekildeki dik ya-  
muğu [AB] etra-  
fında  $360^\circ$  döndü-  
rürsek oluşan ye-  
ni şeklin hacmi  
kaç  $\text{cm}^3$  olur?

Cevap:  $31\pi$ 

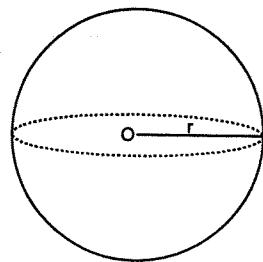
Örnek:



Şekildeki dik ya-  
muğu [AD] etra-  
fında  $360^\circ$  döndü-  
rürsek oluşacak  
yeni şeklin hacmi  
kaç  $\text{cm}^3$  olur?

Cevap:  $42\pi$

## KÜRE



Kürenin hacmi:  $\frac{4}{3}\pi r^3$

Kürenin Alanı:  $4\pi r^2$

Küre: Uzayda sabit bir noktaya eşit uzaklıklarda noktalar kümesine denir.

**Örnek:**

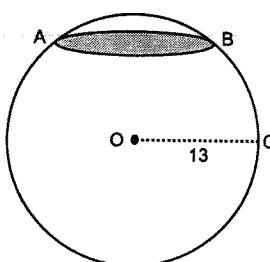
Yarıçapı 3 cm olan kürenin hacmi kaç  $\text{cm}^3$  tür?

Cevap:  $36\pi$

**Örnek:**

Yarıçapı 4 cm olan kürenin alanı kaç  $\text{cm}^2$  dir?

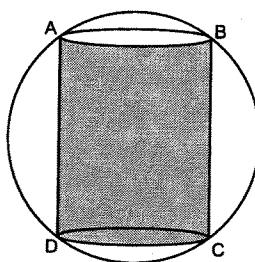
Cevap:  $64\pi$



**Örnek:**

Şekildeki kürenin yarıçapı 13 cm ve [AB] çaplı daire diliminin alanı  $25\pi$  ise kürenin merkezinin Taralı kesite olan uzaklıği kaç cm dir?

Cevap: 12

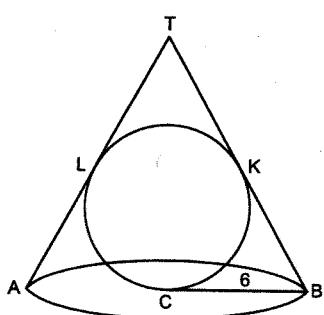


**Örnek:**

Şekildeki kürenin içerisine en büyük hacimli bir silindir yerleştirilmiştir.

Kürenin yarıçapı 10 cm silindirin yarıçapı 6 cm ise silindirin hacmi kaç  $\text{cm}^3$  tür?

Cevap:  $576\pi$



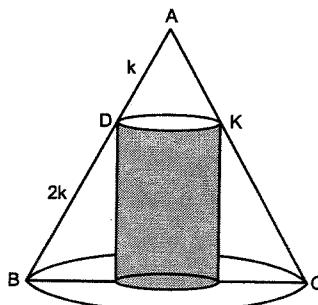
**Örnek:**

Şekildeki dik koninin içinde en büyük hacimli bir küre yerleştirilmiştir.

$$|BC| = 6 \text{ cm}$$

$|TB| = 10 \text{ cm}$  ise bu kürenin hacmi kaç  $\text{cm}^3$  tür?

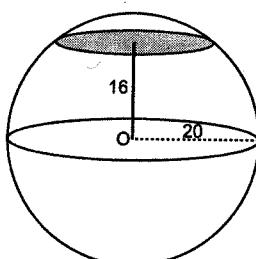
Cevap:  $36\pi$



**Örnek:**

Şekildeki koninin hacminin, içerisinde yerleştirilen silindirin hacmine oranı kaçtır?

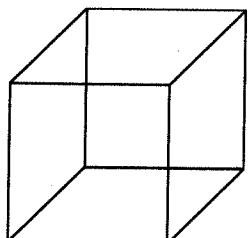
Cevap:  $\frac{9}{2}$



**Örnek:**

Yarıçapı 20 cm olan kürenin merkezinden 16 cm uzaklıkta bulunan bir düzleme kesiliyor. Bu kesitin alanı kaç  $\text{cm}^2$  dir?

Cevap:  $144\pi$



**Örnek:**

Şekildeki bir ayrıtı 6 cm olan küpün içerisinde en büyük hacimli silindir yerleştiriliyor. Silindirin hacmi kaç  $\text{m}^3$  tür?

Cevap:  $54\pi$

**Örnek:**

Bir ayrıtı 6 cm olan bir küpün içerisinde en büyük hacimli bir koni yerleştiriliyor.

**Koninin hacmi kaç  $\text{cm}^3$  tür?**

**Cevap:  $18\pi$**

**Örnek:**

Bir ayrıtı 6 cm olan bir küpün içerisinde en büyük hacimli bir küre yerleştiriliyor.

**Kürenin hacmi kaç  $\text{cm}^3$  tür?**

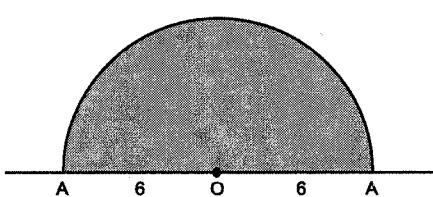
**Cevap:  $36\pi$**

**Örnek:**

Yarıçapı  $3\sqrt{3}$  olan bir kürenin içerisinde en büyük hacimli bir küp yerleştiriliyor.

**Küpün hacmi kaç  $\text{cm}^3$  tür?**

**Cevap: 216**

**Örnek:**

**Şekildeki yarıçapı 6 cm olan yarı daire [AB] etrafında  $360^\circ$  döndürülürse oluşan yeni şeklin hacmi kaç  $\text{cm}^3$  tür?**

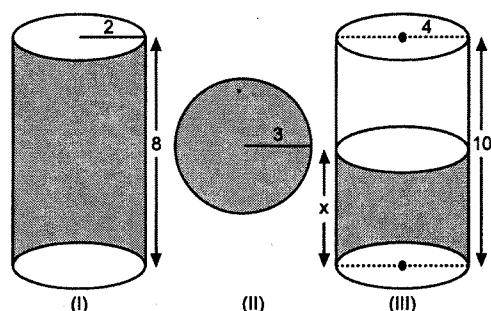
**Cevap:  $288\pi$**

**Örnek:**

Bir kenarı  $2\sqrt{3}$  cm yüksekliği 6 cm olan düzgün altıgen dik prizmanın içine en büyük hacimli bir küre yerleştiriliyor.

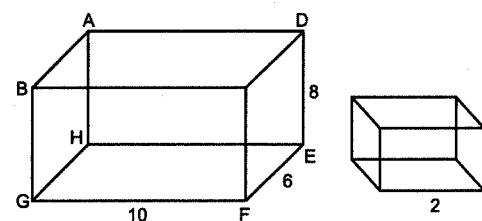
**Bu kürenin hacmi kaç  $\text{cm}^3$  tür?**

**Cevap:  $36\pi$**

**Örnek:**

Şekil I ve Şekil II deki katı cisimler Şekil III'e boşaltılıyor. x uzunluğu kaç cm olur?

**Cevap:  $\frac{17}{4}$**

**Örnek:**

Şekildeki dikdörtgenler prizmasını içeresine bir kenarı 2 cm olan küplerden 12 tane eritilerek boş olan prizmaya konuluyor.

**Prizmada biriken maddenin yüksekliği kaç cm olur?**

**Cevap:  $\frac{8}{5}$**

# PİRAMİT

## Düzgün Piramit:

Tabanı düzgün çokgen ve yüksekliği tabanın ağırlık merkezinden geçen piramite denir.

a) Yan yüzeyleri birbirine eş ikitenar üçgendir.

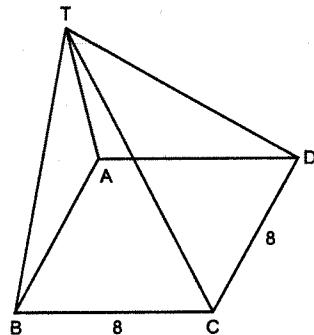
b) Yan ayrıtların uzunlukları eşittir.

$$c) \text{Yanal Alan} = \frac{\text{Taban çevresi} \times \text{Yanal yükseklik}}{2}$$

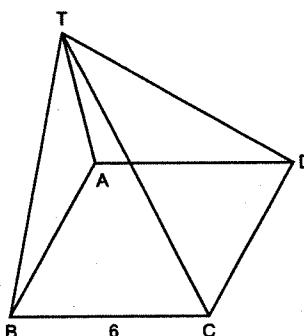
$$d) \text{Hacim} = \frac{\text{Taban alanı} \times \text{Yükseklik}}{3}$$

## Örnek:

Yanal Alanı  $80 \text{ cm}^2$  ise hacmi kaç  $\text{cm}^3$  tür?



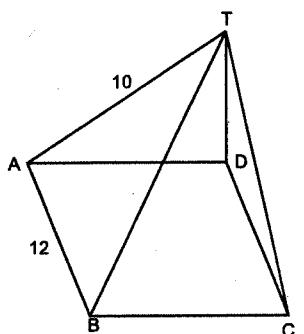
Cevap:  $64 \text{ cm}^3$



## Örnek:

Yüksekliği  $6 \text{ cm}$  olan düzgün kare piramidinin hacmi kaç  $\text{cm}^3$  tür?

Cevap: 72



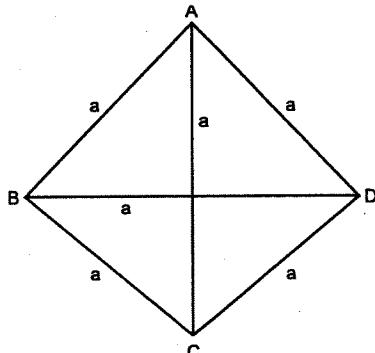
## Örnek:

Sekildeki düzgün kare piramidinin hacmi kaç  $\text{cm}^3$  tür?

Cevap:  $96\sqrt{7}$

## Düzgün Dörtyüzlü:

Tüm yüzeyleri birer eşkenar üçgen olan piramide denir.



$$\text{Alanı} = 4 \text{ eşkenar üçgenin alanı} = \frac{a^2\sqrt{3}}{4} \cdot 4 = a^2\sqrt{3}$$

$$\text{Hacim} = \frac{a^3\sqrt{2}}{12} \text{ dir.} = \frac{\text{Taban Alanı} \times \text{yükseklik}}{3}$$

$$\text{Yükseklik} = \frac{a\sqrt{6}}{3}$$

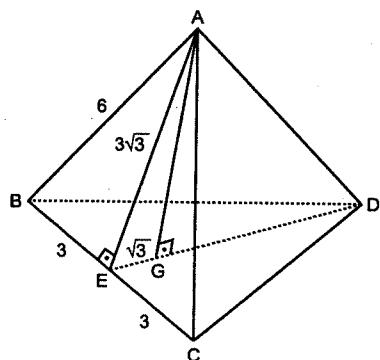
$$\frac{a^2\sqrt{3}}{4} \cdot \frac{a\sqrt{6}}{3} = \frac{a^3\sqrt{2}}{12} = V$$

**Örnek:**

Bir kenarı 6 cm olan düzgün dörtyüzlünün hacmi kaç  $\text{cm}^3$  tür?

Cevap:  $18\sqrt{2}$

**Çözüm:**



G:BCD nin ağırlık merkezi

$$|AE|^2 + 3^2 = 6^2$$

$$|AE| = 3\sqrt{3}$$

[DE] ⊥ [BC] olur. (Üç dikme Teoremi)

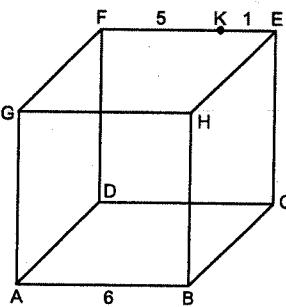
$$|AG|^2 + (\sqrt{3})^2 = (3\sqrt{3})^2 \Rightarrow |AG| = 2\sqrt{6}$$

$$V = \frac{\text{Taban Alanı} \times \text{Yükseklik}}{3} = \frac{6^2\sqrt{3}}{4} \cdot \frac{2\sqrt{6}}{3}$$

$$V = 18\sqrt{2}$$

$$\text{Formül: } k \Rightarrow V = \frac{a^3\sqrt{2}}{12} = \frac{6^3\sqrt{2}}{12} = 18\sqrt{2}$$

**Örnek:**

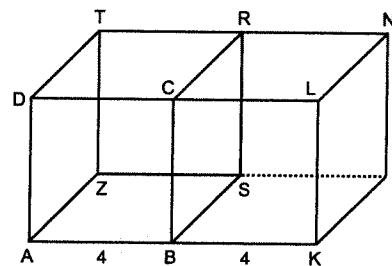


Bir ayrıtı 6 cm olan bir küp için; A noktasından başlayarak.

ABHG ve GHEF yüzeylerinden hareket eden bir karınca K noktasına en kısa kaç cm giderek ulaşır?

Cevap: 13

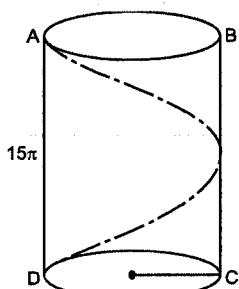
**Örnek:**



Şekildeki ayrıları 4 cm olan küpler için. A noktasından hareket eden bir karınca N noktasına en kısa kaç cm de ulaşır?

Cevap:  $8\sqrt{2}$

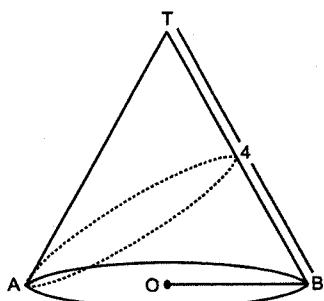
Örnek:



Yarıçapı 4 cm ve yüksekliği  $15\pi$  olan bir silindir için A noktasından D noktasına hareket eden bir karıncanın silindiri bir tam döner alacağı en kısa yol kaç cm dir?

Cevap:  $17\pi$ 

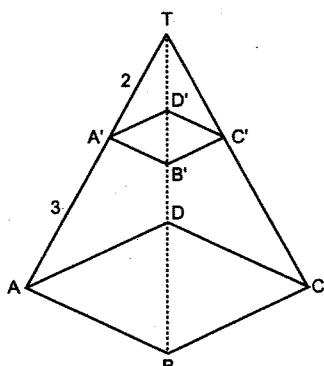
Örnek:



Yarıçapı 1 cm ve ana doğrusu 4 cm olan bir dik koni için A noktasından hareket ederek. Koninin etrafını bir tam dönen bir karıncanın alacağı en kısa yol kaçtır?

Cevap:  $4\sqrt{2}$ 

Örnek:

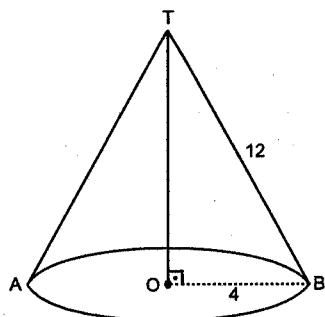


Şekildeki kare dik piramid için ABCD düzlemini A'B'C'D' düzlemine paraleldir.

(T, A'B'C'D') piramidinin hacminin (T, ABCD) piramidinin hacmine oranı kaçtır?

Cevap:  $\frac{8}{125}$ 

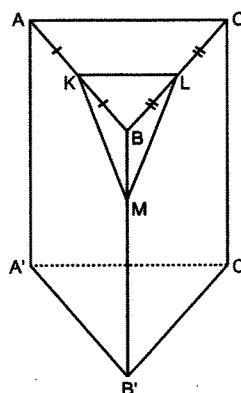
Örnek:



Şekildeki yarıçapı 4 cm ve ana doğrusu 12 cm olan bir dik koninin A köşesinden başlayan bir karıncada B noktasına en kısa kaç cm de ulaşır?

Cevap: 12

Örnek:



Şekildeki üçgen dik prizmanın [AB], [BC] ve [BB'] doğrularının orta noktaları K, L, M dir.

(M, KBL) piramidinin hacminin üçgen prizmanın hacmine oranı kaçtır?

Cevap:  $\frac{1}{24}$

**Notlar:** .....